

# Electroweak Baryogenesis and Dark Matter from a Complex Singlet

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- Motivation
- Strongly First-Order Electroweak Phase Transition
- Dark Matter Physics
- CP Violation and EW Baryogenesis
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- Summary

# Motivation

➤ In spite of the great success of the **Standard Model (SM)** of particle physics, there are still many puzzles needing to be explained. Among others, two important questions are

- **Dark Matter** : In the SM, there is no DM candidate.

- **Matter-Antimatter Asymmetry in our Universe**

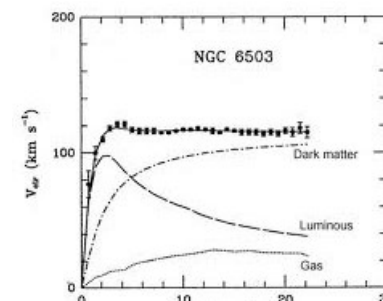
➤ Both problems require the physics beyond the SM.

# Motivation

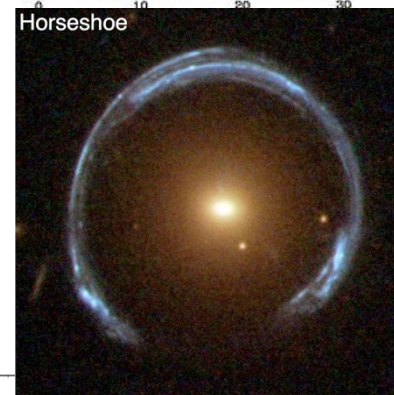
➤ There are already many established evidences for the existence of **dark matter**

- Rotation Curves of Spiral Galaxies

Babcock, 1939, Bosma, 1978; Rubin & Ford, 1980

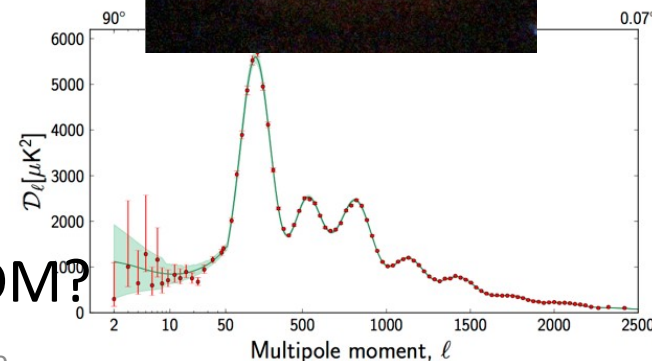
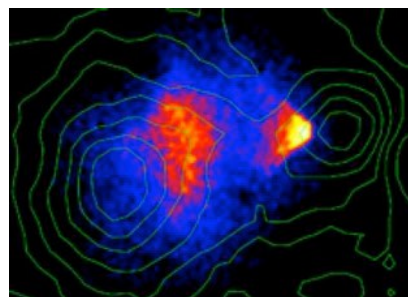


- Gravitational Lensing



- CMB

- Bullet Clusters



But , what is the **particle nature** of DM?

# Motivation

- Observed Baryon Asymmetry: Planck Collaboration, arXiv: 1502.01589

$$\eta_B \equiv \frac{n_B}{s} = (8.61 \pm 0.09) \times 10^{-11}$$

- Three Sakharov criteria for baryogenesis:

- ✓ B violation
- ✓ C and CP violation
- ✓ Thermal non-equilibrium

A. D. Sakharov, 1967

- Situation in the SM:

F. R. Klinkhamer & N.S. Manton 1984

- ✓ B violation: weak sphaleron process
- ✓ The CP violation due to CKM phase is inadequate
- ✓ EW phase transition is actually a cross-over, rather than being of strongly first-order.

M. E. Shaposhnikov, 1987

K. Kajantie et al, hep-ph/9605288

# Motivation

➤ EW Baryogenesis:

V. A. Kuzmin, V.A. Rubakov, M.E. Shaposhnikov, 1985;  
A. G. Cohen, D. B. Kaplan and A. E. Nelson, 1990

✓ new CPV sources

✓ adding new particles with masses of EW scale in order to make the EWPT of strongly first-order, which provides the necessary deviation from an equilibrium.

➤ **Problem:** The new CPV source required by the baryogenesis is strongly constrained by the EDMs of electrons and neutrons.

ACME Collaboration, 1310.7534; PDG 2016;

➤ **Possible solution:** If the CP is spontaneously broken at high temperatures before the EWPT while restored afterward, then the CPV constraint can be evaded!

