

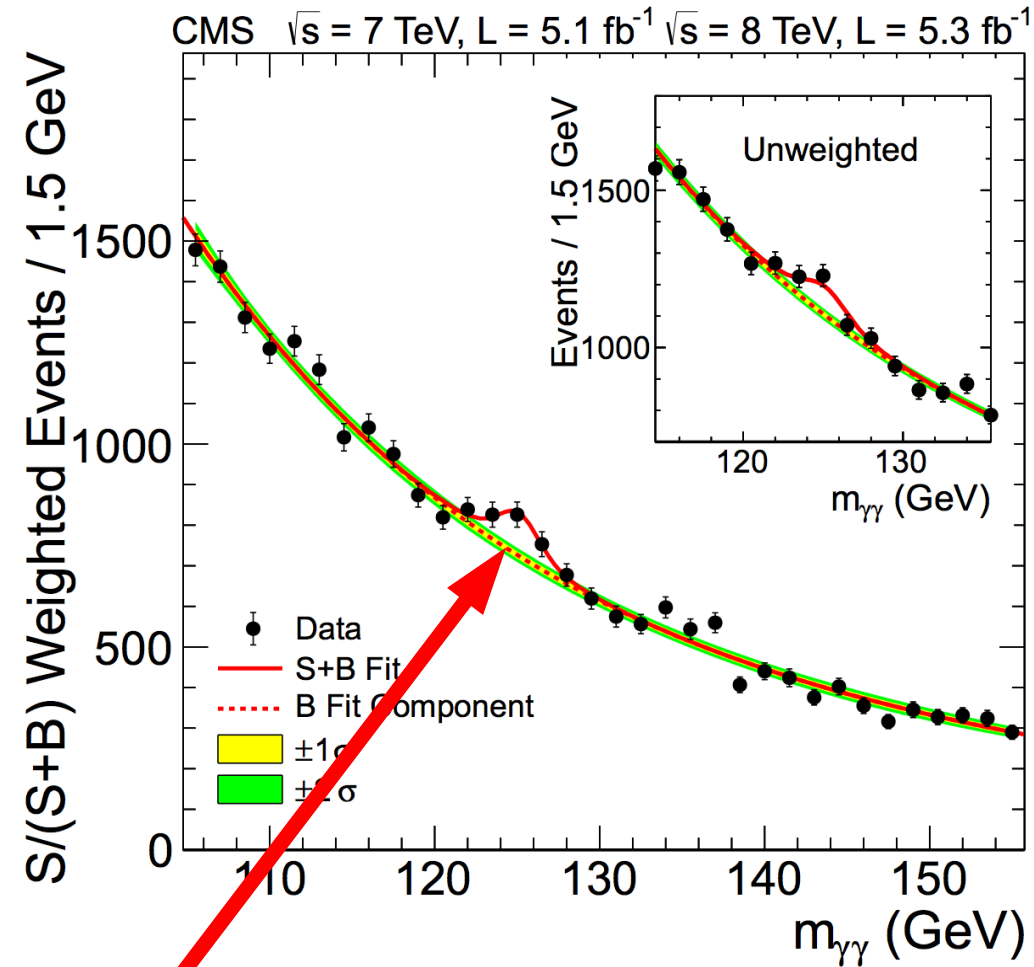
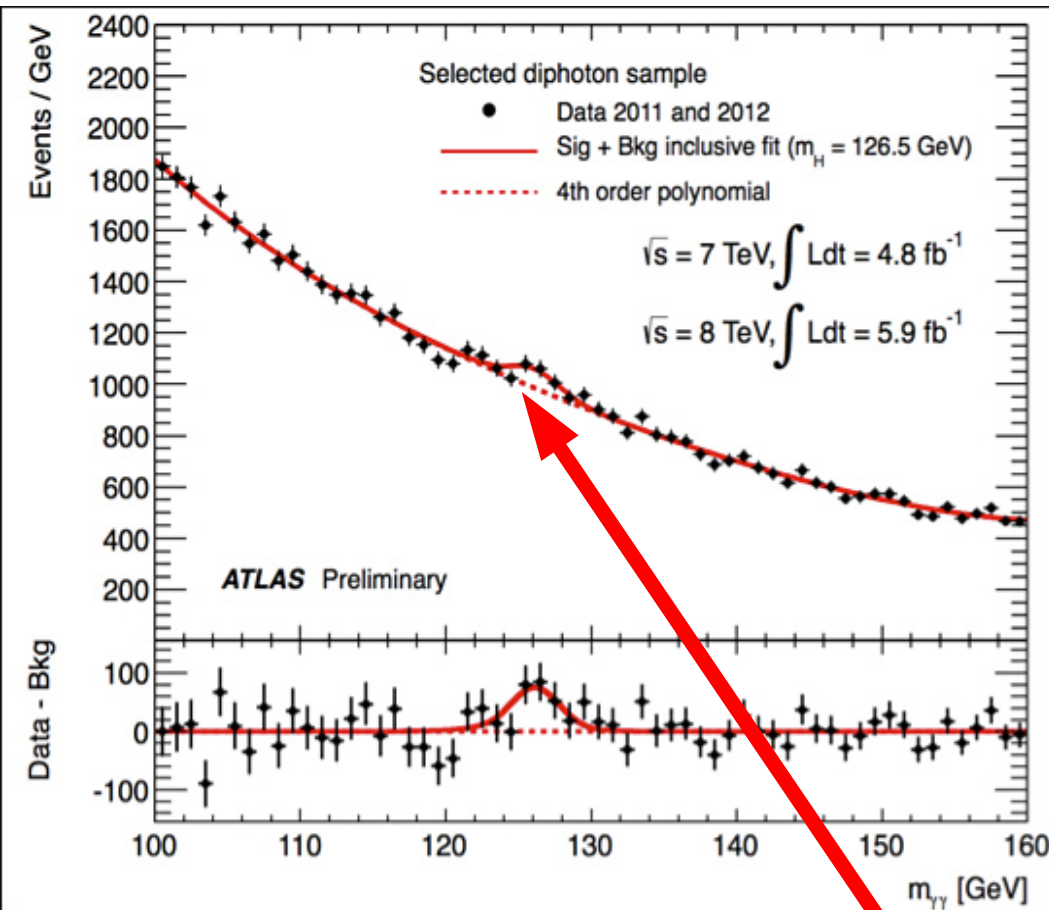
Discrimination possibility between composite and fundamental multi-Higgs doublet models with derivative interactions

Yasuhiro Yamamoto (U. Tokyo)

Based on
arXiv:1111.2120 with Y. Kikuta and Y. Okada
and succeeding works with Y. Kikuta

