

Dark side of the seesaw

Ivo de Medeiros Varzielas

CFTP, Instituto Superior Técnico, Universidade de Lisboa

Workshop on Multi-Higgs Models, Lisbon, 2018/09/07



Dark side of the seesaw

Ivo de Medeiros Varzielas

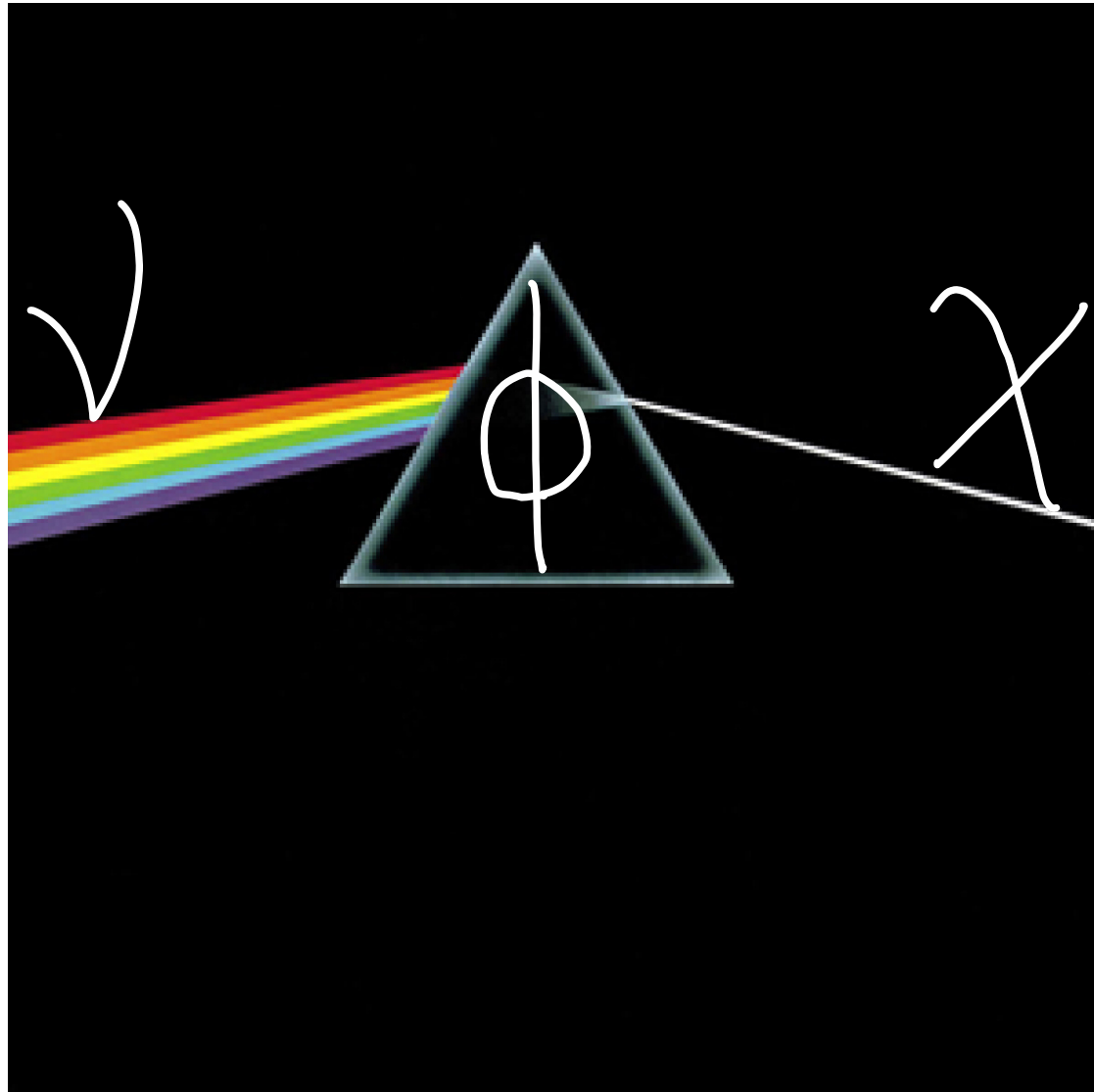
CFTP, Instituto Superior Técnico, Universidade de Lisboa

