

MultiHiggs Workshop

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**Inert Doublet Model
and
Strong First Order Phase Transition**

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Plan

General introduction

Higgs and Dark sector in IDM

Different phases of Universe

Thermal T2 evolution (short)

Beyond T2 evolution

(effective potential approach)

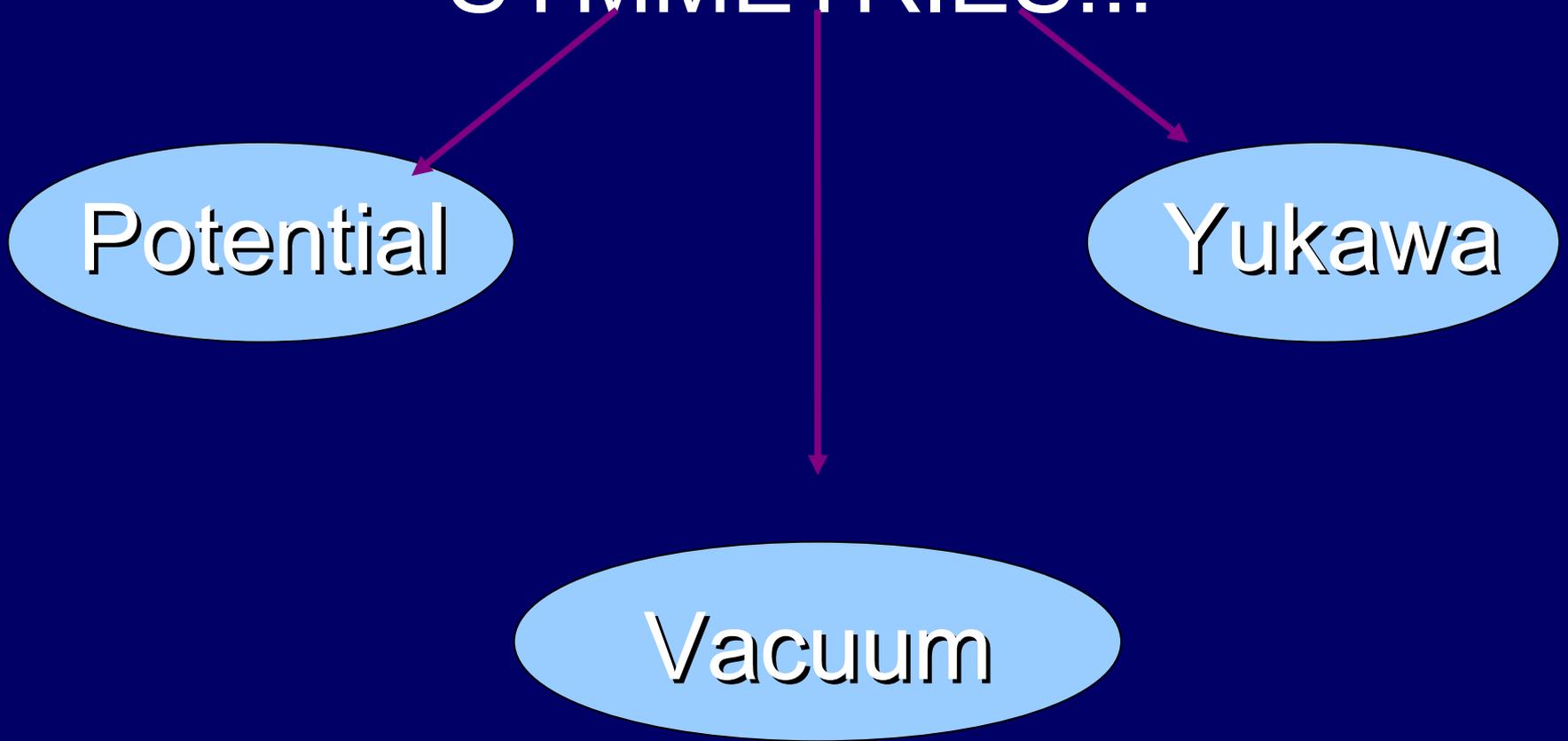
→ strength of the phase transition
towards electroweak baryogenesis

2HDM- great laboratory of BSM

- Inert Doublet Model (IDM) provides DM and it is in agreement with present astrophysical and collider data including the 125 GeV Higgs boson
- If today ($T=0$) Universe in the Inert phase what was in the past ?
- We have studied temperature dependent Z_2 sym. 2HDM potential \rightarrow evolution of the inert vacuum and sequences of different vacua in the past (one, two and three phase transitions)
 - with leading T^2 corrections (only $m_{ij}^2 (T^2)$)
(PRD 82(2010) GKKS, I. Ginzburg and D. Sokołowska talks here)
 - beyond T^2 corrections (to find strong enough first-order phase transition needed for baryogenesis)
(G. Gil Thesis'2011, G.Gil, P. Chankowski, MK 1207.0084 [hep-ph])

2HDM's

SYMMETRIES!!!



Various models of Yukawa inter.

typically with some Z_2 type symmetry to avoid FCNC

Model I - only one doublet interacts with fermions

Model II - one doublet with down-type fermions d, l
other with up-type fermions u

Model III - both doublets interact with fermions

Model IV (X) - leptons interact with one
doublet, quarks with the other

Model Y - one doublet with down-type quarks d

other with up-type quarks u and leptons

Top 2HDM - top only with one doublet

Fermiophobic 2HDM - no coupling to the lightest Higgs

+ Extra dim 2HDM models

2HDM Potential (Lee'73)

$$\begin{aligned} V = & \frac{1}{2}\lambda_1(\Phi_1^\dagger\Phi_1)^2 + \frac{1}{2}\lambda_2(\Phi_2^\dagger\Phi_2)^2 + \lambda_3(\Phi_1^\dagger\Phi_1)(\Phi_2^\dagger\Phi_2) \\ & + \lambda_4(\Phi_1^\dagger\Phi_2)(\Phi_2^\dagger\Phi_1) + \frac{1}{2} [\lambda_5(\Phi_1^\dagger\Phi_2)^2 + \text{h.c.}] \\ & + [(\lambda_6(\Phi_1^\dagger\Phi_1) + \lambda_7(\Phi_2^\dagger\Phi_2))(\Phi_1^\dagger\Phi_2) + \text{h.c.}] \\ & - \frac{1}{2}m_{11}^2(\Phi_1^\dagger\Phi_1) - \frac{1}{2}m_{22}^2(\Phi_2^\dagger\Phi_2) - \frac{1}{2}[m_{12}^2(\Phi_1^\dagger\Phi_2) + \text{h.c.}] \end{aligned}$$

Z_2 symmetry transformation: $\Phi_1 \rightarrow \Phi_1$ $\Phi_2 \rightarrow -\Phi_2$

Hard Z_2 symmetry violation: λ_6, λ_7 terms

Soft Z_2 symmetry violation: m_{12}^2 term (Re $m_{12}^2 = \mu^2$)

Explicit Z_2 symmetry in V : $\lambda_6, \lambda_7, m_{12}^2 = 0$

Possible extrema (vacuum) states

The most general state for V with explicit Z_2

$$\langle \phi_S \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_S \end{pmatrix}, \quad \langle \phi_D \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} u \\ v_D \end{pmatrix}$$

v_S, v_D, u - real
 $v_S, u \geq 0$

$v^2 = v_S^2 + v_D^2 + u^2 = (246 \text{ GeV})^2$

EWs	EWs	$u = 0$	$v_D = v_S = 0$
Inert	I_1	$u = 0$	$v_D = 0$
Inert-like	I_2	$u = 0$	$v_S = 0$
Mixed (Normal, MSSM like)	M	$u = 0$	
Charge Breaking	Ch	$u \neq 0$	$v_D = 0$

