# Alignment in multi-Higgs doublet models through family symmetries

Ivo de Medeiros Varzielas

University of Southampton

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## Multi-Higgs









Hideki Yukawa ("maiden" name, Hideki Ogawa) We might be saying "Ogawa couplings" today...



### Multi-Higgs models and Yukawa

In MHDM, for each family  $(u, d, l, \nu)$  there is a Yukawa for each Higgs.

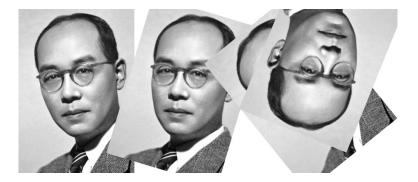
$$\mathcal{L}_{u} = \sum_{A=1}^{N} \left( Y_{A}^{u} \right)^{ij} H_{A}^{\dagger} Q_{i} u_{j}^{c} + h.c.$$
(1)

The  $Y_A^{u,d,l,\nu}$  are in principle unrelated... Not simultaneously diagonal:

would lead to FCNC which have not been observed.



## Multi-Ogawa





#### Yukawa alignment

Solution: Yukawa alignment, no FCNC: A. Pich and P. Tuzon, Phys.Rev. D80 (2009)

Alignment can not be preserved by renormalisation (unless additional symmetries are applied): P. Ferreira, L. Lavoura, and J. P. Silva, Phys.Lett. B688 (2010)

But deviations from running may be sufficiently small (for current bounds):

C. B. Braeuninger, A. Ibarra, and C. Simonetto, Phys.Lett. B692 (2010)



Exact alignment from family symmetries

IdMV, Phys.Lett. B701 (2011)

- Single FS invariant combination (for each family)
- All *H<sub>A</sub>* trivial singlets under the FS

See also different approach: H. Serôdio, Phys.Lett. B700 (2011)



#### Exact alignment example

FS:  $SU(3)_{[]} \otimes SU(3)_{()}$ 

$$\mathcal{L}_{u} = \sum_{A=1}^{N} c_{A}^{u} \mathcal{H}_{A}^{\dagger} [\phi_{Q}^{i} Q_{i}] (\phi_{u}^{j} u_{j}^{c}) + h.c.$$
<sup>(2)</sup>

All  $(Y_A^u)^{ij} \propto \langle \phi_Q^i \phi_u^j \rangle$ : exact alignment Note: single SU(3) has also  $\sum_{A=1}^N c_A'^u H_A^{\dagger}(\phi_u^i Q_i)(\phi_Q^j u_i^c)...$ 



## Alignment





### Up, Down

$$SU(3)_{[]}\otimes SU(3)_{()}\otimes C_2$$

$$\mathcal{L}_{Q} = \sum_{A=1}^{N} [\phi_{Q}^{i} Q_{i}] \left( c_{A}^{d} H_{A}(\phi_{d}^{j} d_{j}^{c}) + c_{A}^{u} H_{A}^{\dagger}(\phi_{u}^{j} u_{j}^{c}) \right) + h.c.$$

With e.g.  $\phi_d$ ,  $d^c$  as -1 under the  $C_2$  (prevents  $\phi_u$ ,  $\phi_d$  swapping places)

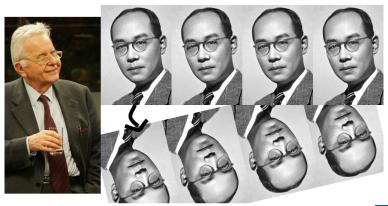


### Up and down alignment



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### Up and down alignment







		и <sup>с</sup>	dc	L	ec	$\phi_{Q}$	$\phi_{u}$	$\phi_{d}$	$\phi_L$	$\phi_{\boldsymbol{e}}$
SU(3) <sub>[]</sub> SU(3) <sub>()</sub>	3	1	1	3	1	Ī	1	1	Ī	1
$SU(3)_{()}^{"}$	1	3	3	1	3	1	Ī	Ī	1	Ī
<i>C</i> <sub>7</sub>	1	1	$\alpha^{3}$	$\alpha$	$\alpha^4$	$\alpha$	$\alpha^{6}$	$\alpha^{3}$	$\alpha^2$	1

Table :  $SU(3)_{[]} \otimes SU(3)_{()} \otimes C_7$  assignments.  $\alpha^7 = 1$ .



### All families

	Q	и <sup>с</sup>	dc	L	ec	$\nu^{c}$	$\phi_{Q}$	$\phi_{u}$	$\phi_{\it d}$	$\phi_L$	$\phi_{\pmb{e}}$	$\phi_{ u}$
SU(3) <sub>[]</sub> SU(3) <sub>()</sub>	3	1	1	3	1	1	Ī	1	1	3	1	1
$SU(3)_{()}$	1	3	3	1	3	3	1	Ī	Ī	1	Ī	3
<i>C</i> <sub>10</sub>	1	1	$\alpha^{3}$	$\alpha$	$\alpha^4$	$\alpha^7$	$\alpha$	$\alpha^{9}$	$\alpha^{6}$	$\alpha^2$	$\alpha^{3}$	1

Table :  $SU(3)_{[]} \otimes SU(3)_{()} \otimes C_{10}$  assignments.  $\alpha^{10} = 1$ .





- All the mass matrices in the above example are rank 1 (this is a feature of using  $SU(3)_{[]} \otimes SU(3)_{()}$ ).
- Can use discrete subgroups (example in paper). IdMV, Phys.Lett. B701 (2011)



#### Approximate alignment

Abandon single FS invariant combination Keep leading order rank 1 Yukawa (as observed): approximate alignment!



### Conclusion

#### Conclusions

- Exact alignment from single FSIC + Family singlet H
- Single FSIC: too restrictive for realistic Yukawas
- FS + LO rank 1 provides approximate alignment