Workshop on Multi-Higgs Models, Lisbon, ~~2018/09/07~~

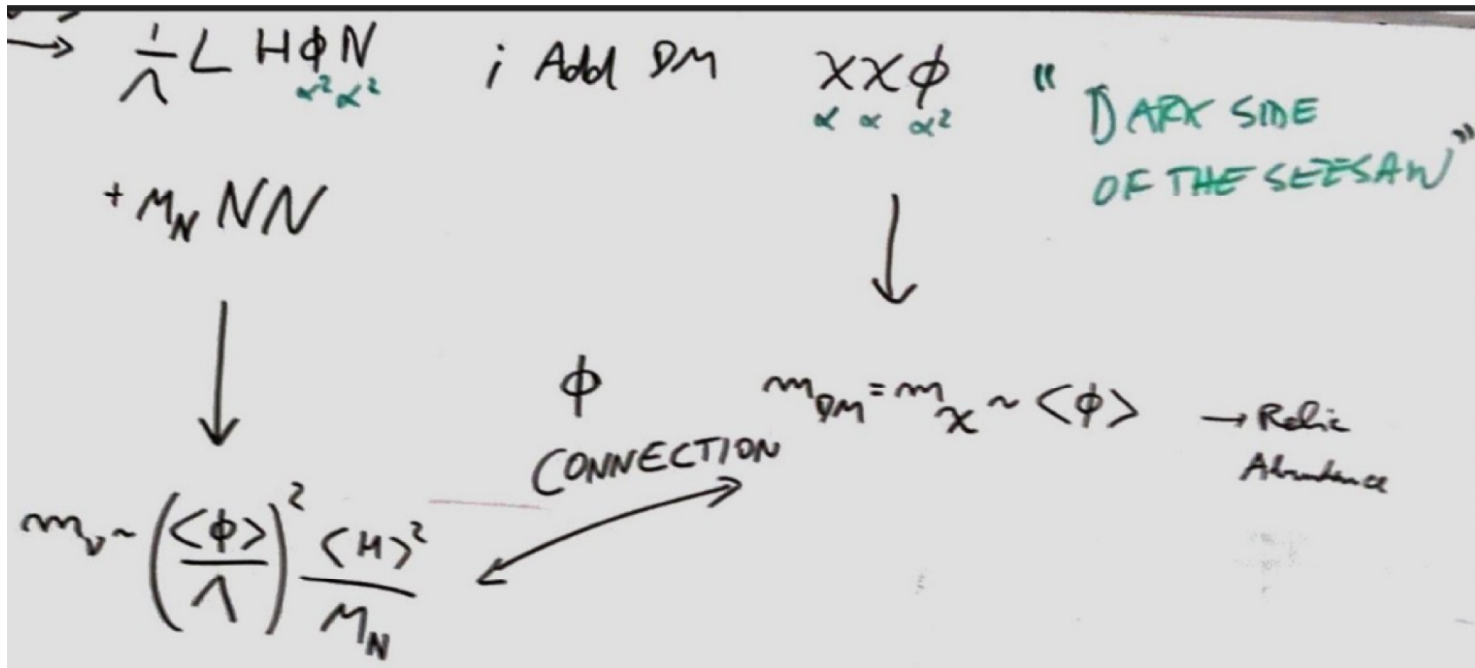
2016/09/09







Idea from 2016





Life is a
piece of
Lith,

9

When you
LuKe
at it...

Paper from 2018

Dark side of the Seesaw

Subhaditya Bhattacharya, Ivo de Medeiros Varzielas, Biswajit Karmakar, Stephen F. King, Arunansu Sil

(Submitted on 1 Jun 2018)

In an attempt to unfold (if any) a possible connection between two apparently uncorrelated sectors, namely neutrino and dark matter, we consider the type-I seesaw and a fermion singlet dark matter to start with. Our construction suggests that there exists a scalar field mediator between these two sectors whose vacuum expectation value not only generates the mass of the dark matter, but also takes part in the neutrino mass generation. While the choice of Z_4 symmetry allows us to establish the framework, the vacuum expectation value of the mediator field breaks Z_4 to a remnant Z_2 , that is responsible to keep dark matter stable. Therefore, the observed light neutrino masses and relic abundance constraint on the dark matter, allows us to predict the heavy seesaw scale as illustrated in this paper. The methodology to connect dark matter and neutrino sector, as introduced here, is a generic one and can be applied to other possible neutrino mass generation mechanism and different dark matter candidate(s).

Comments: 28 pages, 16 figures

Subjects: **High Energy Physics - Phenomenology (hep-ph)**

Cite as: [arXiv:1806.00490](https://arxiv.org/abs/1806.00490) [hep-ph]

(or [arXiv:1806.00490v1](https://arxiv.org/abs/1806.00490v1) [hep-ph] for this version)

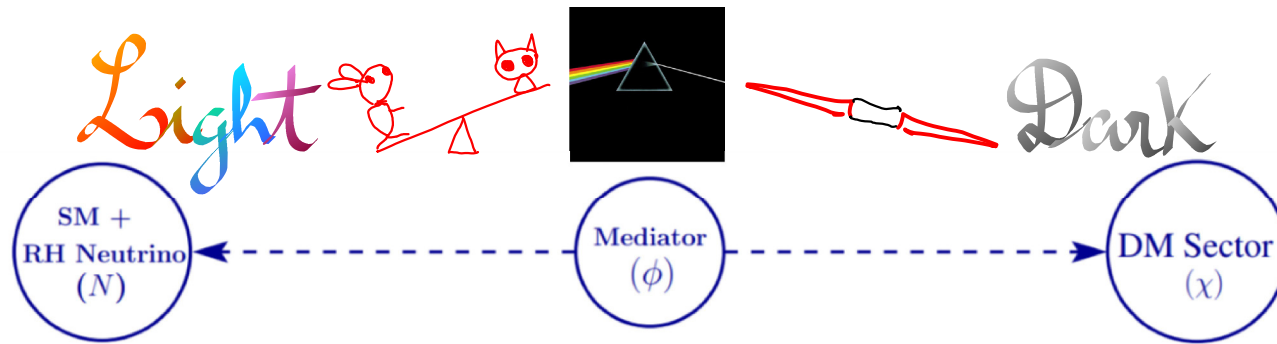


Figure 1: Schematic representation for DM interaction with SM through the scalar ϕ

Field	L	H	N	ϕ	χ
Z_4	0	0	2	2	1

Table 1: Transformation properties fields involved under Z_4 in additive notation where charge q means: the field transforms like $e^{i2\pi q/4}$.