J. McDonald, 1994; W. Chao, 1706.01041

# The Model

- Extend the SM by an EW singlet complex scalar

$$S = (s+ia)/\sqrt{2}$$

with a  $Z_2$  symmetry:  $S \leftrightarrow -S$  and  $CP$  symmetry related to  $S$

J. McDonald, 1994, 1995; G.C. Branco et al, 9805302; S. Profumo et al, 0705.2425; ...

- The scalar potential at zero temperature:

$$\begin{aligned} V_0(H, S) &= \lambda_H \left( |H|^2 - \frac{v_0^2}{2} \right)^2 - \mu_1^2 (S^* S)^2 - \frac{\mu_2^2}{2} (S^2 + S^{*2}) \\ &\quad + \lambda_1 (S^* S)^2 + \frac{\lambda_2}{4} (S^2 + S^{*2})^2 + \frac{\lambda_3}{2} |S|^2 (S^2 + S^{*2}) \\ &\quad + |H|^2 \left[ \kappa_1 (S^* S) + \frac{\kappa_2}{2} (S^2 + S^{*2}) \right] \\ &= -\frac{1}{2} \lambda_H v_0^2 h^2 + \frac{1}{4} \lambda_H h^4 - \frac{1}{2} (\mu_1^2 + \mu_2^2) s^2 - \frac{1}{2} (\mu_1^2 - \mu_2^2) a^2 \\ &\quad + \frac{1}{4} (\lambda_1 + \lambda_2 + \lambda_3) s^4 + \frac{1}{4} (\lambda_1 + \lambda_2 - \lambda_3) a^4 \\ &\quad + \frac{1}{4} (\kappa_1 + \kappa_2) h^2 s^2 + \frac{1}{4} (\kappa_1 - \kappa_2) h^2 a^2 + \frac{1}{2} (\lambda_1 - \lambda_2) s^2 a^2 + \text{const.} \end{aligned}$$

$$H = (0, h/\sqrt{2})^T$$

REAL  
couplings

# The Model

- Leading-order **finite-temperature** corrections at **high-T expansion**

$$V_T = \frac{1}{2}c_h T^2 h^2 + \frac{1}{2}c_s T^2 s^2 + \frac{1}{2}c_a T^2 a^2$$

where

$$c_h = \frac{3g^2}{16} + \frac{g'^2}{16} + \frac{y_t^2}{4} + \frac{\lambda_H}{2} + \frac{\kappa_1}{12},$$
$$c_s = \frac{1}{6}(2\lambda_1 + \kappa_1 + \kappa_2) + \frac{\lambda_3}{4},$$
$$c_a = \frac{1}{6}(2\lambda_1 + \kappa_1 - \kappa_2) - \frac{\lambda_3}{4}.$$

- Total Potential:

$$V_{\text{tot}} = V_0 + V_T.$$



# EW Phase Transition

- Rewrite the total scalar potential

$$\begin{aligned} V_{\text{tot}} = & \frac{\lambda_{hs}}{4} \left( h^2 - v_c^2 + \frac{v_c^2 s^2}{w_c^2 \cos^2 \alpha} \right)^2 + \frac{\lambda_{ha}}{4} \left( h^2 - v_c^2 + \frac{v_c^2 a^2}{w_c^2 \sin^2 \alpha} \right)^2 \\ & + \frac{\lambda_{sa}}{4} (s^2 \sin^2 \alpha - a^2 \cos^2 \alpha)^2 + \frac{\kappa_{hs}}{4} h^2 s^2 + \frac{\kappa_{ha}}{4} h^2 a^2 \\ & + \frac{1}{2} (T^2 - T_c^2) [c_h h^2 + c_s s^2 + c_a a^2] \end{aligned}$$

- **Two vacua:**  $(h, s, a) = (v_c, 0, 0)$  and  $(0, w_c \cos \alpha, w_c \sin \alpha)$

- Critical Temperature:

$$T_c^2 = \lambda_H (v_0^2 - v_c^2) / c_h$$

# EW Phase Transition

## ➤ Further Consistency Constraints:

### ✓ Strongly First-Order EWPT:

$$v_c/T_c > 1$$

G. D. Moore, hep-ph/9805264

### ✓ Potential Stability: assume positive couplings

### ✓ Correct EWPT direction from $(0, w_c \cos \alpha, w_c \sin \alpha)$ to $(v_c, 0, 0)$

$$c_h v_c^2 > c_s w_c^2 \cos^2 \alpha + c_a w_c^2 \sin^2 \alpha$$

### ✓ $Z_2$ symmetry: $\alpha \in (-\pi/2, \pi/2)$

### ✓ Perturbativity: $|\lambda_{1,2,3}, \kappa_{1,2}| \leq 5$ M. Nebot et al, 0711.0483

# Dark Matter Physics

- Depending the mass ordering, either  $s$  or  $a$  can be DM candidate  $X$
- The DM pheno. only depends on **Higgs portal coupling**