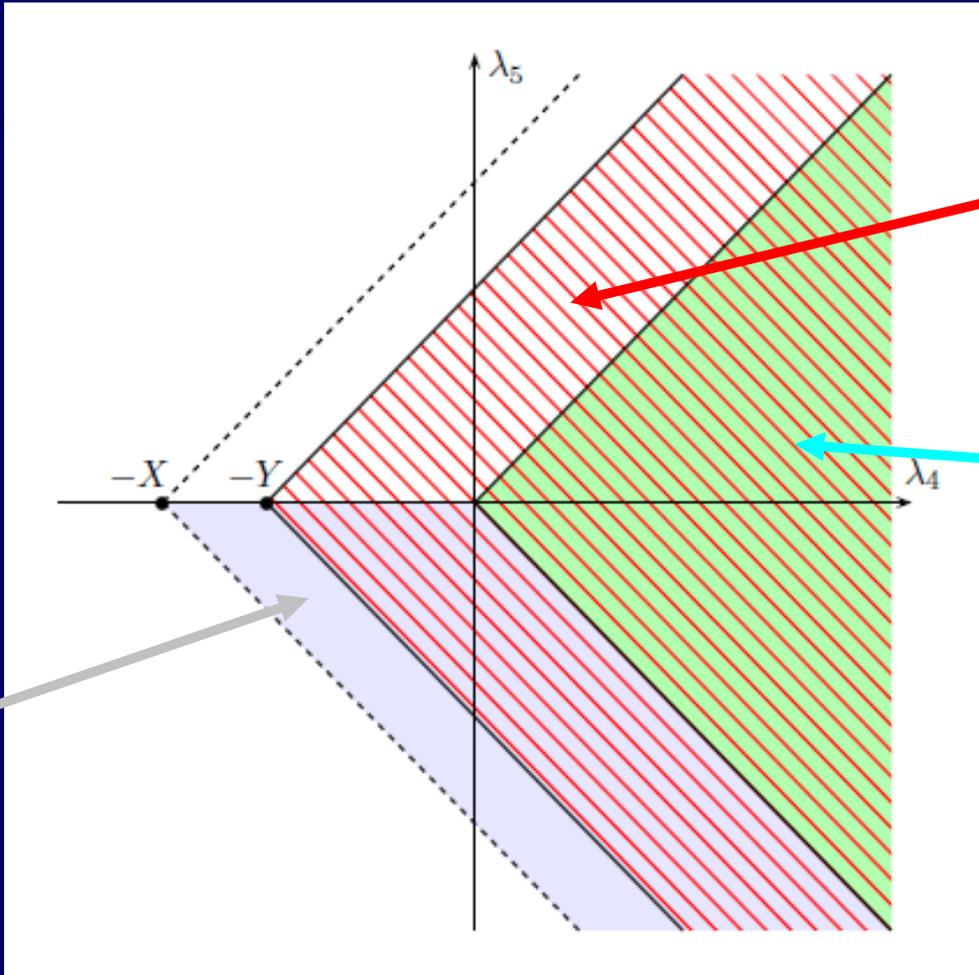
Various extrema (vacua) on (λ_4, λ_5) plane

Positivity constrains: $\lambda_4 \pm \lambda_5 > -X$ $X = \sqrt{\lambda_1 \lambda_2 + \lambda_3} > 0$

Inert (Inert-like)
 $Y = M_{H^+}^2 2/v^2$

Charge
Breaking Ch

Mixed



Note the overlap of the Inert with M and Ch !

TODAY

2HDM with explicit Z_2 (D) symmetry

$$\Phi_S \rightarrow \Phi_S \quad \Phi_D \rightarrow -\Phi_D$$

Model I (Yukawa int. with Φ_S only)

- Charge breaking phase Ch?
photon is massive, el.charge is not conserved...
→ No
- Neutral phases:
 - Mixed M ok, many data, but no DM
 - Inert I1 OK! In agreement with accelerator and astrophysical data (neutral DM)
 - Inert-like I2 No, all fermions massless, no DM

Inert Doublet Model

Ma'78

Barbieri'06

Symmetry under Z_2 transf. $\Phi_S \rightarrow \Phi_S$ $\Phi_D \rightarrow -\Phi_D$
both in L (V and Yukawa interaction = Model I only Φ_S)
and in the vacuum:

$$\langle \Phi_S \rangle = v$$

$$\langle \Phi_D \rangle = 0$$

Inert
vacuum I_1

Today?

Φ_S as in SM (BEH), with Higgs boson h (SM-like)

Φ_D has no vev, with 4 scalars (no Higgs bosons!)

no interaction with fermions (inert doublet)

Here Z_2 symmetry exact $\rightarrow Z_2$ parity, only Φ_D has odd Z_2 -parity
 \rightarrow The lightest scalar stable -a dark matter candidate
(Φ_D dark doublet with dark scalars).

$\Phi_1 \rightarrow \Phi_S$ Higgs doublet S

$\Phi_2 \rightarrow \Phi_D$ Dark doublet D

Constraining Inert Doublet Model

- Positivity, extrema, vacua, pert. unitarity, S, T
- By considering properties of *(Ma'2006,..B. Świeżewska, Thesis2011, 1112.4356, 1112.5086[hep-ph] and talk)*
 - the SM-like h, $M_h^2 = m_{11}^2 = \lambda_1 v^2$
 - the dark scalars D always in pairs!

$$\begin{aligned}
 M_{H^+}^2 &= -\frac{m_{22}^2}{2} + \frac{\lambda_3 v^2}{2} \\
 M_H^2 &= -\frac{m_{22}^2}{2} + \frac{\lambda_3 + \lambda_4 + \lambda_5 v^2}{2} \\
 M_A^2 &= -\frac{m_{22}^2}{2} + \frac{\lambda_3 + \lambda_4 - \lambda_5 v^2}{2}
 \end{aligned}$$

λ_{345}

D couple to $V = W/Z$ (eg. AZH, H^-W^+H), not DVV !

Quartic selfcouplings D^4 proportional to λ_2

hopeless to be measured at colliders! ($\rightarrow D. Sokołowska$ talk)

Couplings with Higgs: $hHH \sim \lambda_{345}$ $h H^+H^- \sim \lambda_3$

Evolution of the Universe in 2HDM– through different vacua in the past

Ginzburg, Ivanov, Kanishev 2009

Ginzburg, Kanishev, Krawczyk,

Sokołowska 2010, Sokołowska 2011

We consider 2HDM with an explicit $D (Z_2)$ symmetry assuming that today the **Inert Doublet Model** describes reality