Z_4

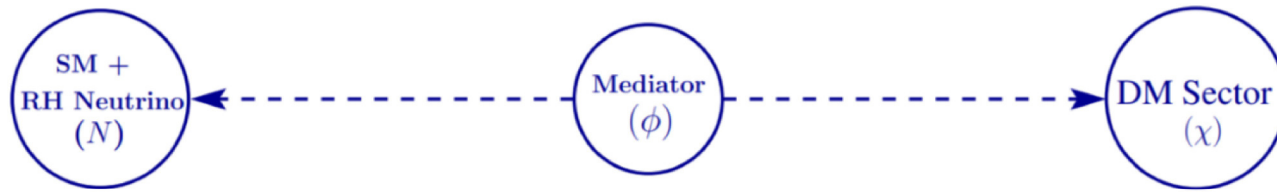


Figure 1: Schematic representation for DM interaction with SM through the scalar ϕ

$$\begin{array}{ccc}
 \frac{1}{\Lambda} \bar{L} \tilde{H} \phi N + M_N \bar{N}^c N & & y \phi \bar{\chi}^c \chi \\
 \downarrow & & \downarrow \\
 m_\nu \propto \frac{\langle \phi \rangle^2 \langle H \rangle^2}{\Lambda^2 M_W} & \leftarrow \phi \rightarrow & M_\chi \propto \langle \phi \rangle
 \end{array}$$

$$V(H, \phi) = -\mu_1^2 H^\dagger H + \lambda_1 (H^\dagger H)^2 - \frac{1}{2} \mu_2^2 \phi^2 + \frac{1}{4} \lambda_2 \phi^4 + \frac{1}{2} \underbrace{\lambda_{12} \phi^2 H^\dagger H}_{\text{Portal}}$$

$$H = \begin{pmatrix} 0 \\ v + \tilde{h} \end{pmatrix} / \sqrt{2} \quad \xrightarrow{\quad \quad \quad} \quad \xrightarrow{\quad \quad \quad} \quad \phi = u + h'$$

$$M_{h, h'}^2 = \begin{pmatrix} 2\lambda_1 v^2 & \lambda_{12} v u \\ \lambda_{12} v u & 2\lambda_2 u^2 \end{pmatrix}$$

Diagonalise

↓
Mass eigenstates

h, H'

↓
 $m_h, m_{H'}$
↓
 $\sin \theta$

Simplifying assumption : $\lambda_1 = \lambda_2 = \lambda$ (general case in App)

$$m_h^2 = \lambda(v^2 + u^2) - \sqrt{\lambda^2(v^2 - u^2)^2 + \lambda_{12}^2 u^2 v^2}$$

$$m_{H'}^2 = \lambda(v^2 + u^2) + \sqrt{\lambda^2(v^2 - u^2)^2 + \lambda_{12}^2 u^2 v^2}$$

$$\sin 2\theta = \frac{\lambda_{12} uv}{\sqrt{(\lambda_1 v^2 - \lambda_2 u^2)^2 + \lambda_{12}^2 u^2 v^2}}$$

Two options :

1. $m_{H'} = m_{h_{SM}}$ & $m_h = m_{H_{light}}$, with $H_{light} \sim h' (\phi)$
 $\sin \theta \gtrsim 0.9$

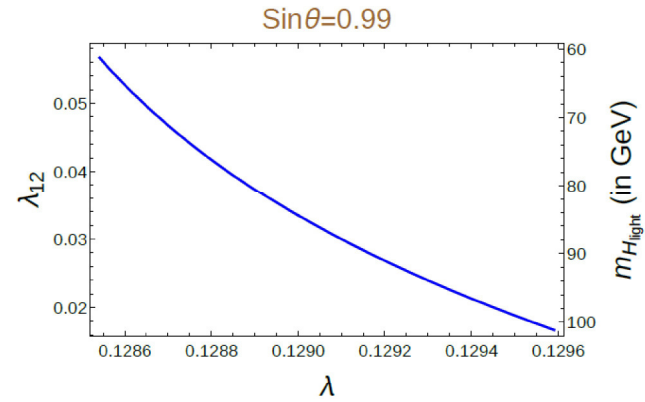
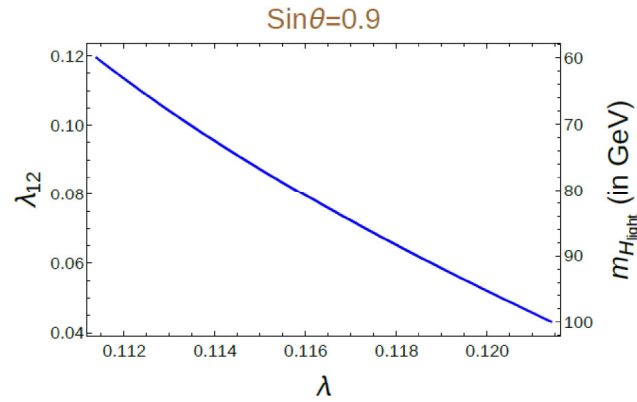
"Low mass region"