$$\boxed{\lambda_{hX} h^2 X^2 / 4} \quad \text{J. M. Cline \& K. Kainulainen, 1210.4196}$$

with

$$\lambda_{hX} = \begin{cases} \kappa_{hs} + \frac{2\lambda_{hs}v_c^2}{w_c^2 \cos^2 \alpha}, & X = s \\ \kappa_{ha} + \frac{2\lambda_{ha}v_c^2}{w_c^2 \sin^2 \alpha}, & X = a \end{cases}$$

- The **DM relic density** is obtained by **the freeze-out mechanism**, and is calculated with MicrOMEGAs code.
- In order to consider the case with subdominant DM, we define the **DM fraction**:  $f_X = \frac{\Omega_X h^2}{\Omega_{\text{DM,obs}} h^2}$  **with**  $\Omega_{\text{DM,obs}} h^2 = 0.1186$

# Dark Matter Physics

## ➤ DM Constraints:

- ✓ DM direct detection: XENON1T

- ✓ DM Indirect detection: Fermi-LAT, Planck, and AMS-02

- ✓ SM Higgs Invisible Decay:  $\text{Br}(h \rightarrow XX) \leq 0.24$  PDG 2016

- ✓ Monojet searches: CMS

# High-T CP Violation

- S can acquire a **complex VEV** before EWPT

$$\langle S \rangle = w_c e^{i\alpha} / \sqrt{2}$$

- With the following dim-6 operator

$$\mathcal{O}_6 = \frac{S^2}{\Lambda^2} \bar{Q}_{3L} \tilde{H} t_R + \text{H.c.}$$

J. R. Espinosa et al., 1110.2876;  
J.M. Cline & K. Kainulainen,  
1210.4196;  
V. Vaskonen, 1611.02073

the CP symmetry is spontaneously broken, which is shown by the induced **complex-valued top quark Yukawa** coupling

$$\frac{w_c^2 e^{i2\alpha}}{2\Lambda^2} \bar{Q}_{3L} \tilde{H} t_R + \text{H.c.}$$

- Together with top Yukawa, we have a complex top-quark mass

# First-Order EWPT

- For a first-order EWPT, the PT proceeds via the **bubble nucleation**.
- Near the bubble wall, the top acquires a **spatially varying** complex mass

$$m_t(z) = \frac{y_t}{\sqrt{2}} h(z) \left( 1 + \frac{S(z)^2}{y_t \Lambda^2} \right) \equiv |m_t(z)| e^{i\theta(z)}$$

M. Joyce, et al., hep-ph/9410282; J.M. Cline et al., hep-ph/9708393, hep-ph/0006119

- This top mass would generate **CPV force** that acts on tops and anti-tops differently when they pass through the wall.

$$F_z = -\frac{(m^2)'}{2E_0} \pm s \frac{(m^2 \theta')'}{2E_0 E_{0z}} \mp s \frac{\theta' m^2 (m^2)'}{4E_0^3 E_{0z}}$$

L. Fromme & S.J. Huber,  
hep-ph/0604159

which is the source of CPV in the **EW baryogenesis**.

# First-Order EWPT

- Approximate solution of bubble wall profile:

$$S(z) \equiv \frac{w_c e^{i\alpha}}{2\sqrt{2}} [1 + \tanh(z/L_w)],$$
$$h(z) \equiv \frac{v_c}{2} [1 - \tanh(z/L_w)],$$