Yukawa interaction – Model I \rightarrow

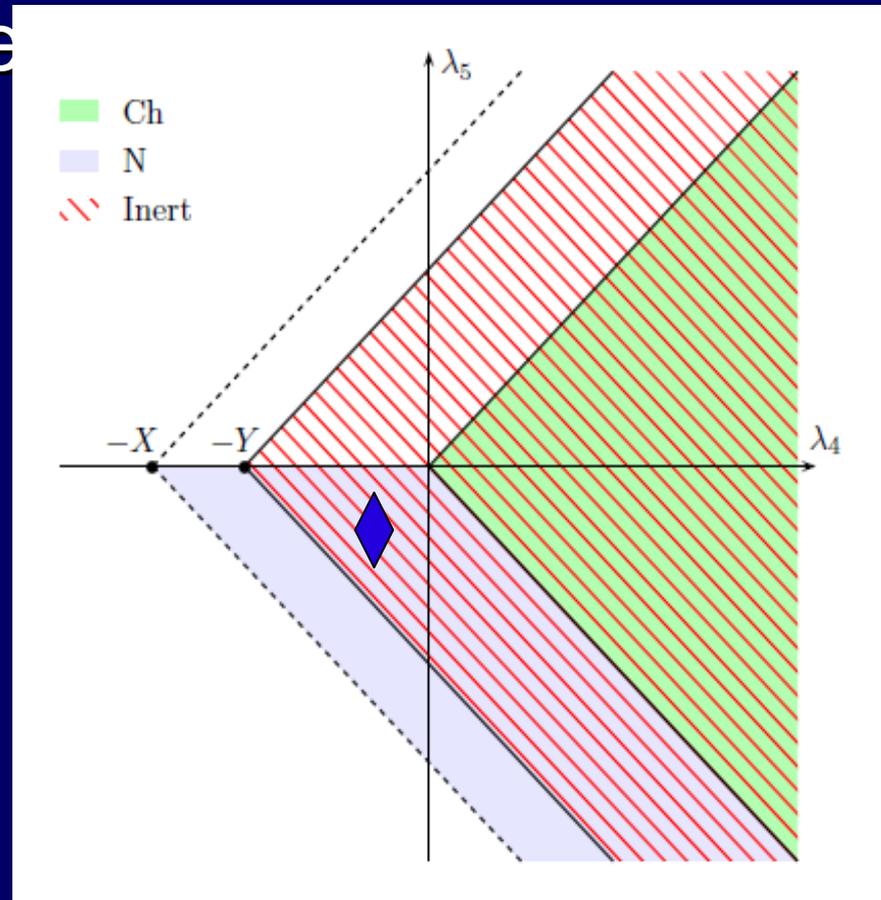
all fermions couple only to Φ_S

From the EW symmetric phase to the INERT phase in T2 approximation

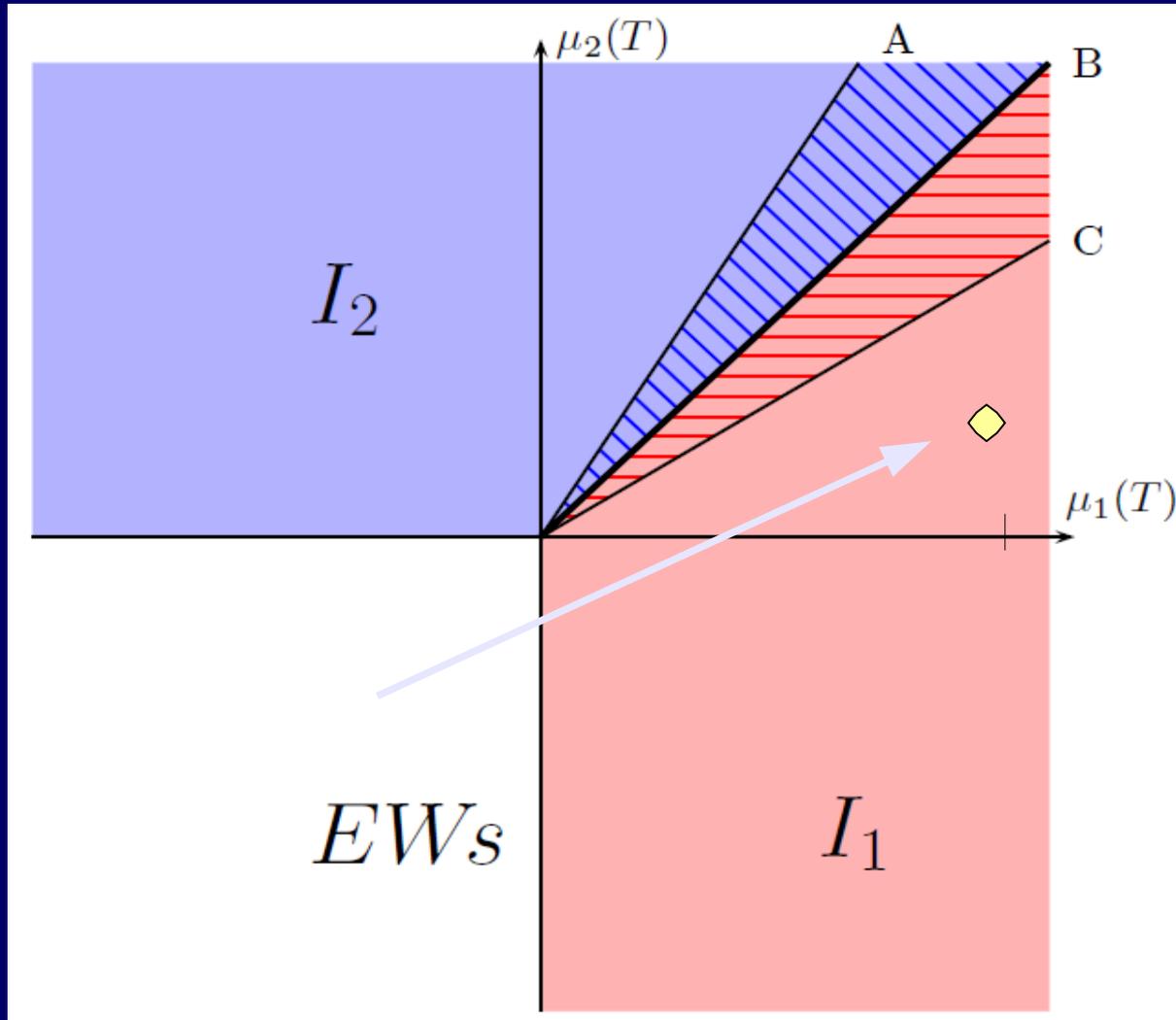
In the simplest T2 approximation only *mass terms* in V vary with temperature like T^2 , while *lambdas* are fixed

Various scenarios possible in one, two or three steps, with 1st or 2nd type phase transitions → *Sokołowska talk*

Ginzburg, Kanishev, MK,
Sokołowska Phys. Rev D 2010



Phase diagram (μ_1, μ_2)



$$\mu_i = m_{ii}^2 / \sqrt{\lambda_i}$$

$$R + 1 > 0$$

Stability condition

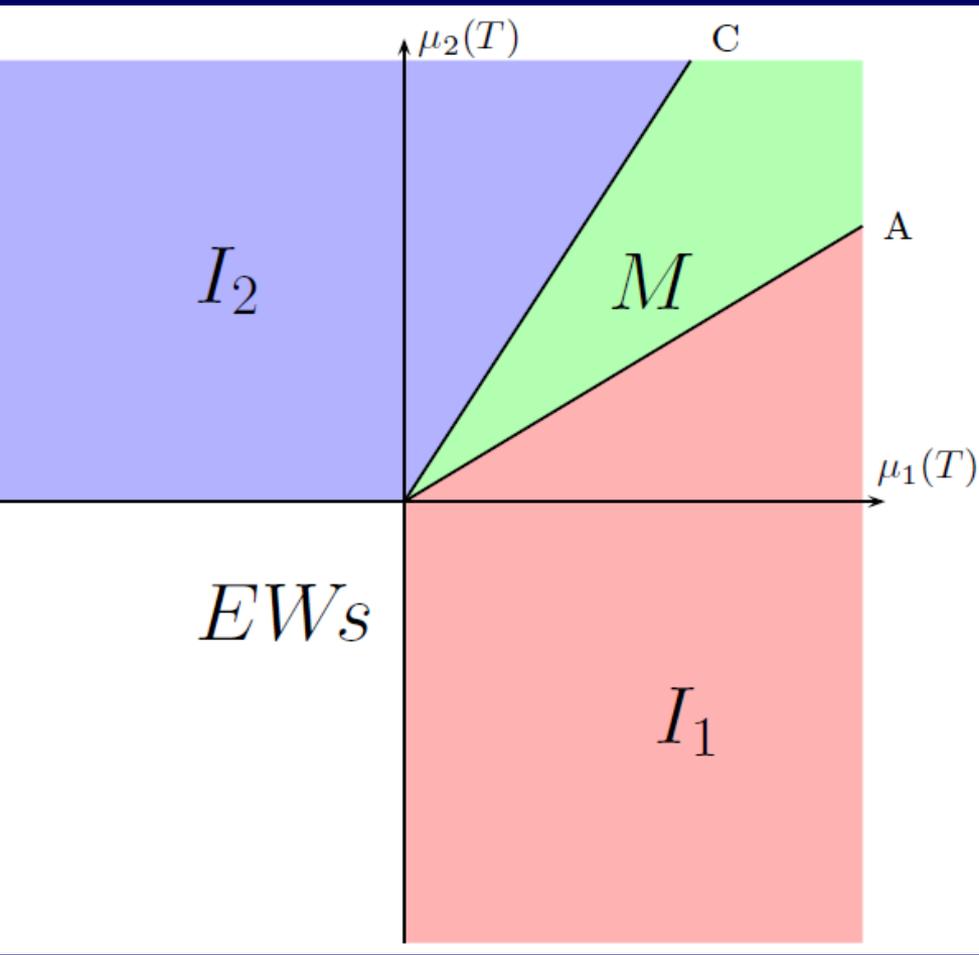
$$R = \frac{\lambda_{345}}{\sqrt{\lambda_1 \lambda_2}}$$