2. $m_h = m_{h_{SM}}$ & $m_{H'} = m_{H_{heavy}}$
 $\sin \theta \lesssim 0.3$

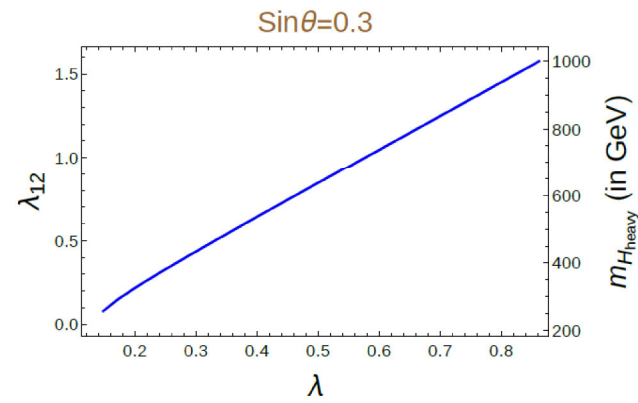
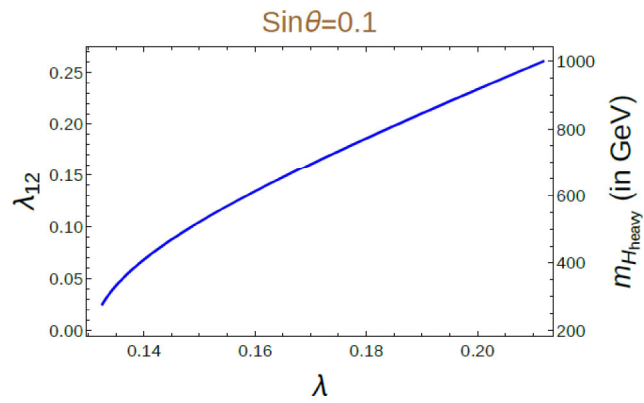
"High mass region"

$m_{h_{SM}}$ fixed; fixing $m_{H_{light}}$ or $m_{H_{heavy}}$ and $\sin\theta$...

1.



2.



$\langle \phi \rangle = u$ depends on V, \dots

1.

Benchmark Points $m_{H_{\text{light}}}$ (GeV)	u (GeV)		λ		λ_{12}	
	$s_\theta = 0.999$	$s_\theta = 0.9$	$s_\theta = 0.999$	$s_\theta = 0.9$	$s_\theta = 0.999$	$s_\theta = 0.9$
60	117.91	162.98	0.1303	0.1114	0.0188	0.1194
80	156.89	188.01	0.1304	0.1158	0.0109	0.0797
100	195.89	213.80	0.0827	0.1214	0.0034	0.0433

Table 2: Vacuum Expectation value of singlet scalar (u) and the dimensionless couplings in the scalar potential ($\lambda_1 = \lambda_2 = \lambda, \lambda_{12}$) evaluated at some selected benchmark points for $m_{H_{\text{light}}} = 60, 80,$ and 100 GeV with $\sin \theta = 0.999(0.90), m_{h_{\text{SM}}} = 125.7$ GeV with SM Higgs vev $v = 246$ GeV.

2.

Benchmark Points $m_{H_{\text{heavy}}}$ (GeV)	u (GeV)		λ		λ_{12}	
	$s_\theta = 0.3$	$s_\theta = 0.001$	$s_\theta = 0.3$	$s_\theta = 0.001$	$s_\theta = 0.3$	$s_\theta = 0.001$
200	356.81	391.41	0.1485	0.1306	0.0789	0.0003
400	556.02	782.81	0.2378	0.1306	0.3017	0.0008
600	662.42	1174.21	0.3865	0.1306	0.6138	0.0012
800	700.61	1565.60	0.5947	0.1306	1.0365	0.0016
1000	726.93	1956.98	0.8624	0.1306	1.5751	0.0020

Table 3: Values obtained for $\lambda_1 = \lambda_2 = \lambda$ and vev u (in GeV) for some chosen heavy Higgs masses $m_{H_{\text{heavy}}} = 200, 400, 600$ and 1000 GeV and two extreme values of mixing angles $\sin \theta = 0.3 (0.001), m_{h_{\text{SM}}} = 125.7$ GeV and $v = 246$ GeV.

DM Phenom

3 Parameters : M_χ , $\sin \Theta$, $m_{H_{light}}$ or $m_{H_{heavy}}$

$(\lambda_1 = \lambda_2 = \lambda)$

Z_4 :