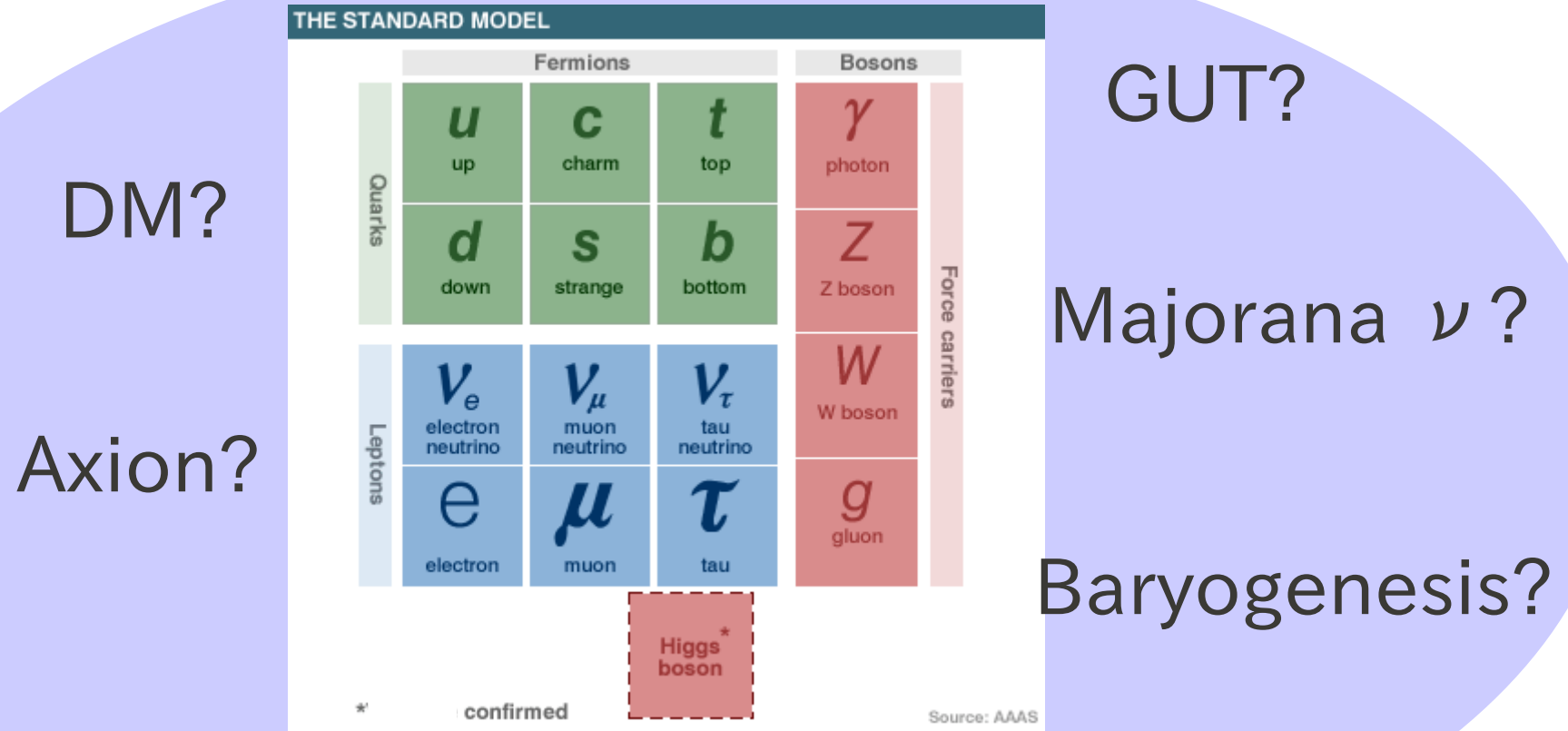
@ Workshop on Multi-Higgs Models,
Aug. 2012, Lisbon

The Higgs (?) boson is discovered!!



SM Higgs like resonance

The Standard Model is established!!



Beyond the Standard Model

Where is the new scale?

How to break the EW symmetry.

By hand in the SM



$$V = -\mu^2 H^\dagger H + \frac{\lambda}{2} (H^\dagger H)^2$$



A mechanism in the BSM

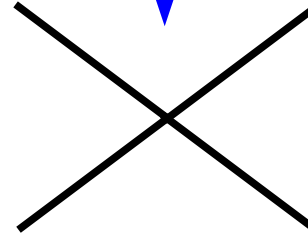
TeV

E ↑

\mathcal{L}_0



\mathcal{L}_{eff}



Higgs doublet

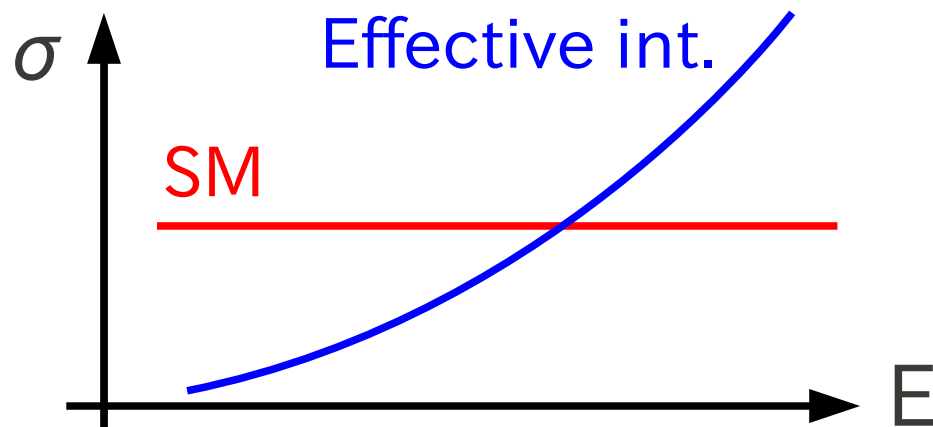
$$\partial(H^\dagger H)\partial(H^\dagger H), \dots \quad (H^\dagger \overleftrightarrow{\partial} H)(H^\dagger \overleftrightarrow{\partial} H), \dots$$

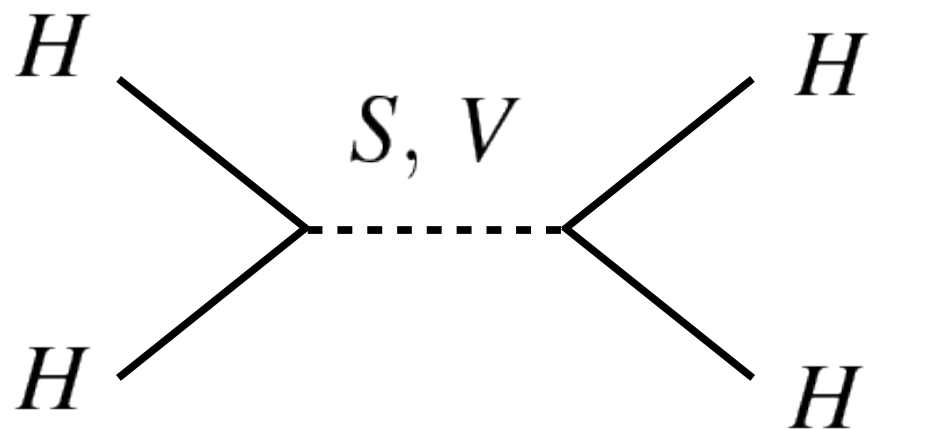
$$\frac{c^H}{2f^2} \partial(H^\dagger H) \partial(H^\dagger H), \dots$$