J. R. Espinosa, et al,  
arXiv: 1110.2876

where  $L_w$  is the bubble wall width given by

$$L_w = \frac{v_c^2 + w_c^2}{6V_\times}$$

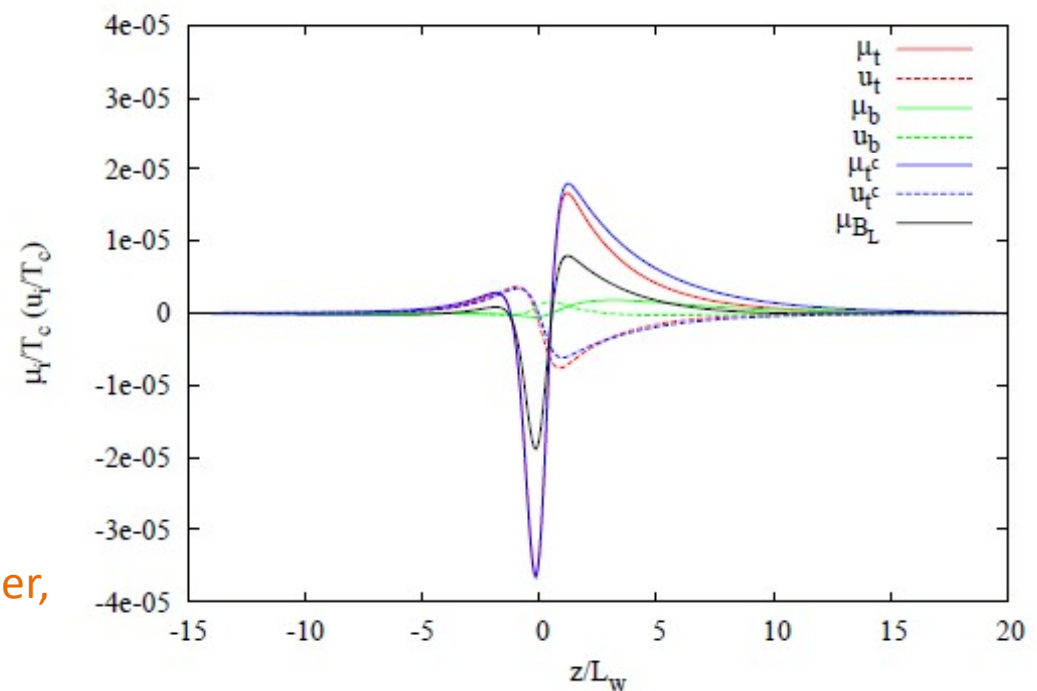
with  $V_\times$  the potential energy at the top of the barrier.

# First-Order EWPT

➤ The CP violations created around the bubble wall would transport to the EW symmetric phase deeply, where it biases the EW sphaleron processes to generate baryon asymmetry.

➤ The transportation of the CP asymmetry is described by the transport equations of chemical potentials and velocity perturbations of  $t_L$ ,  $t_R$ ,  $b_L$  and SM Higgs.

L. Fromme & S.J. Huber,  
hep-ph/0604159



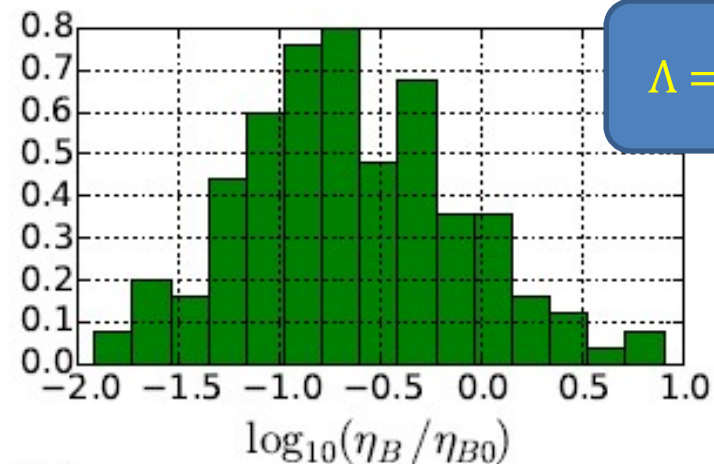
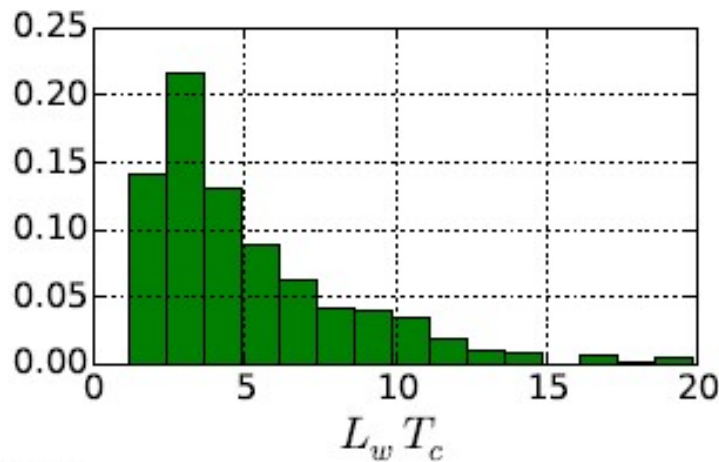