No ϕ^3



DM
Relic
Density

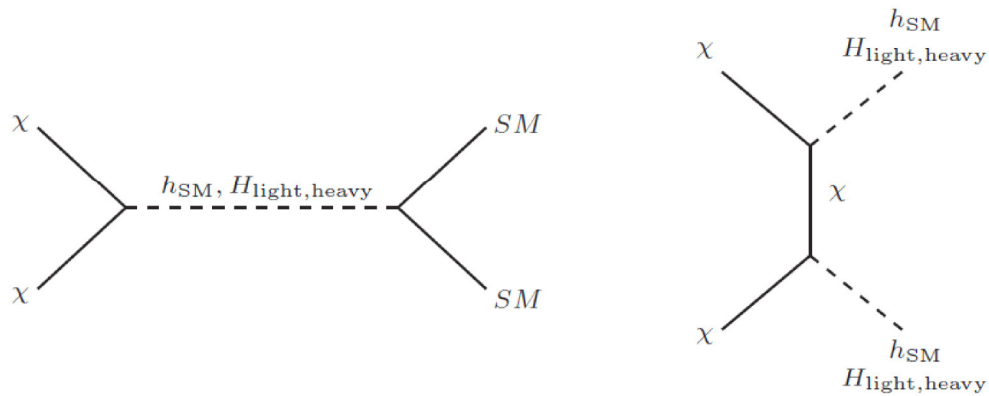
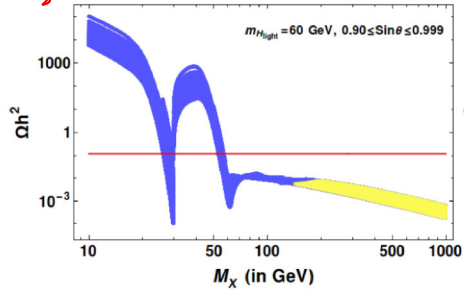


Figure 4: DM (χ) annihilation process that yield relic density of the DM.

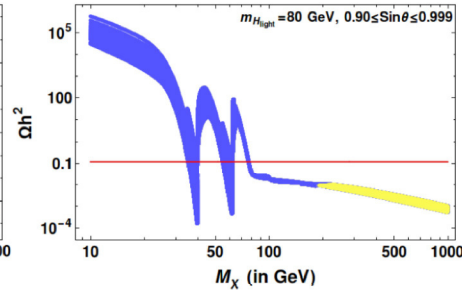
Relic Density

$m_{\text{light}} = 60$

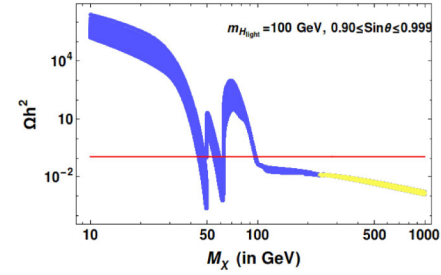
1.



80

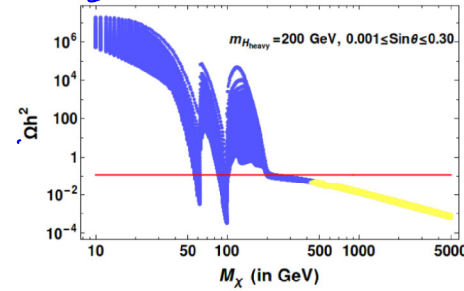


100

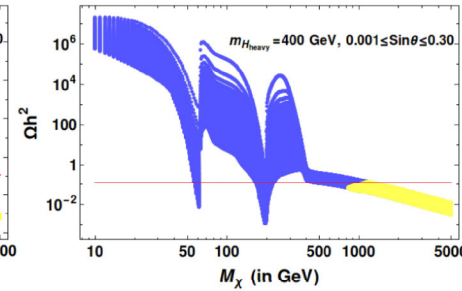


$m_{\text{heavy}} = 200$

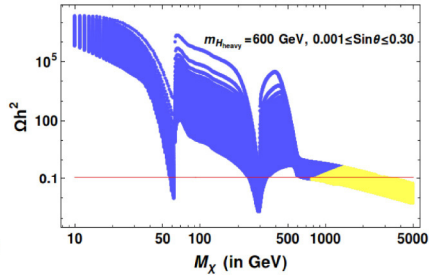
2.



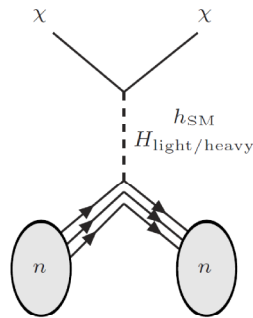
400



600



Direct search



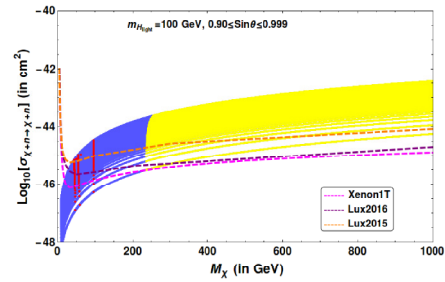
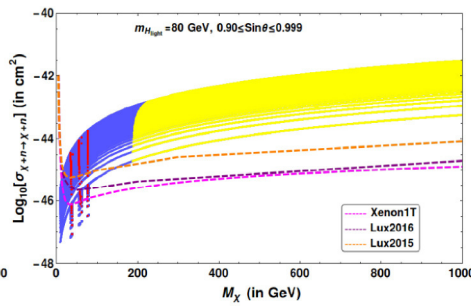
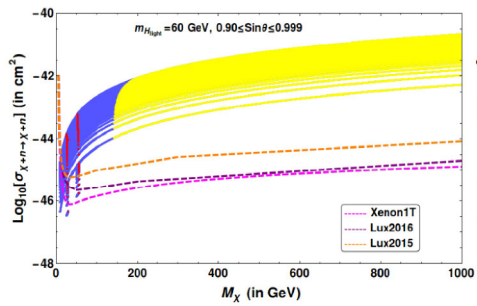
Red dots at Ω_{DM} relic density

$m_{\text{light}} = 60$

80

100

1.