3 regions of R

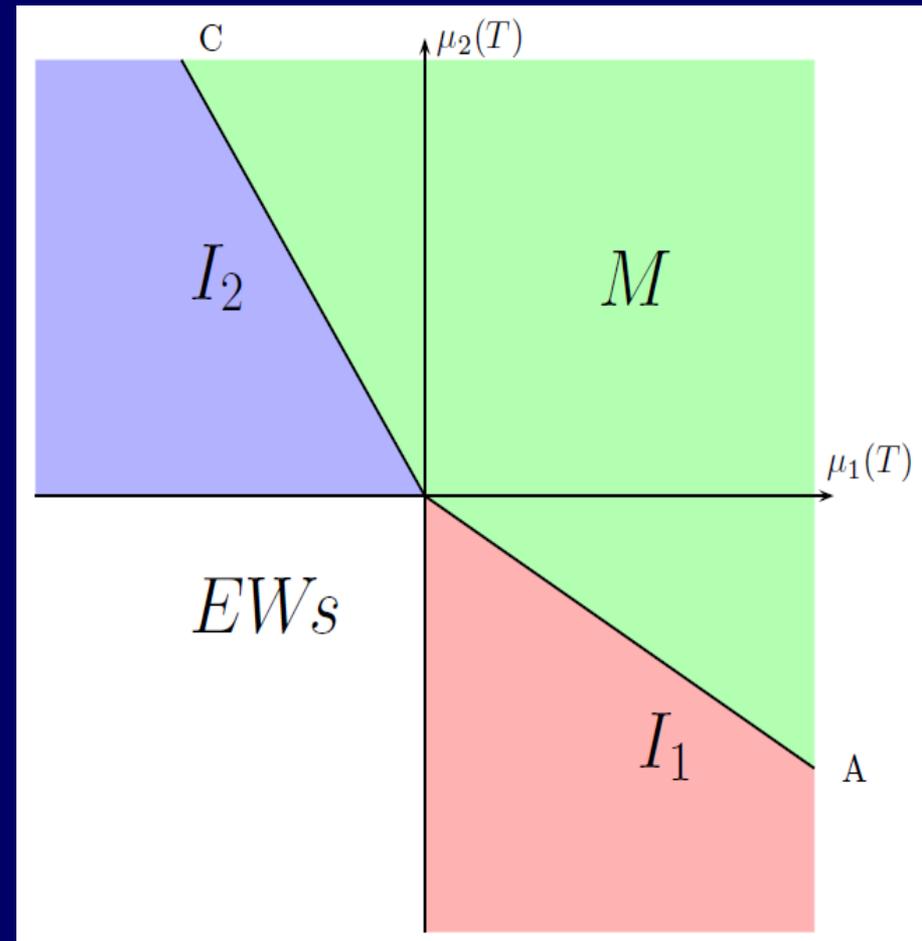
T2 corrections
 \rightarrow rays from
 EW s to Inert
 phase

$R > 1$

Phase diagrams



$$1 > R > 0$$



$$0 > R > -1$$

Transitions to the Inert phase beyond T2 corrections

We applied one-loop effective potential at $T=0$ (Coleman-Wienberg term) and temperature dependent effective potential at $T \neq 0$ (with sum of ring diagrams)

$$V_T^{(1L)}(v_1, v_2) = V_{\text{eff}}^{(1L)}(v_1, v_2) + \Delta^{(1L)} V_{T \neq 0}(v_1, v_2).$$

The one-loop effective potential $V_{\text{eff}}(v_1, v_2)$ is given in the Landau gauge by standard formula

$$V_{\text{eff}}^{(1L)} = V_{\text{tree}} + \frac{1}{64\pi^2} \sum_{\text{fields}} C_s \left\{ \mathcal{M}_s^4 \left(\ln \frac{\mathcal{M}_s^2}{4\pi\mu^2} - \frac{3}{2} + \frac{2}{d-2} - \gamma_E \right) \right\} + \text{CT},$$

number of states

counter terms →

Fixing counterterms

We require that $v_1 = v_1(\text{tree})$

and that h field propagator has a pole for tree-level mass-squared M_h^2

Then we put conditions on λ_{345} (hHH), λ_2 (HHHH)

On the other hand λ_2 cannot be directly measured in the foreseeable future⁶ so its precise definition at the loop-level is not important. Here for simplicity we choose to subtract the divergences of $V_{\text{eff}}^{(1L)}$ proportional to v_2^4 and $v_1^2 v_2^2$ using the $\overline{\text{MS}}$ scheme. This fixes the combinations $\delta\lambda_2 + 2\lambda_2\delta Z_2$ and $\delta\lambda_{345} + \lambda_{345}(\delta Z_1 + \delta Z_2)$. Once the latter counterterm is fixed the last necessary combination $\delta m_{22}^2 + m_{22}^2\delta Z_2$ is determined by renormalizing the H^0 propagator on-shell. The counterterms $\delta\lambda_3$ and $\delta\lambda_5$ can be then used to enforce that the tree-level masses M_{A^0} and M_{H^\pm} remain unchanged by one-loop corrections (they do not need to be determined explicitly).

One-loop temperature dependent effective potential

$$\Delta^{(1L)}V_{T \neq 0} = \frac{T^4}{2\pi^2} \sum_{\text{fields}} C_s \int_0^\infty dx x^2 \ln \left[1 - (-1)^{2s} \exp \left(-\sqrt{x^2 + \mathcal{M}_s^2/T^2} \right) \right].$$

For $T^2 \gg \mathcal{M}_s^2$ the contribution of \mathcal{M}_s^2 to (12) can be expanded:

$$(\Delta^{(1L)}V_{T \neq 0})_B = |C_s| \left\{ -\frac{\pi^2}{90} T^4 + \frac{1}{24} T^2 \mathcal{M}_s^2 - \frac{T}{12\pi} |\mathcal{M}_s^3| - \frac{\mathcal{M}_s^4}{64\pi^2} \left(\ln \frac{\mathcal{M}_s^2}{T^2} - C_B \right) \right\}$$