$$\frac{1}{2} \left(1 + c^H \frac{v^2}{f^2} \right) (\partial h)^2$$

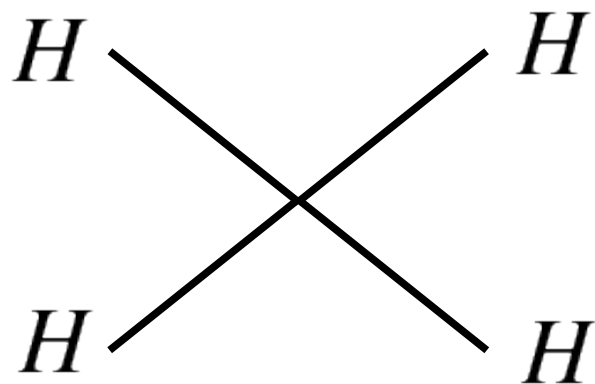
$$\frac{c^H}{f^2} h(\partial h) \phi(\partial \phi)$$

$$h \rightarrow \frac{h}{\sqrt{1 + c^H \frac{v^2}{f^2}}}$$





Integrate



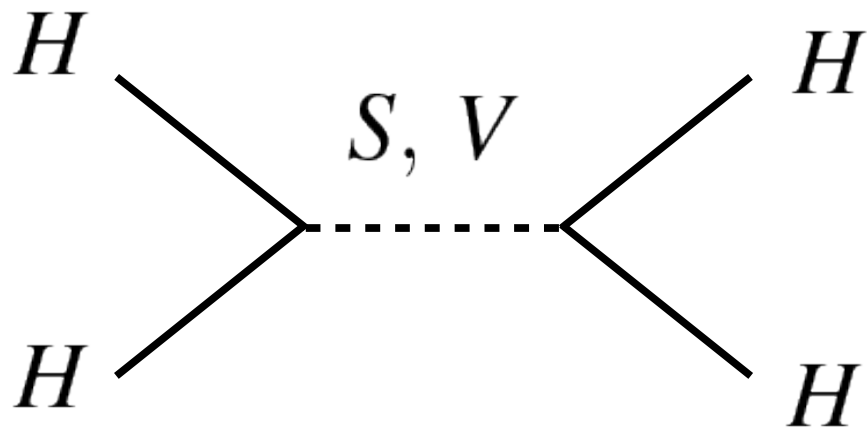
$$\frac{f^2}{2} \text{tr} \left[(\partial e^{-i\pi/f}) (\partial e^{i\pi/f}) \right]$$

Expand

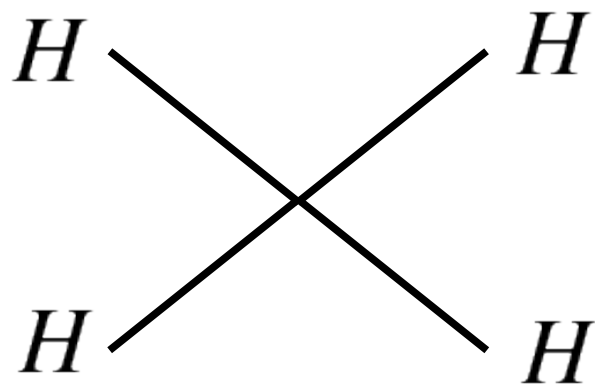
$$\frac{1}{f^2} \mathcal{T}^{abcd} h^a h^b (\partial h^c) (\partial h^d)$$

$$\partial(H^\dagger H) \partial(H^\dagger H), \dots$$

Fundamental



Integrate

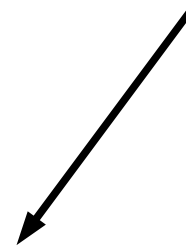


$\partial(H^\dagger H)\partial(H^\dagger H), \dots$

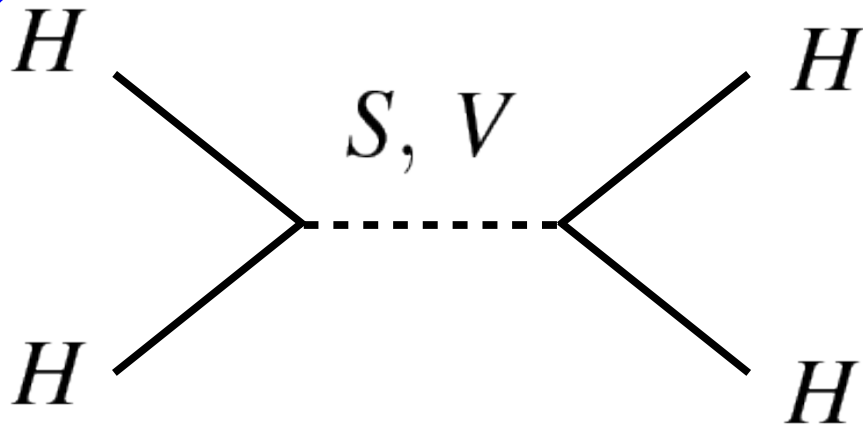
$$\frac{f^2}{2} \text{tr} \left[(\partial e^{-i\pi/f})(\partial e^{i\pi/f}) \right]$$

Expand

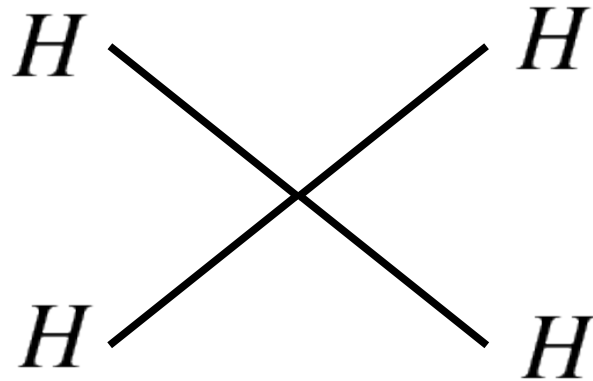
$$\frac{1}{f^2} \mathcal{J}^{abcd} h^a h^b (\partial h^c)(\partial h^d)$$



Composite



Integrate



$$\frac{f^2}{2} \text{tr} \left[(\partial e^{-i\pi/f}) (\partial e^{i\pi/f}) \right]$$

Expand

$$\frac{1}{f^2} \mathcal{T}^{abcd} h^a h^b (\partial h^c) (\partial h^d)$$

$$\partial(H^\dagger H) \partial(H^\dagger H), \dots$$

Why multi Higgs doublets?