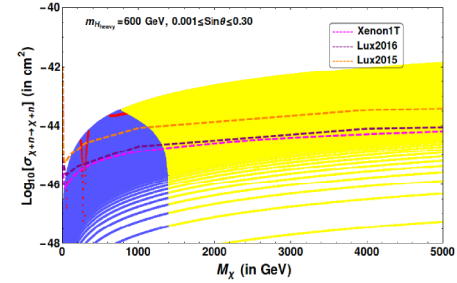
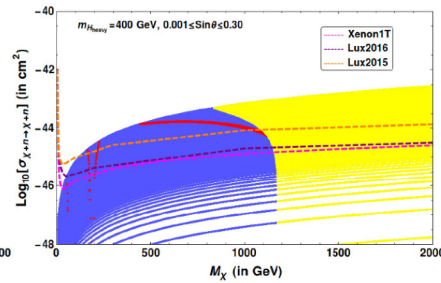
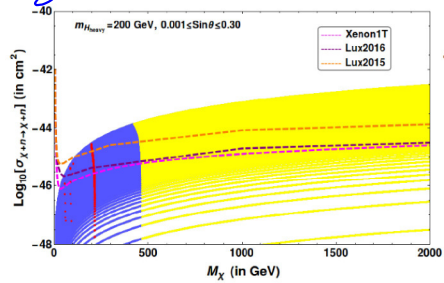


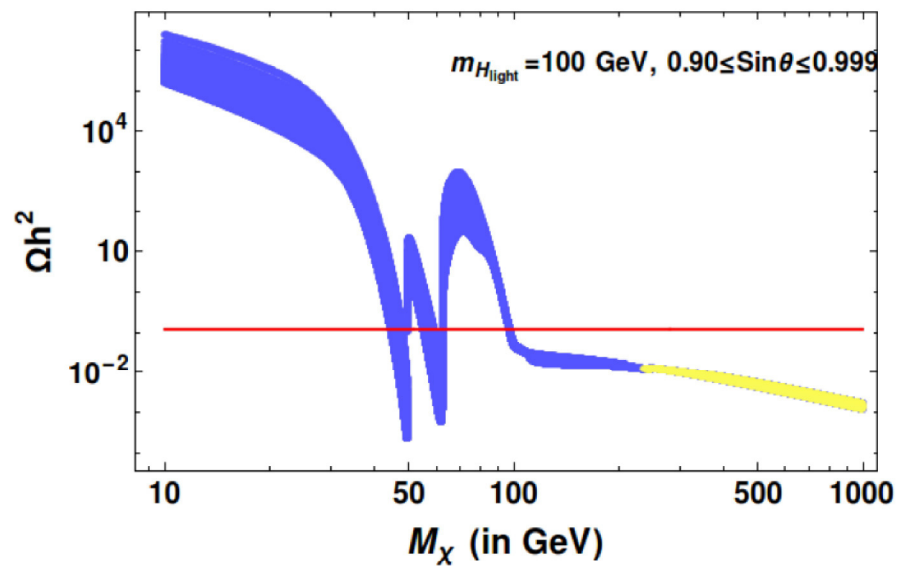
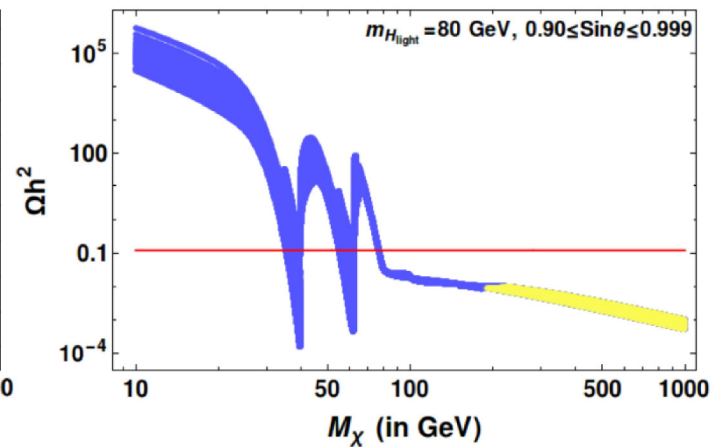
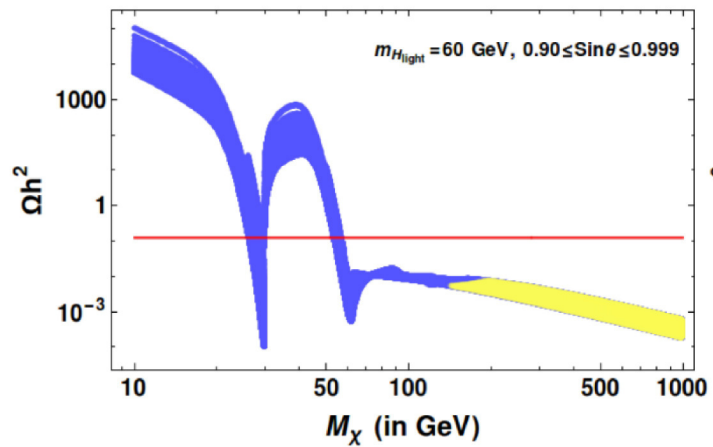
$m_{\text{heavy}} = 200$