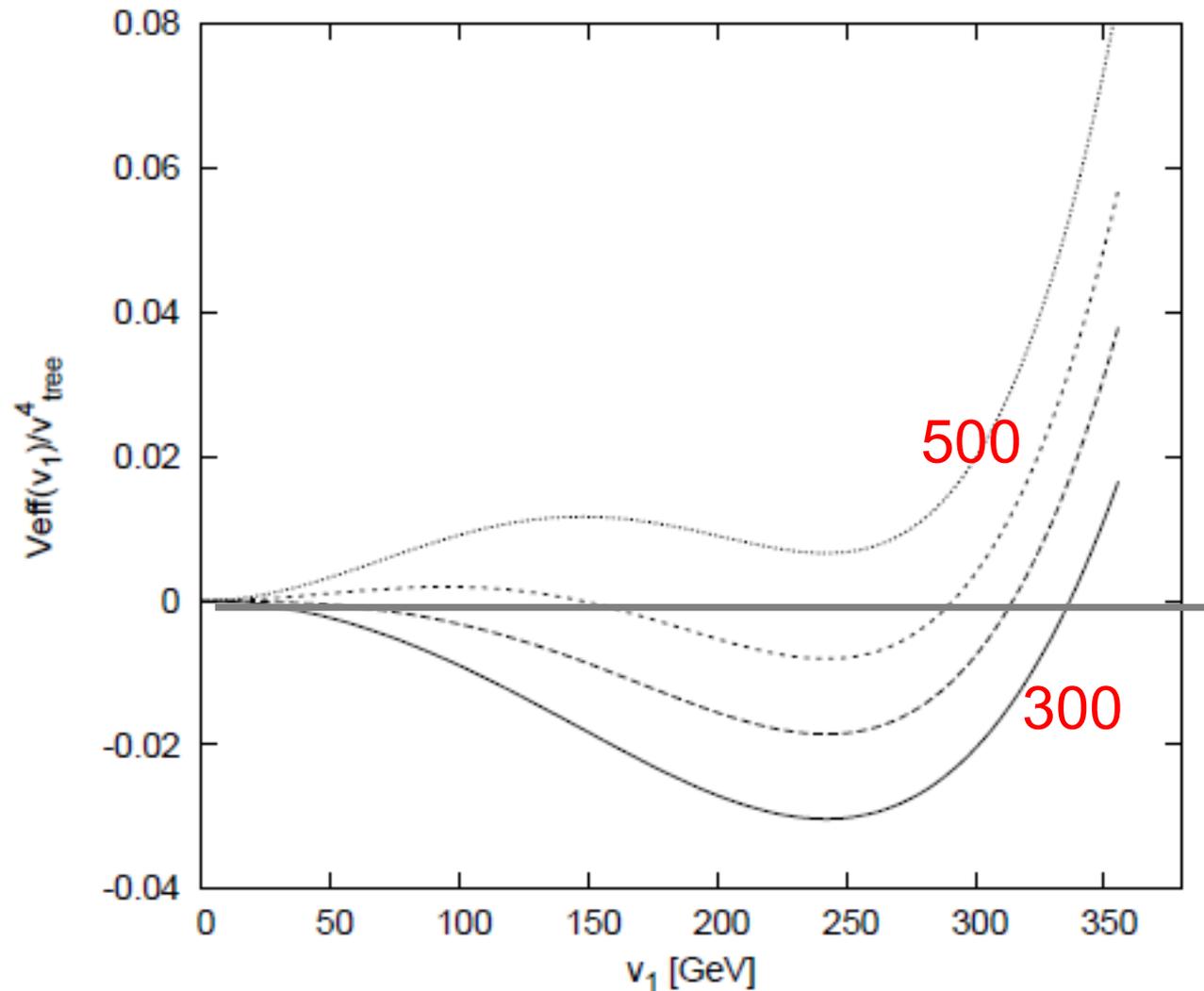
$$(\Delta^{(1L)}V_{T \neq 0})_F = |C_s| \left\{ -\frac{7\pi^2}{720} T^4 + \frac{1}{48} T^2 \mathcal{M}_s^2 + \frac{\mathcal{M}_s^4}{64\pi^2} \left(\ln \frac{\mathcal{M}_s^2}{T^2} - C_F \right) \right\}$$

($C_B = 5.40762$, $C_F = 2.63503$). In the opposite limit $T^2 \ll \mathcal{M}_s^2$ one has

$$(\Delta^{(1L)}V_{T \neq 0})_s = -|C_s| T^4 \left(\frac{|\mathcal{M}_s|}{2\pi T} \right)^{3/2} \left(1 + \frac{15}{8} \frac{T}{|\mathcal{M}_s|} + \dots \right) \exp \left(-\frac{|\mathcal{M}_s|}{T} \right),$$

both for B and F

Effective $T=0$ potential



$M_h = 125$ GeV

$M_H = 65$ GeV

$M_{H^\pm} = M_{A^0} =$
500, 450, 400, 300
GeV \tilde{V}

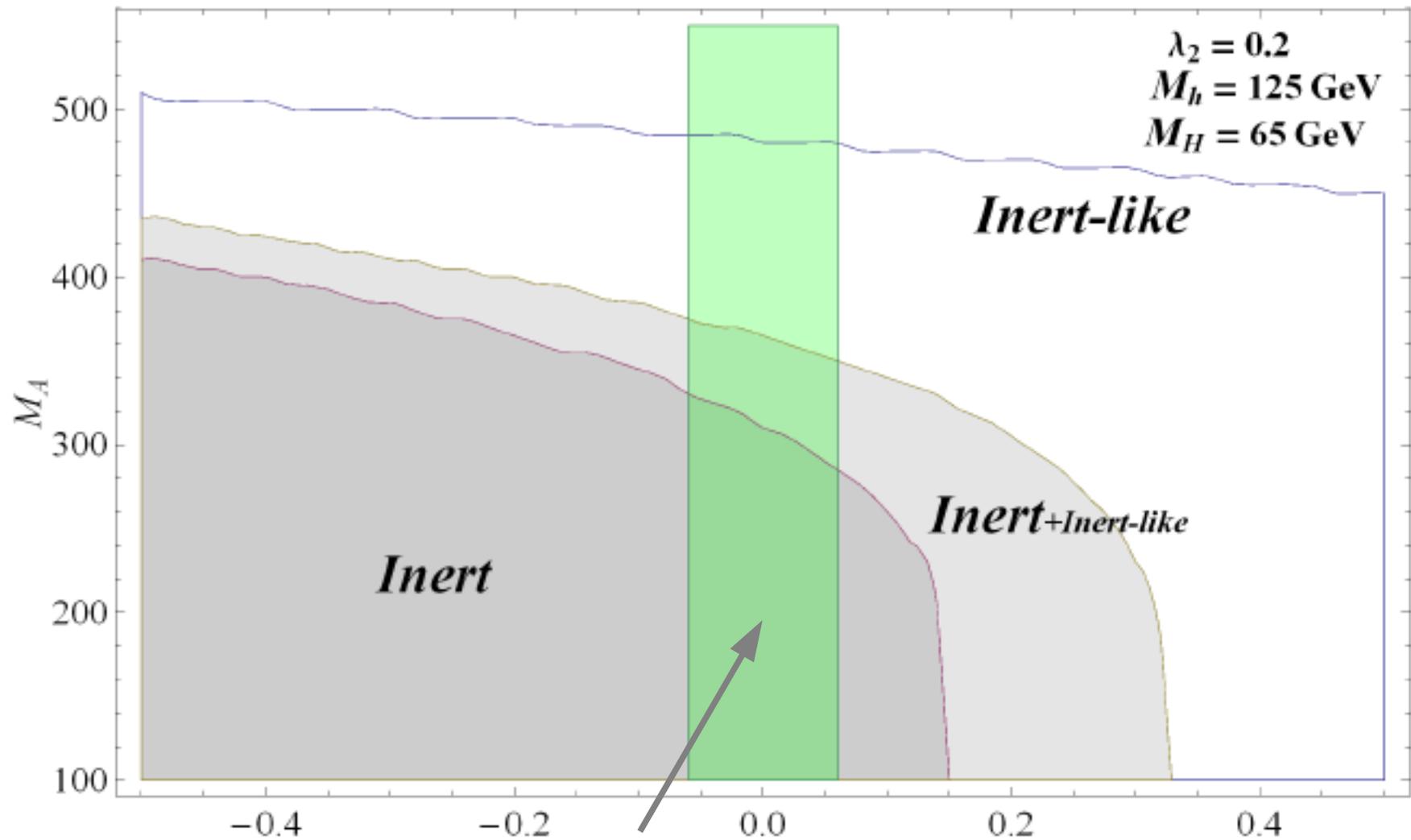
$\lambda_{345} = 0.2,$

$\lambda_2 = 0.2$

$v_{2(D)} = 0$

Critical temperature T_{EW} : V at new minimum = V at $v_{1(s)} = v_{2(D)} = 0$

Phases at T=0



Xenon100 bound

λ_{345}

Strength of the phase transition

$$v(T_{EW})/T_{EW}$$

We are looking for parameter space of IDM which allows for a strong first order phase transition