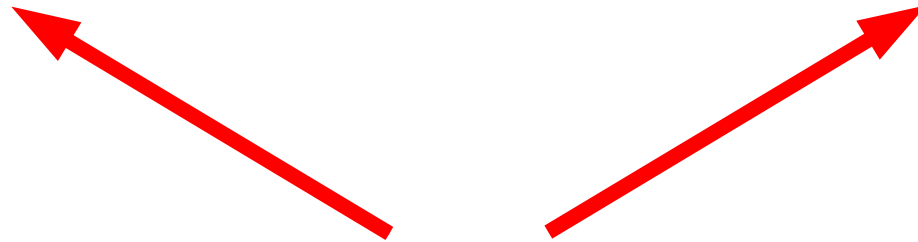
Fundamental : 2HDM, SUSY,

Composite : large global symmetry breaking

$$\pi = \begin{pmatrix} h_1 & h_2 & h_3 & \dots \\ h_1^T & \ddots & & \\ h_2^T & & \ddots & \\ h_3^T & & & \ddots \\ \vdots & & & & \ddots \end{pmatrix}$$

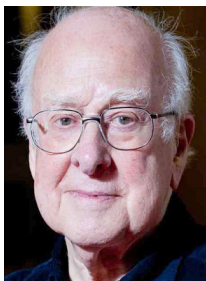
Fundamental

Composite

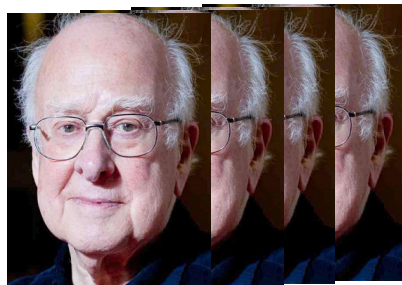


$$\partial(H^\dagger H)\partial(H^\dagger H), \dots$$

Can we discriminate them?



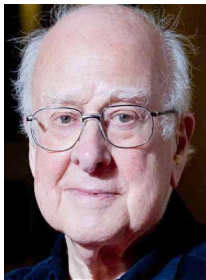
Difficult ← '09 Low et. al.



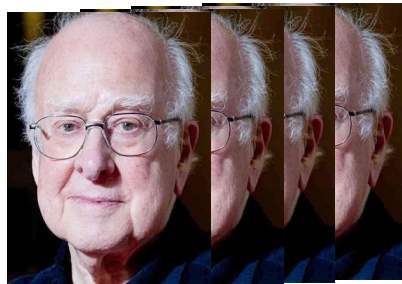
...

Possible ← This talk

DOF	Fundamental	Composite
1HDM	ϕ_0, ϕ_L^a	$\partial(H^\dagger H)\partial(H^\dagger H)$
2HDM	EWPM: 4~6	6, 8



Difficult ← '09 Low et. al.



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Possible ← This talk

$$\begin{aligned}
\mathcal{L}_{\text{NG}} &= \frac{f^2}{2} \text{tr} \left[(\partial e^{-i\pi/f}) (\partial e^{i\pi/f}) \right] && \text{4 real scalars} \\
\supset & -\frac{1}{24f^2} \left(4f^{ac} f^{bd} + f^{ace} f^{bde} \right) h^a h^b (\partial h^c) (\partial h^d) \\
& && \text{Generators of SO(4)} \\
&= a_L (h T_L^\alpha \partial h) (h T_L^\alpha \partial h) + a_R (h T_R^\beta \partial h) (h T_R^\beta \partial h) \\
&\quad + a_Y (h T_R^3 \partial h) (h T_R^3 \partial h) \\
&\blackrightarrow \partial(H^\dagger H) \partial(H^\dagger H), \quad (H^\dagger \overleftrightarrow{\partial} H) (H^\dagger \overleftrightarrow{\partial} H)
\end{aligned}$$

Even in NHDM,

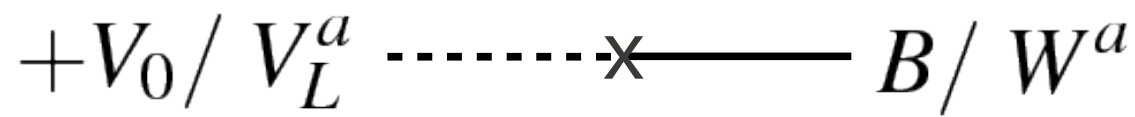
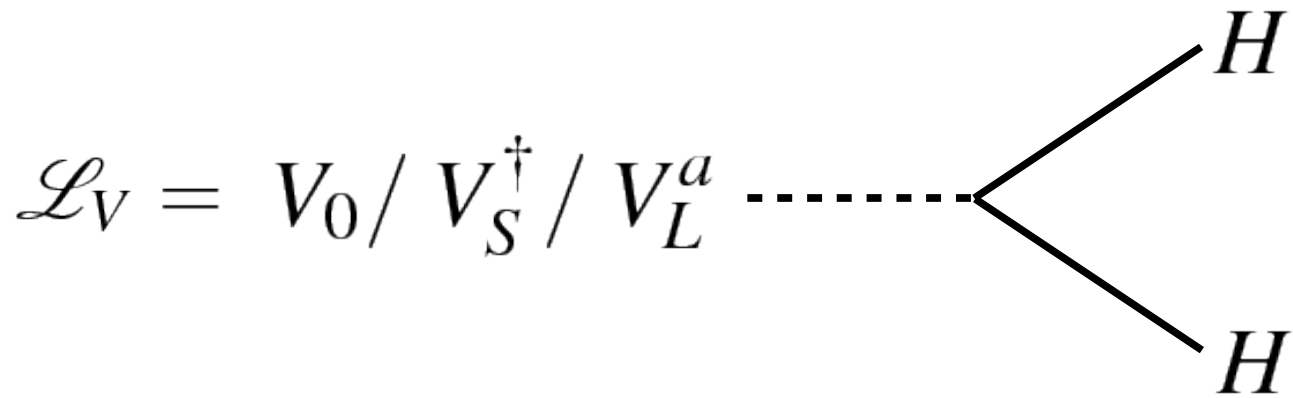
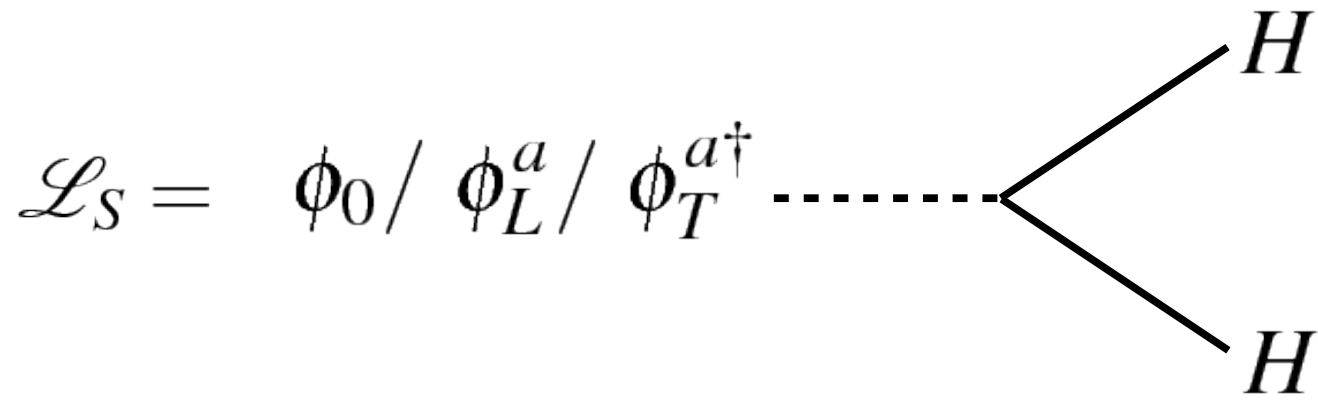
DOF(composite) = DOF(general)