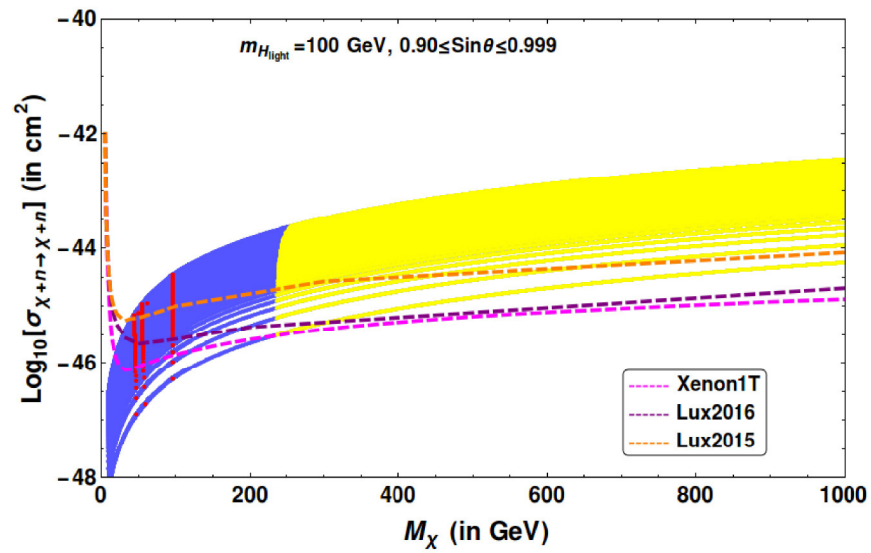
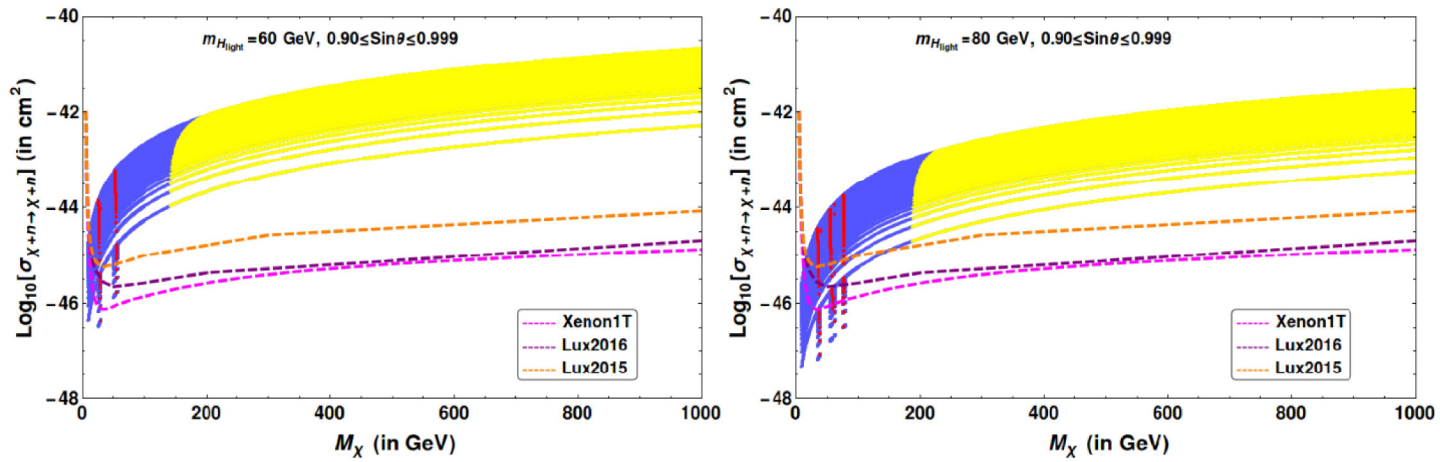
400