# First-Order EWPT

- The final baryon asymmetry density is predicted to be

$$\eta_B = \frac{n_B}{s} = \frac{405\Gamma_{\text{sph}}}{4\pi^2 v_w g_* T} \int_0^\infty dz \mu_{BL}(z) e^{-45\Gamma_{\text{sph}}|z|/(4v_w)}$$

where  $\mu_{BL} = \frac{1}{2}(1 + 4K_{1,tL})\mu_{tL} + \frac{1}{2}(1 + 4K_{1,bL})\mu_{bL} + 2K_{1,tR}\mu_{tR}$ ,  $v_w$  is the bubble wall velocity in the plasma, and  $\Gamma_{\text{sph}} \simeq 10^{-6}T$  is the sphaleron rate in the symmetric phase. J.M. Cline et al., hep-ph/0006119



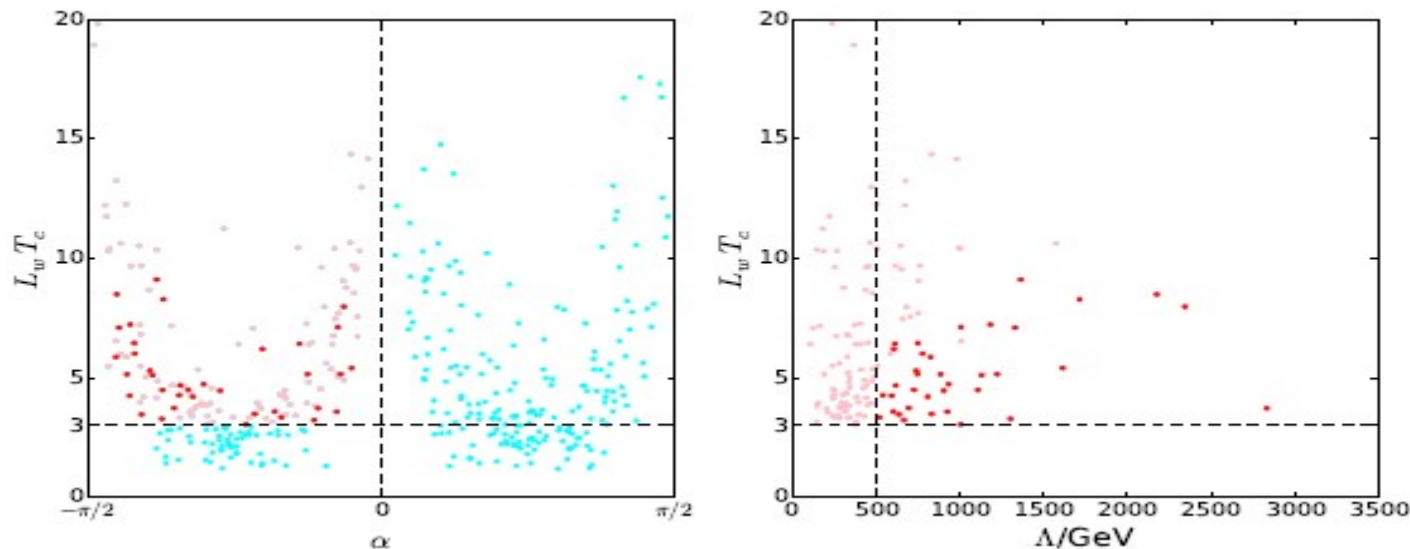
# First-Order EWPT

➤ Additional Constraints:

✓ Positive baryon asymmetry ➡ CPV phase  $\alpha < 0$

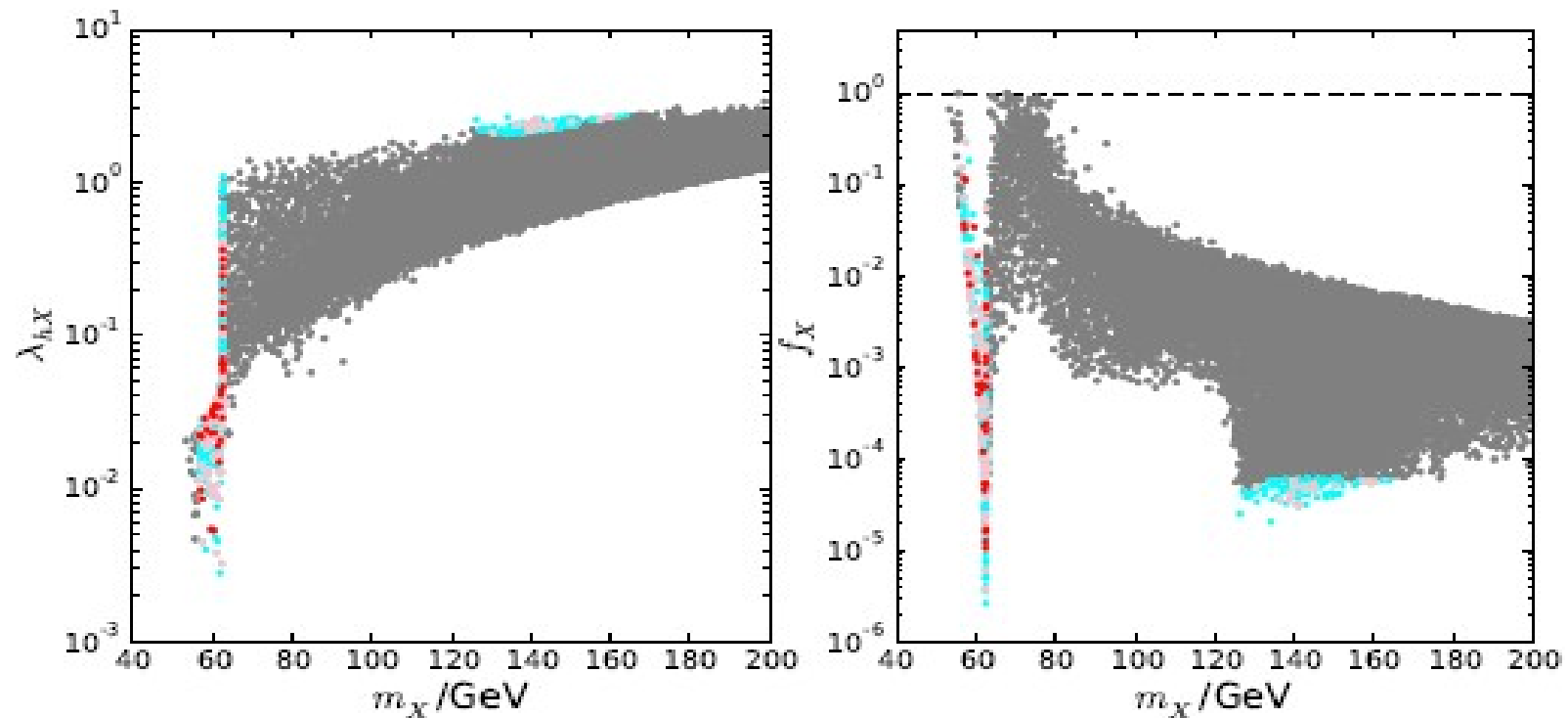
✓ Validity of semiclassical framework ➡  $L_w T_c \geq 3$

✓ Reliable use of  $O_6$  ➡  $\Lambda > 500$  GeV and  $w_c^2/\Lambda^2 < 0.5$  for  $\eta_B = \eta_B^{\text{obs}}$