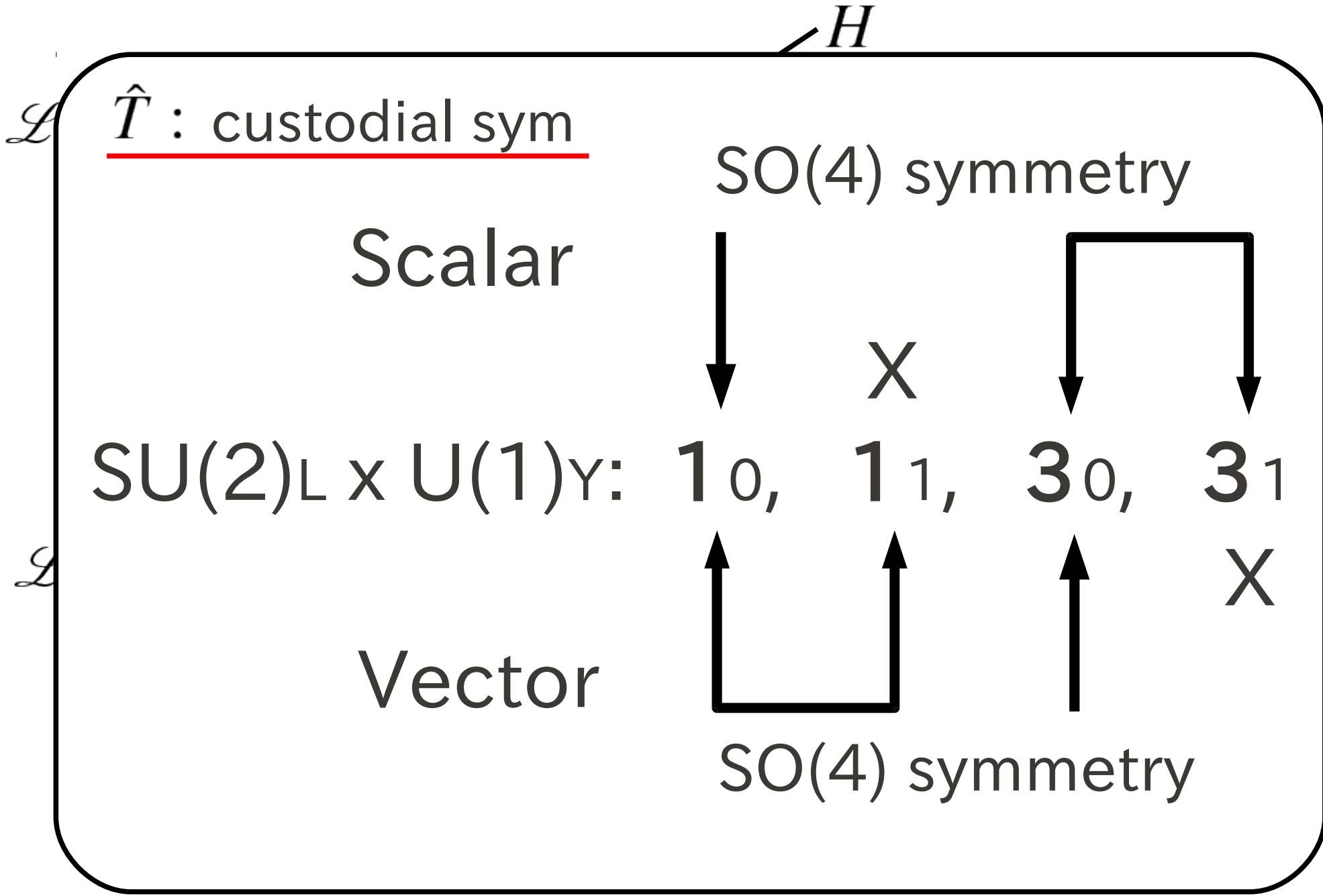
arXiv:1111.2120

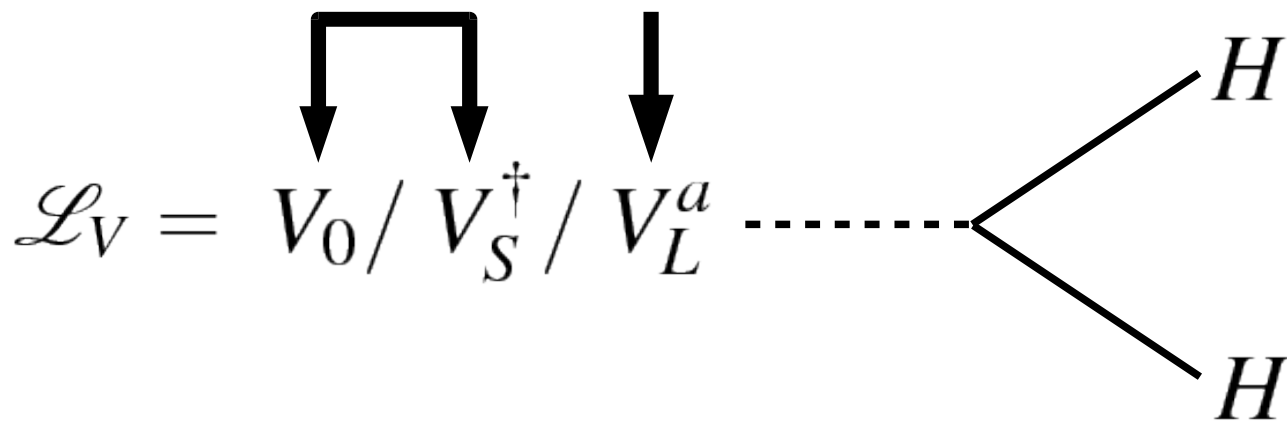
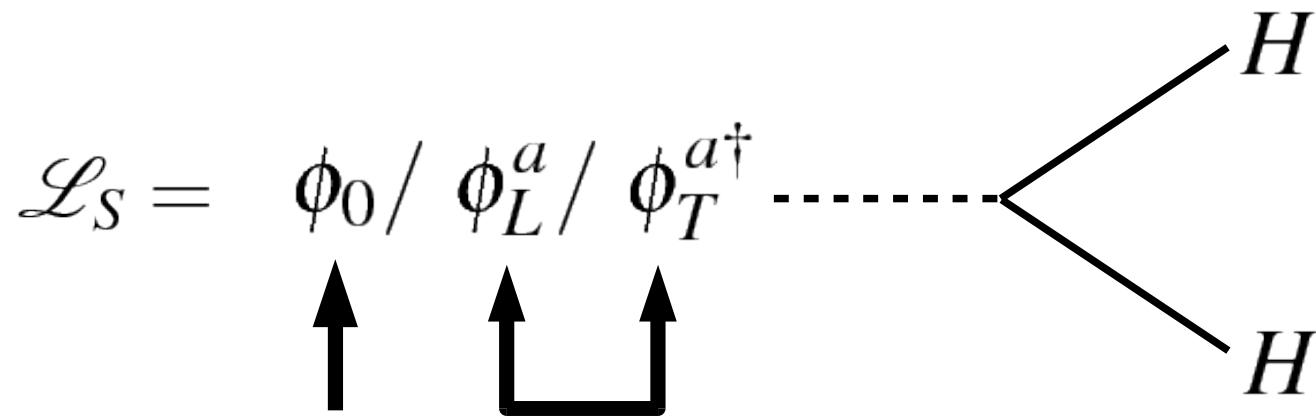
Lagrangian