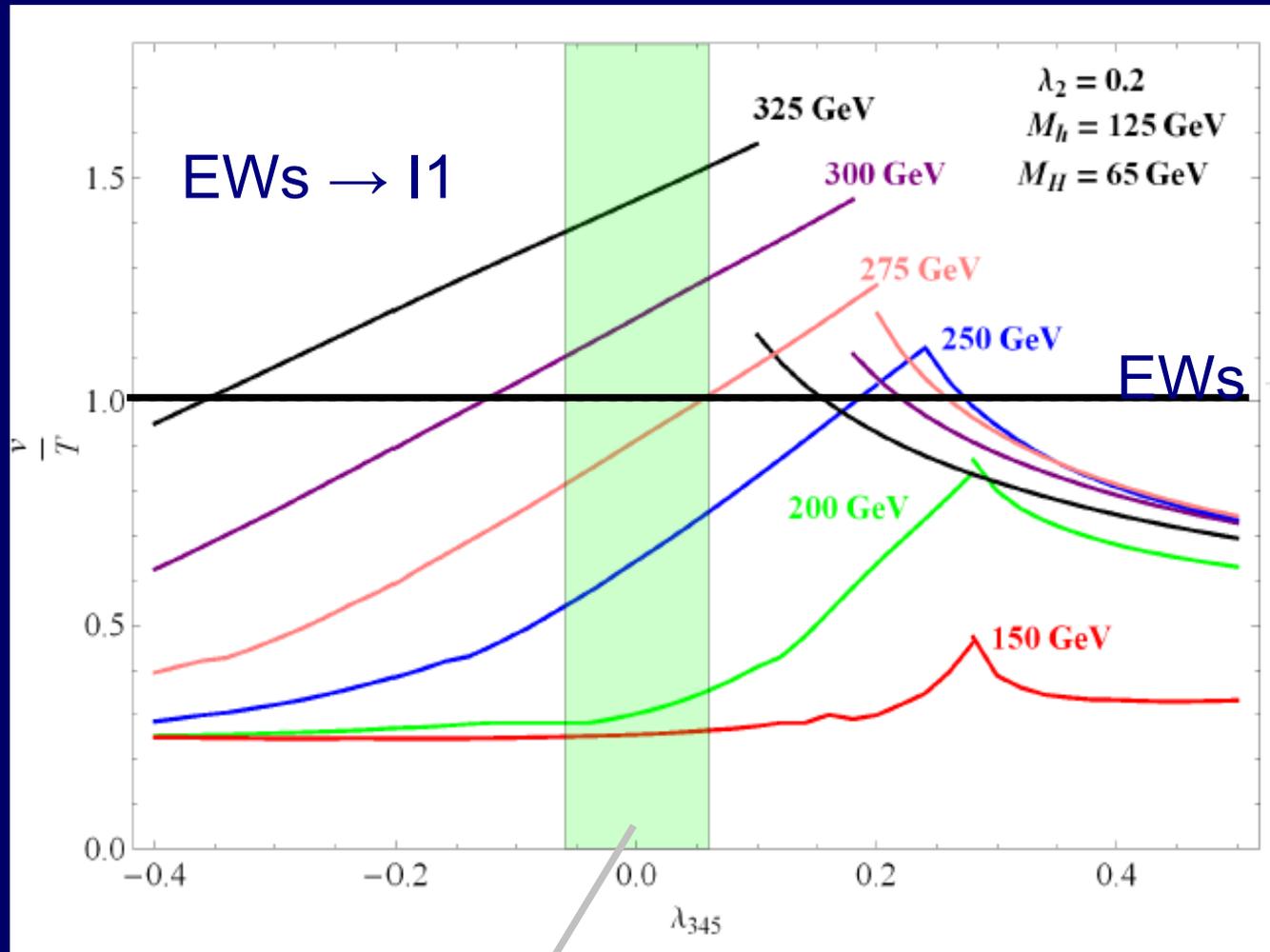
$$v(T_{EW})/T_{EW} > 1$$

being in agreement with collider and astrophysical data

We focus on medium DM, with $M_H \ll v$, heavy degenerated A and H⁺ and $M_h = 125$ GeV

Results for $v(T_{EW})/T_{EW}$

$M_h=125$ GeV, $M_H=65$ GeV, $\lambda_2=0.2$



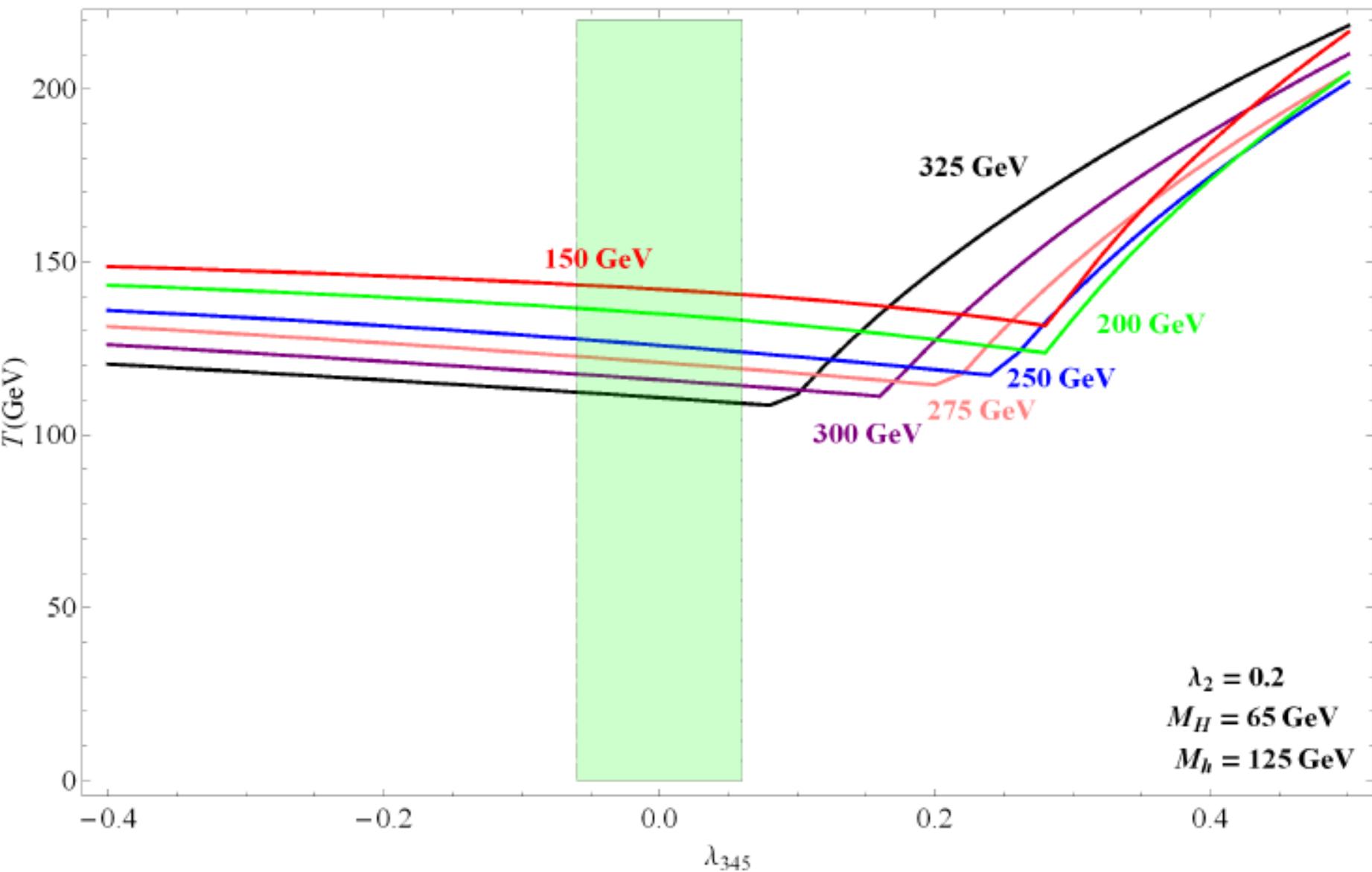
\rightarrow I2 \rightarrow I1

Allowed
MH+=MA
between 275
and 380 GeV
(one step)