# Scanning Results

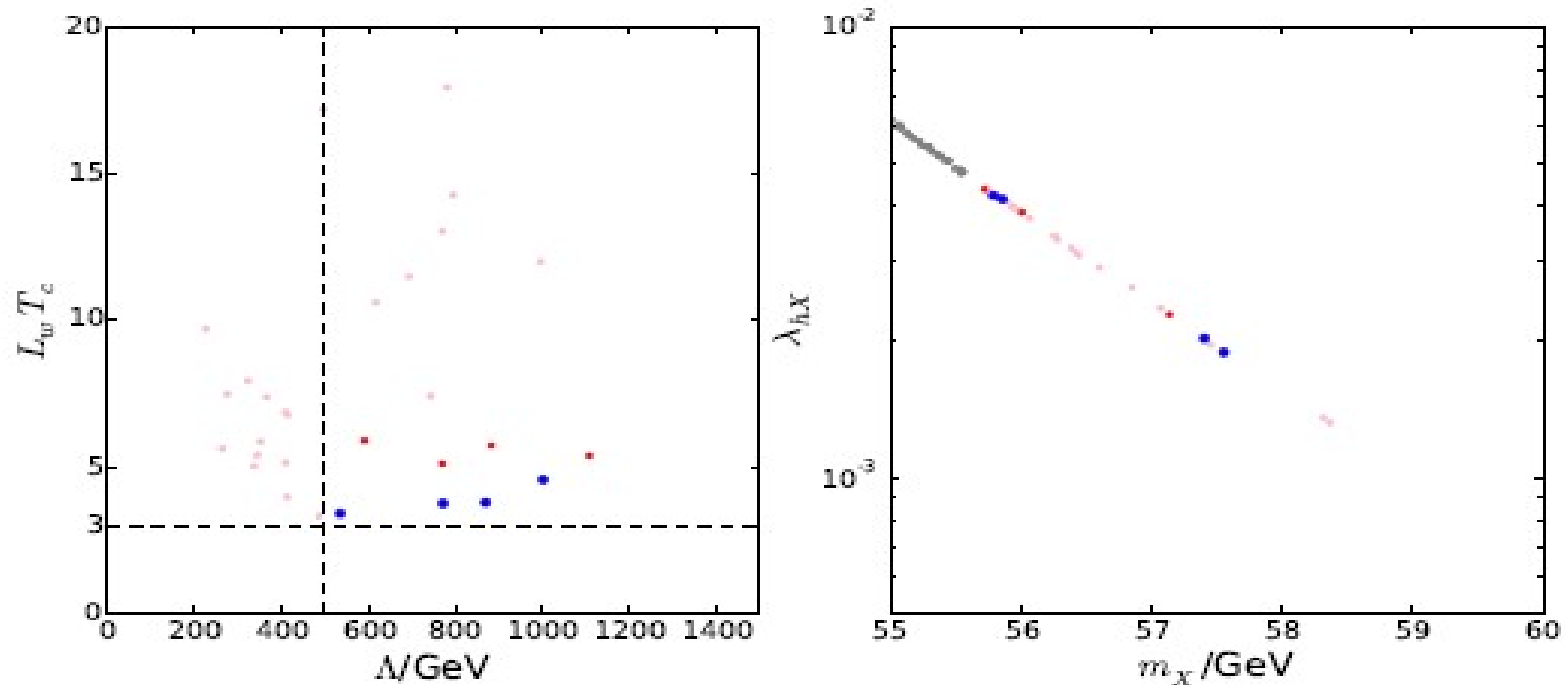
- Implications of **EWBG** on the **DM** properties



- Only **SM Higgs resonance region** can generate the enough **cosmological baryon asymmetry** without violating any bounds.

# Models with Correct DM Density

- Question: Can this simple model explain the **DM relic density** and **baryon asymmetry** simultaneously?
- Zoom-in Scan near SM Higgs Resonance



Red:  $w_c^2/\Lambda^2 < 0.5$

Blue:  $w_c^2/\Lambda^2 < 0.2$

@ Workshop on Multi-Higgs Models 2018

## Summary

- We explored a new connection between **DM** and **EWBG** in a simple **EW singlet extension** of the SM.
- The model is appealing in that the CPV necessary for the EWBG is only spontaneously generated **at temperatures higher than the EWPT**, while the CP symmetry is restored at present time, so that the low-energy **electron** and **neutron EDM** constraints can be evaded.
- We show that the model can generate the **DM relic density** and **baryon asymmetry** with the DM mass near the **SM Higgs resonance**.

*Thanks for your attention!*

# Problems with Exact CP Symmetry

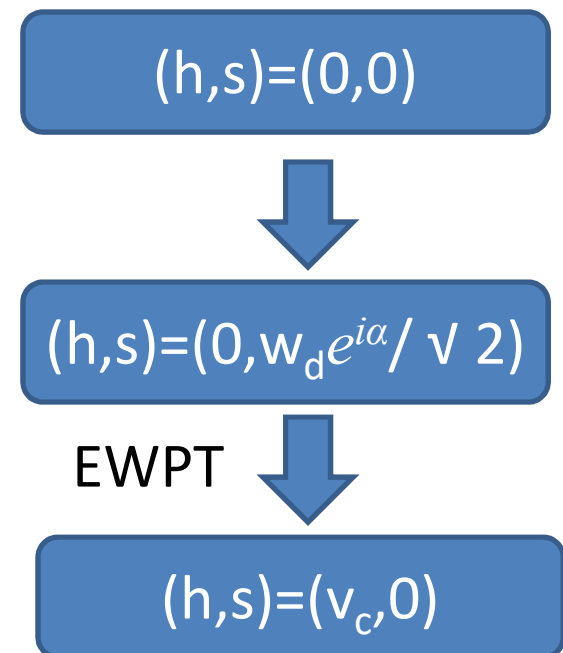
➤ Previously, we assumed that at the time before the EWPT, the Universe is filled with one vacuum with  $(h,S) = (0, w_c e^{i\alpha} / \sqrt{2})$ .

➤ However, in the present model, the transition has **two steps**.

➤ If  $Z_2$  and  $CP$  symmetries are exact, when these two symmetries are broken in the 1<sup>st</sup> PT, it is expected that there are **4 vacua** with  $\langle S \rangle = \pm w_d e^{\pm i\alpha}$  left in the Universe, each with the same volume.