$$\begin{aligned}\mathcal{L}_S = & -\frac{m_{S0}^2}{2}\phi_0^2 + \lambda_0 f \phi_0 (H^\dagger H) \\ & -\frac{m_{SL}^2}{2}\phi_L^a \phi_L^a + \lambda_L f \phi_L^a (H^\dagger \sigma^a H) \\ & -m_{ST}^2 \phi_T^{a\dagger} \phi_T^a + \left(\frac{\lambda_T}{2} f \phi_T^{a\dagger} (\tilde{H}^T \sigma^a H) + \text{H.c.} \right)\end{aligned}$$

$$\begin{aligned}\mathcal{L}_V = & \frac{m_{V0}^2}{2} V_0 \cdot V_0 + V_0 \cdot \left(i g_0 \left(H^\dagger \overleftrightarrow{\partial} H \right) + g' \gamma_0 \partial \cdot B \right) \\ & + m_{VS}^2 V_S^\dagger \cdot V_S + \left(\frac{i g_S}{2} V_S^\dagger \cdot \left(\tilde{H}^T \overleftrightarrow{\partial} H \right) \right) \\ & + \frac{m_{VL}^2}{2} V_L^a \cdot V_L^a + V_L^a \cdot \left(i g_L \left(H^\dagger \overleftrightarrow{\partial} \sigma^a H \right) + g \gamma_L (\partial \cdot W)^a \right)\end{aligned}$$







$+V_0 / V_L^a \cdots \times \longleftarrow B / W^a \longleftarrow \hat{S}, W, Y$

Vectors should be decoupled.

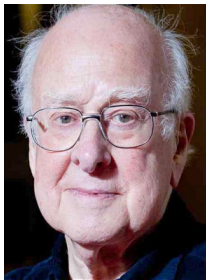
$$\mathcal{L}_S = \phi_0 / \phi_L^a / \phi_T^{a\dagger} \cdots \begin{array}{l} \diagup H \\ \diagdown H \end{array}$$

$$\Rightarrow f^2 \left(\frac{\lambda_0^2}{m_{S0}^4} - \frac{3\lambda_L^2}{m_{SL}^4} \right) \partial(H^\dagger H) \partial(H^\dagger H)$$

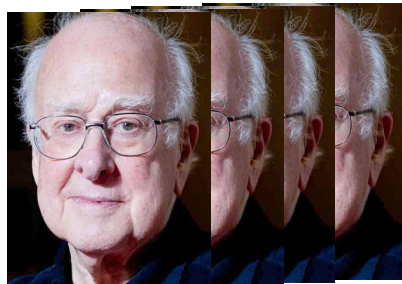
$$\text{DOF(fund.)} = 2 > \text{DOF(comp.)} = 1$$

It is difficult to discriminate them.

DOF	Fundamental	Composite
1HDM	ϕ_0, ϕ_L^a	$\partial(H^\dagger H)\partial(H^\dagger H)$
2HDM	EWPM: 4~6	6, 8