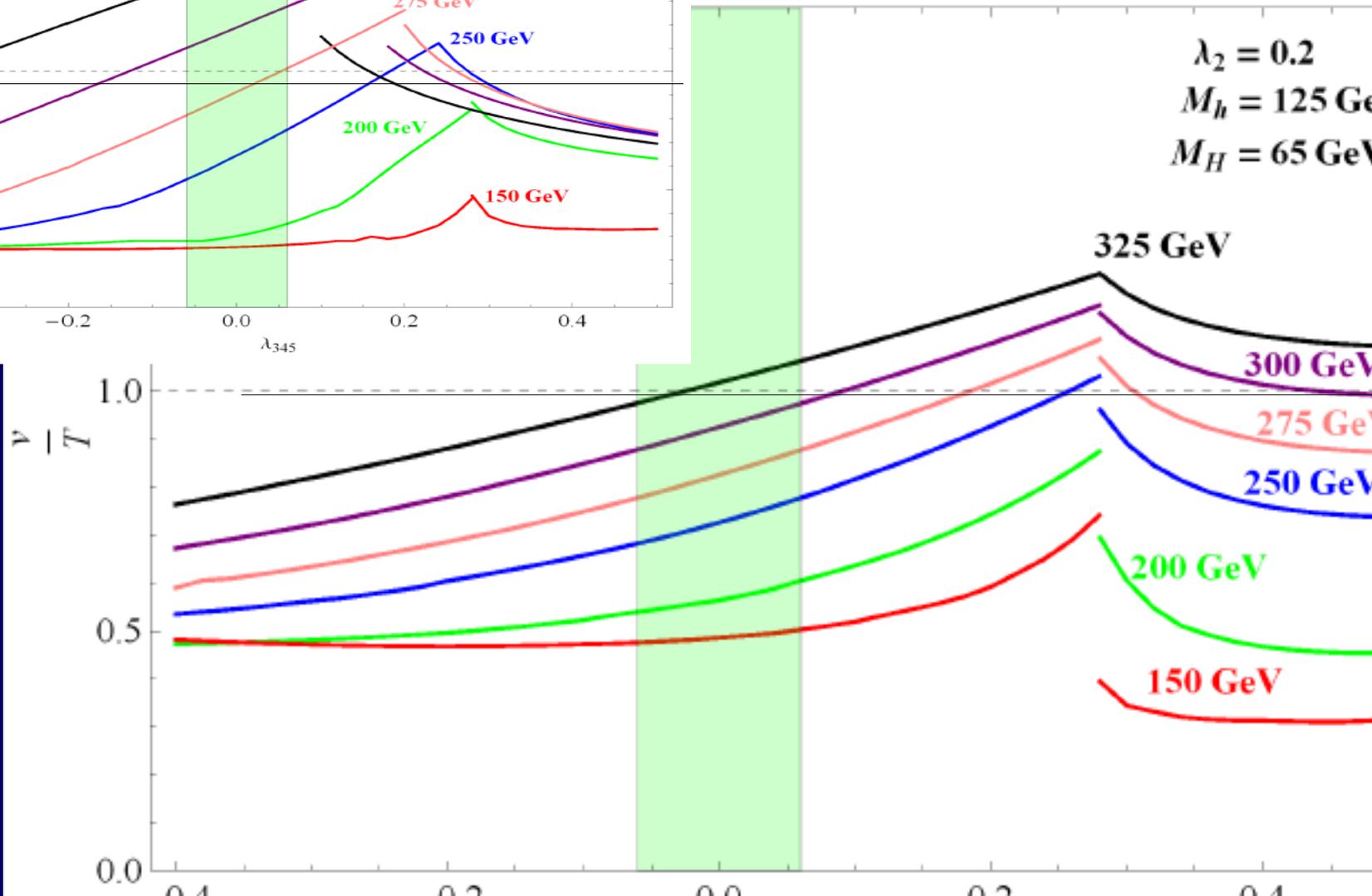
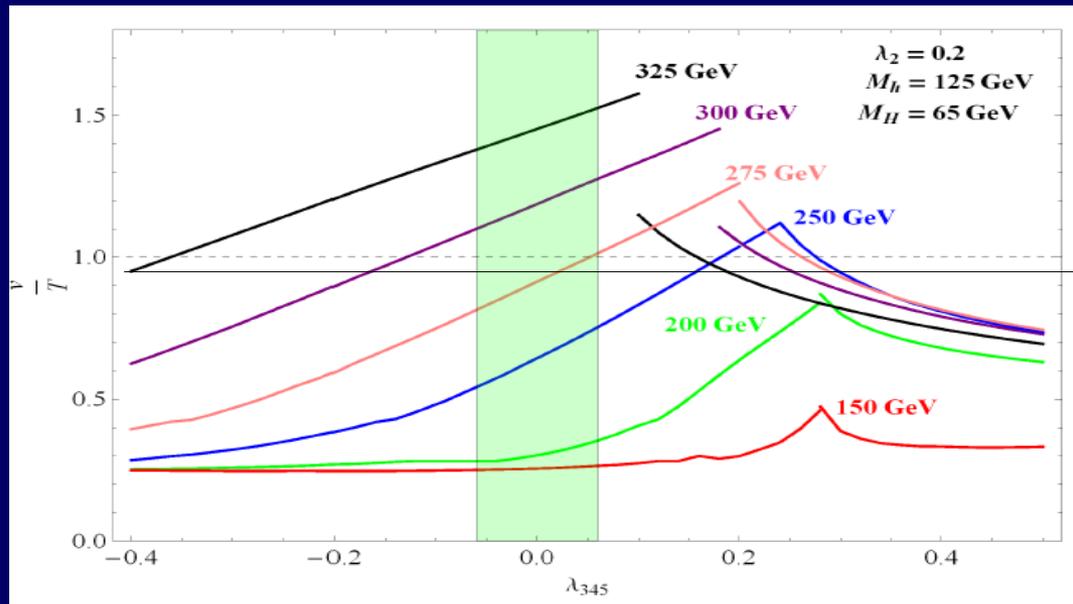
λ_{345}