➤ Note that **vacua with positive phases** would produce **negative baryon asymmetry** during EWPT, which would **cancel** the positive baryon numbers created in vacua of negative phase.

D. Comelli, et al., arXiv: 9304267;  
J. McDonald, PLB **323**, 339 (1994);  
PLB **357**, 19 (1995);



## Possible Solution with Explicit CPV

➤ One possible solution is to introduce a **small explicit CPV phase** in the scalar potential, which uplifts the vacua degeneracy so that the ones with **negative phases** are favored.

➤ **Example:** Explicit CPV in quartic term **S<sup>4</sup>**

$$V_4 = \frac{\lambda_2 e^{i\delta}}{4} S^4 + \frac{\lambda_2 e^{-i\delta}}{4} S^{*4} + \frac{\lambda_2}{2} |S|^4,$$

So that the vacua  $(0, \pm w_d e^{i\alpha} / \sqrt{2})$  have the potential density

$$V_T^+ = \frac{1}{8} \lambda_2 w_d^4 \cos(\delta + 4\alpha) + V_T^{\text{CP}},$$

while the potential for vacua  $(0, \pm w_d e^{-i\alpha} / \sqrt{2})$  is

$$V_T^- = \frac{1}{8} \lambda_2 w_d^4 \cos(\delta - 4\alpha) + V_T^{\text{CP}},$$

D. Comelli, et al., arXiv:  
hep-ph/9304267;  
J. McDonald, PLB **323**,  
339 (1994);  
PLB **357**, 19 (1995);

➤ **Potential difference:**  $\Delta V_T = -\frac{1}{4} \lambda_2 w_d^4 \sin(4\alpha) \sin \delta$

## Possible Solution with Explicit CPV

- It is shown that the disappearance of the wrong-sign vacua can proceed via **the movement of the domain walls** interpolating between the wrong- and right-sign vacua.

H. Lew and A. Riotto, arXiv: hep-ph/9304203; J.McDonald, PLB **357**, 19 (1995);

- The domain wall begin to move when the energy scale of the **potential difference** approaches that of its **surface energy**  $\eta_{\text{DW}} \sim w_d^3$ . Thus, the time for bubble wall movement is

$$t_{\text{DW}} \approx \frac{\eta_{\text{DW}}}{|\Delta V_T|} \sim \frac{1}{|\lambda_2 \sin(4\alpha) \sin \delta| w_d}.$$

- Our picture of EWBG requires to eliminate the wrong-sign domains at least **before the EWPT** with the time  $t_{\text{EW}} \sim M_{\text{Pl}}/T_c^2$

$$|\sin \delta| > \frac{T_c^2}{|\lambda_2 \sin(4\alpha)| w_d M_{\text{Pl}}} \sim \frac{T_c^2}{|\lambda_2 \sin(4\alpha)| w_c M_{\text{Pl}}},$$



# Possible Solution with Explicit CPV

- Typical EWPT parameters:

$T_c \sim 100 \text{ GeV}$ ,  $w_c \sim 100 \text{ GeV}$ ,  $|\sin(4\alpha)| \sim 0.1$ ,  $|\lambda_2| \sim \mathcal{O}(0.1)$   
the needed CPV phase can be as small as  $\mathcal{O}(10^{-15})$ .

- It is obvious that such a small CPV phase **cannot** have any visible effects under the current experimental status.

- For the domain walls **separating the two right-sign vacua**  $(0, \pm w_d e^{-i\alpha} / \sqrt{2})$ , one would worry that they might dominate the energy density and change the evolution of the Universe.

- However, these domain walls would **decay** immediately after the  $Z_2$  symmetry is restored at the EWPT with  $T_c \sim 100 \text{ GeV}$ , which is **well before** their domination time at  $T \sim 10^{-7} \text{ GeV}$ .

J. R. Espinosa, et al. arXiv: 1110.2876; J. M. Cline and K. Kainulainen, arXiv: 1210.4196

# Problems with Exact CP Symmetry

- In the model with an exact **dark CP symmetry**, when this CP spontaneously breaks at high-T, there must exist regions with **positive VEV CPV phase** ( $\alpha > 0$ ) with the same volume as the ones with negative phase.
- The regions with **positive phase** would produce the **negative baryon number** in the EWPT.
- Thus, when the EWPT finishes, the opposite baryon numbers created in these two kinds of regions will cancel each other, so that there is **NO** net baryon number left in the Universe.

# Scanning Results

- Constraining power of **DM direct searches**