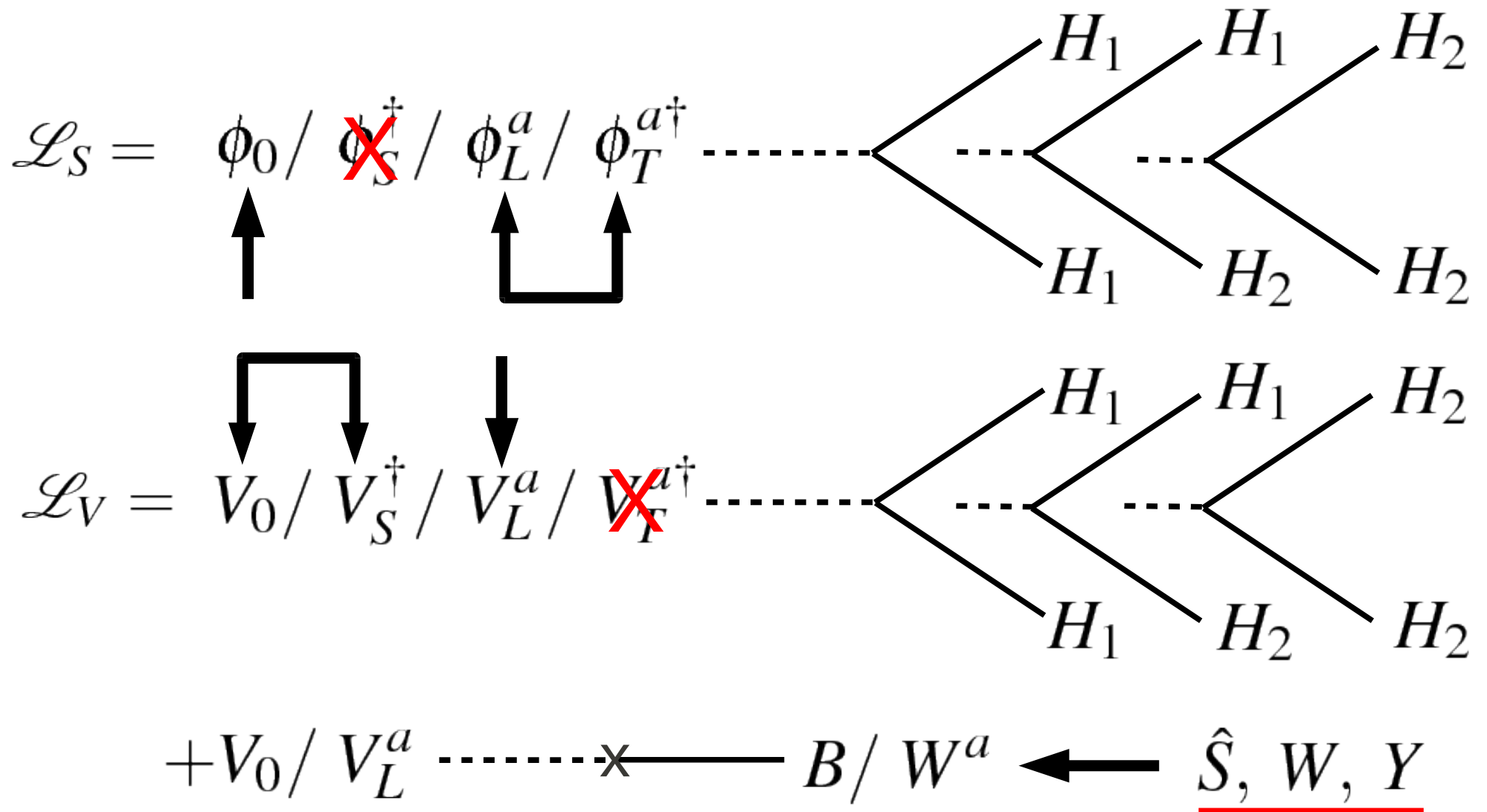


Difficult ← '09 Low et. al.