Xenon100 bound

T_{EW} as a function of λ_{345}



Role of Coleman-Weinberg



Conclusion

Strong first order phase transition in IDM possible for realistic mass of Higgs boson (125 GeV)

and DM (~ 65 GeV) for

1/ heavy (degenerate) H^+ and A with mass 275 -380 GeV

2/ low value of hHH coupling $|\lambda_{345}| < 0.1$

3/ Coleman-Weinberg term important

Our results in agreement with recent papers on IDM

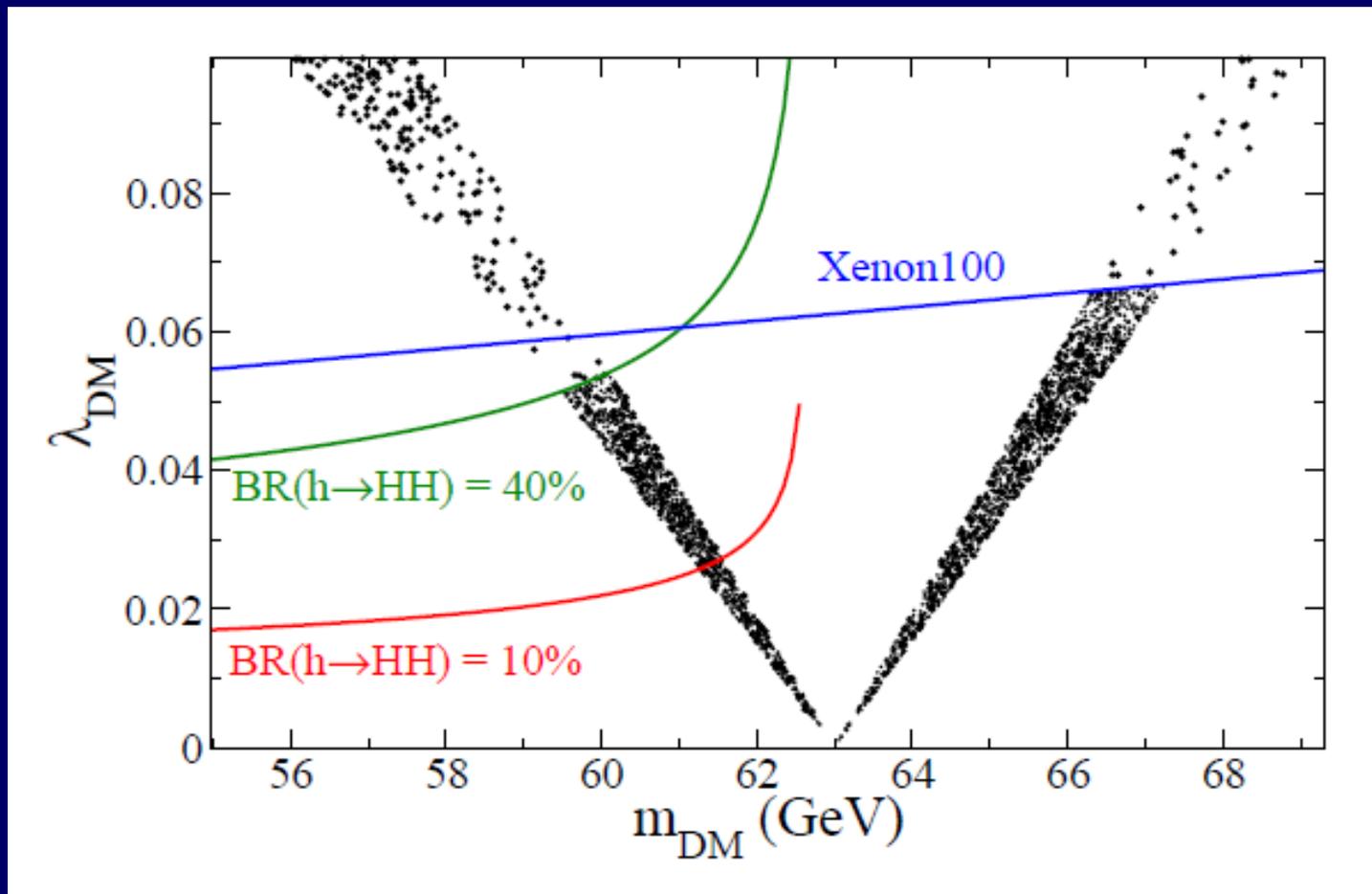
Borach, Cline 1204.4722

Chowdhury et al 1110.5334 (DM as a trigger of strong EW PT)

(on 2HDM Cline et al, 1107.3559 and Kozhusko..1106.0790)

D. Borach, J. Cline

Inert Doublet DM with Strong EW
phase transition 1204.4722[hep-ph]



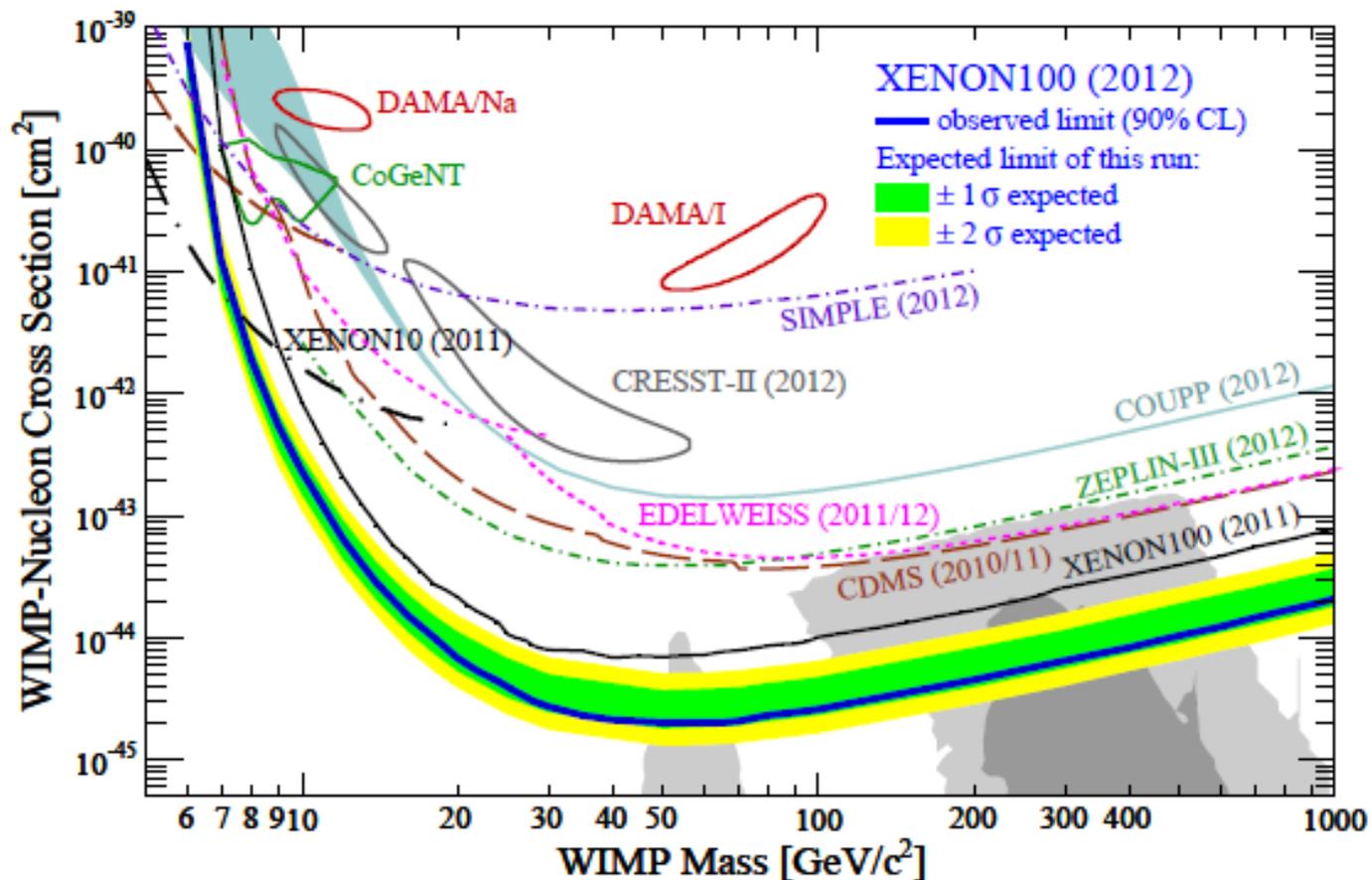


FIG. 3: New result on spin-independent WIMP-nucleon scattering from XENON100: The expected sensitivity of this run is shown by the green/yellow band ($1\sigma/2\sigma$) and the resulting exclusion limit (90% CL) in blue. For comparison, other experimental results are also shown [19–22], together with

Contour plot of $\Delta\lambda_{hhh}/\lambda_{hhh}$ and φ_c/T_c in the m_Φ - M plane