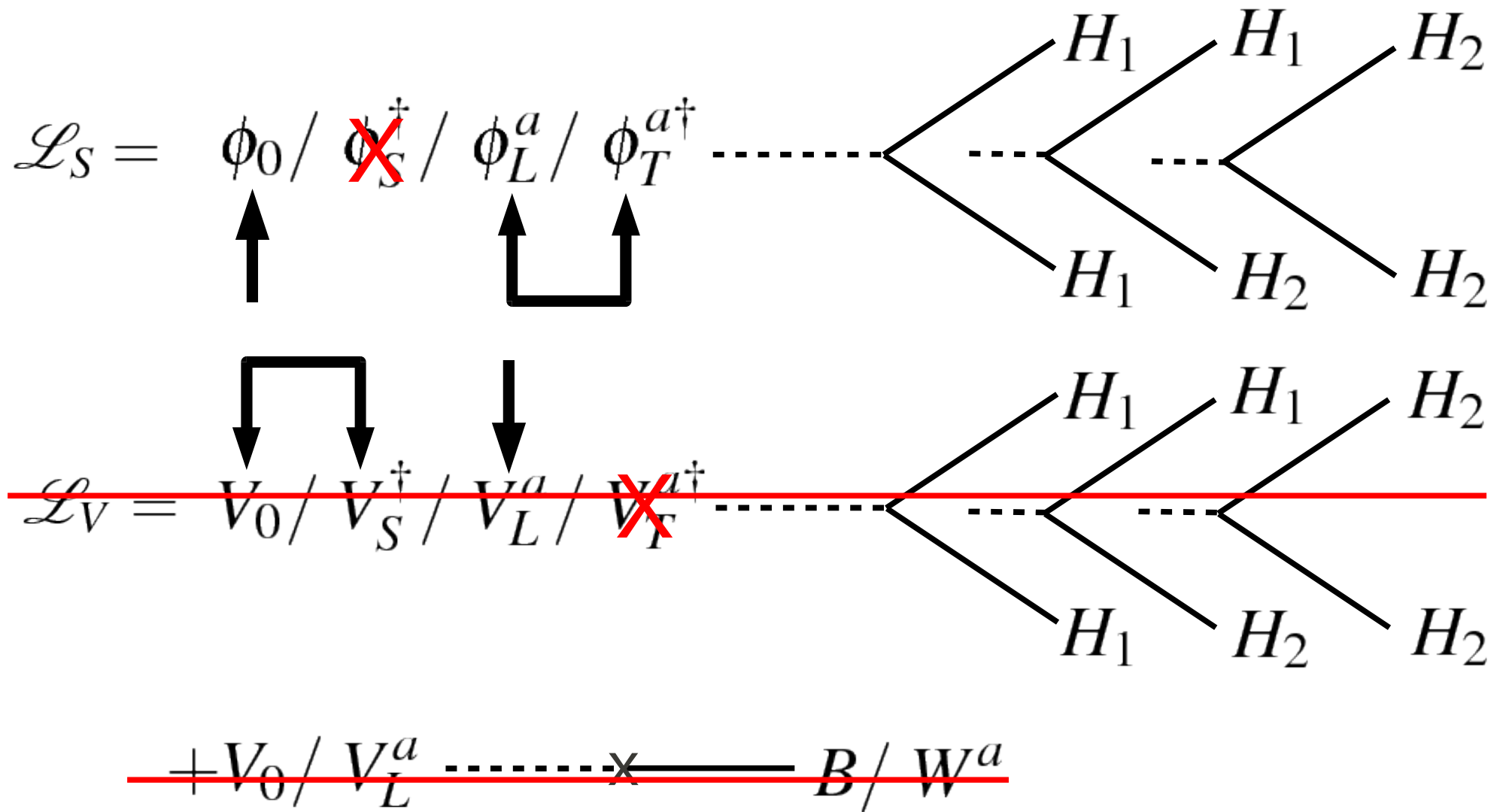


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Possible ← This talk

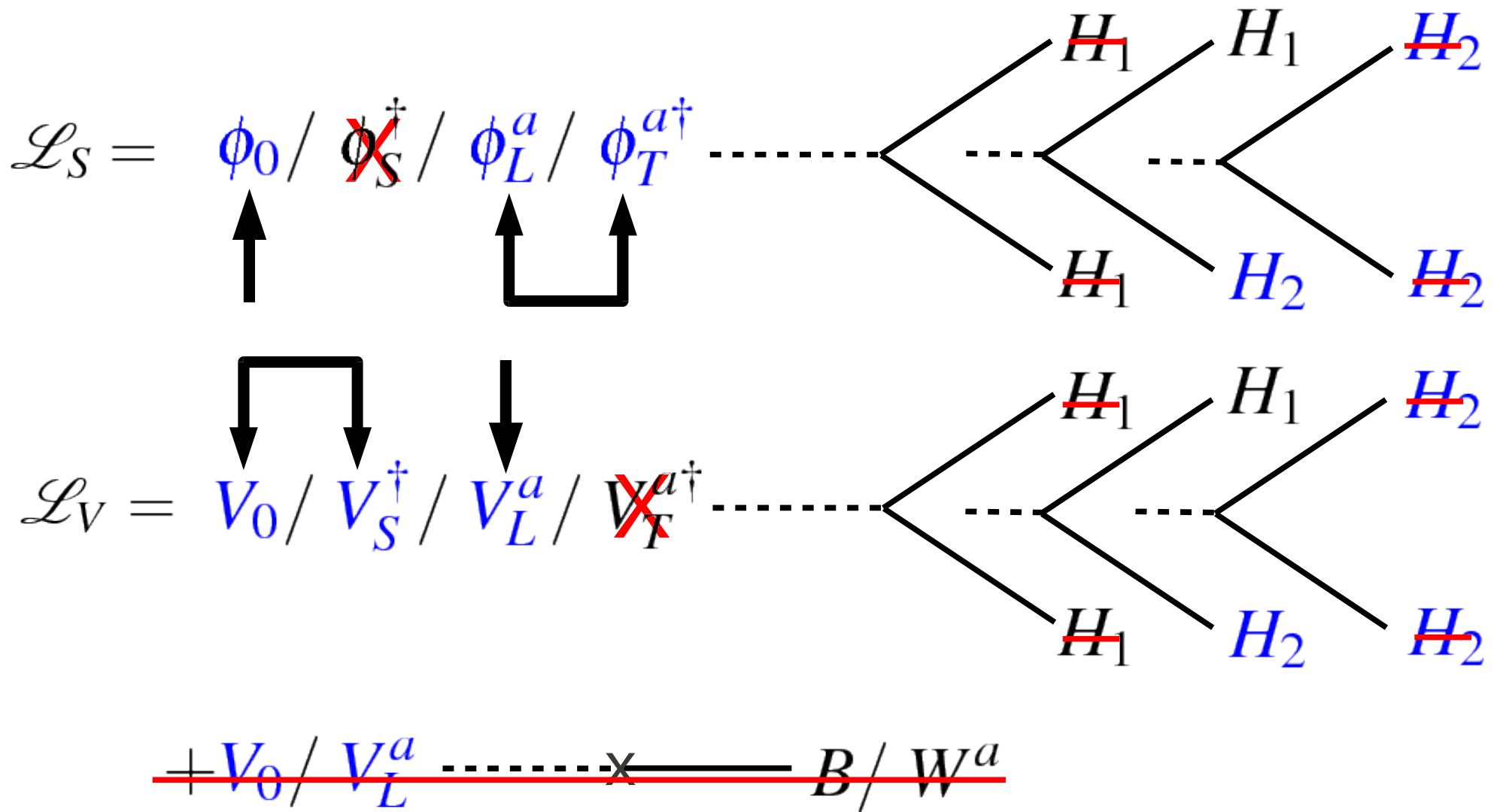


Oblique operators are suppressed by large M_V / additional Z_2



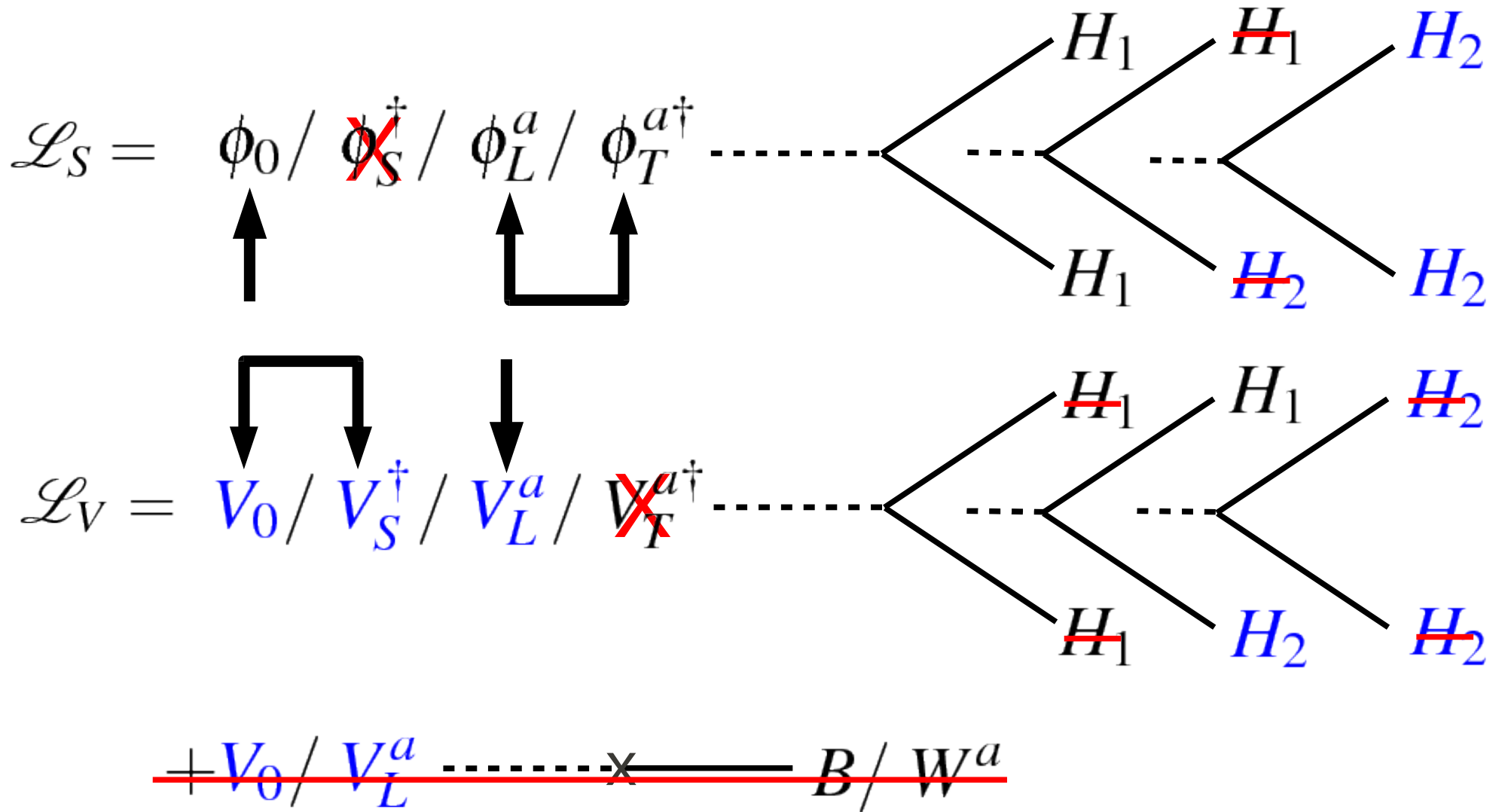
Decouple:

$$\text{DOF}(\text{fund})=6 < \text{DOF}(\text{comp.})=8$$



Z_2 symmetry (odd scalar):

$$\text{DOF}(\text{fund.})=4 < \text{DOF}(\text{comp.})=6$$



Z₂ symmetry (even scalar):

$$\text{DOF}(\text{fund.})=6 = \text{DOF}(\text{comp.})=6$$

$$\partial(H^\dagger H)\partial(H^\dagger H), \dots$$

Integrating out Nonlinear sigma model

Is the Higgs fundamental or composite?

Suppression of oblique corrections

SO(4) symmetry

Large M_v / Additional Z_2

For $N > 1$,

$\text{DOF}(\text{Fundamental}) \leq \text{DOF}(\text{Composite})$

Complete results for NHDM will appear arXiv:1209.xxxx