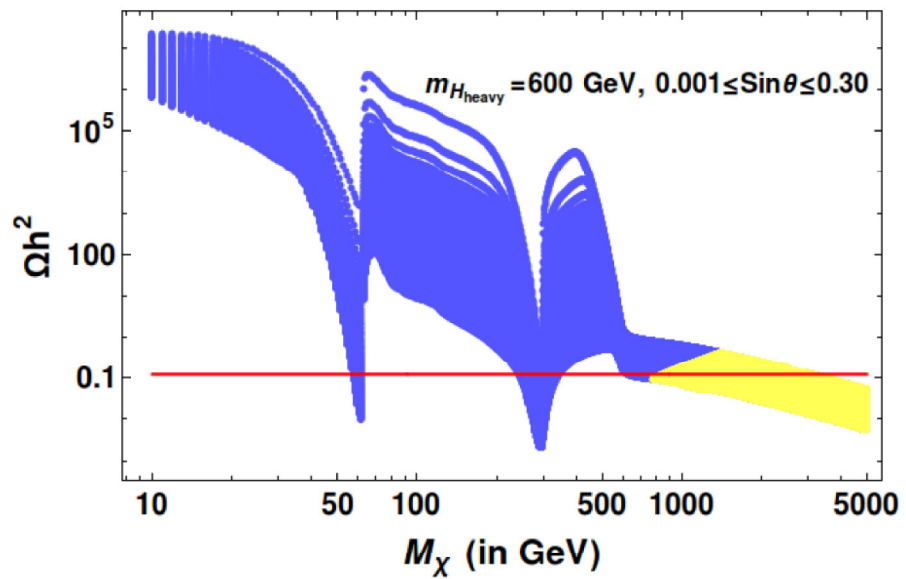
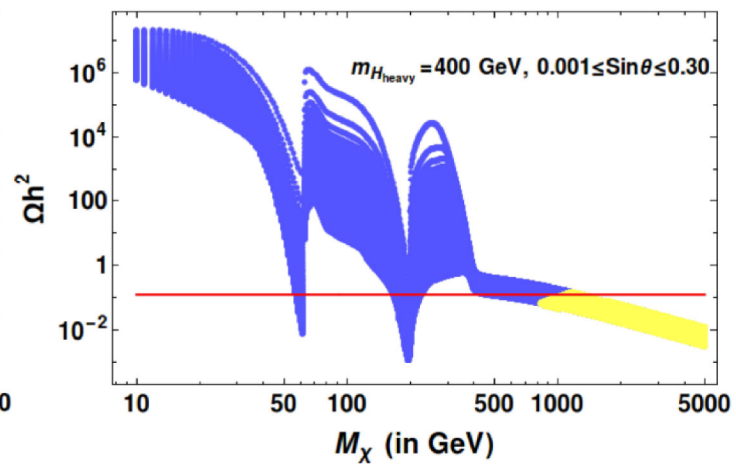
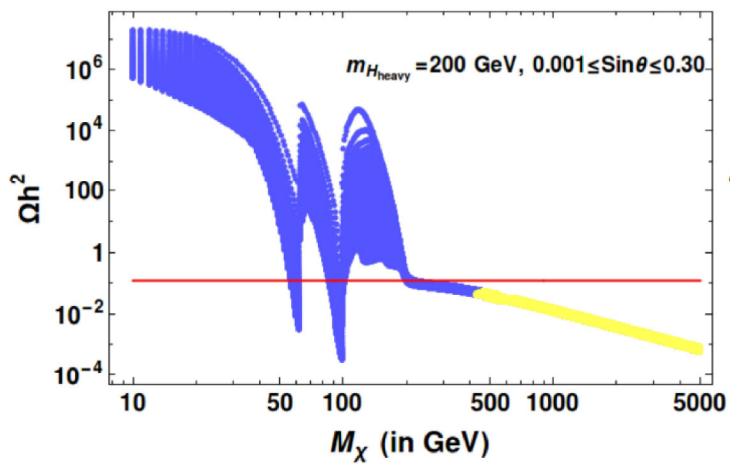
600

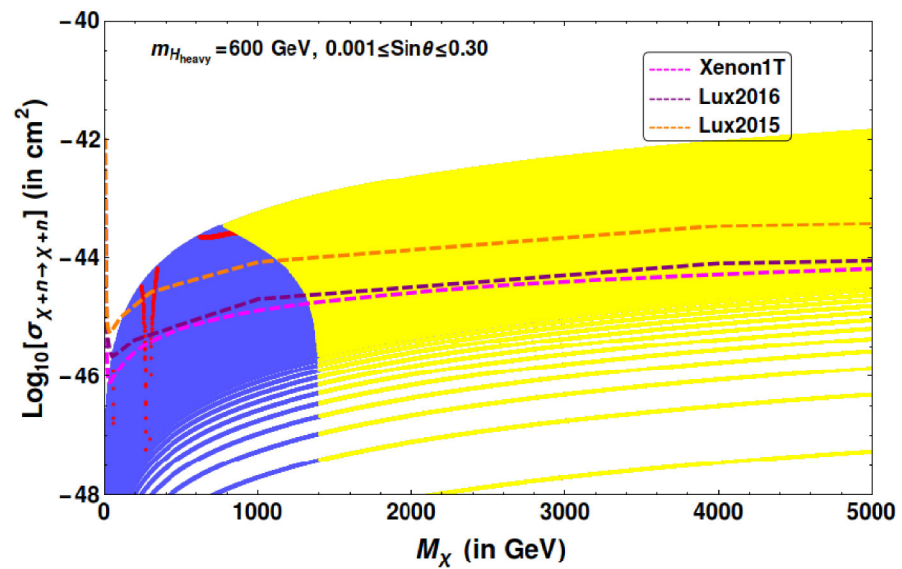
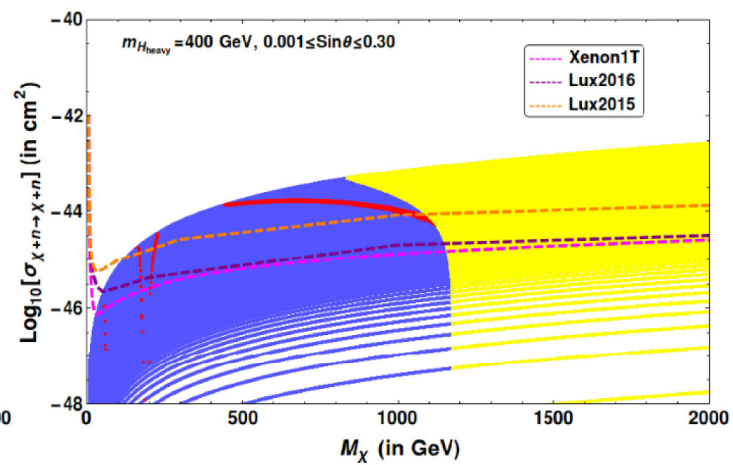
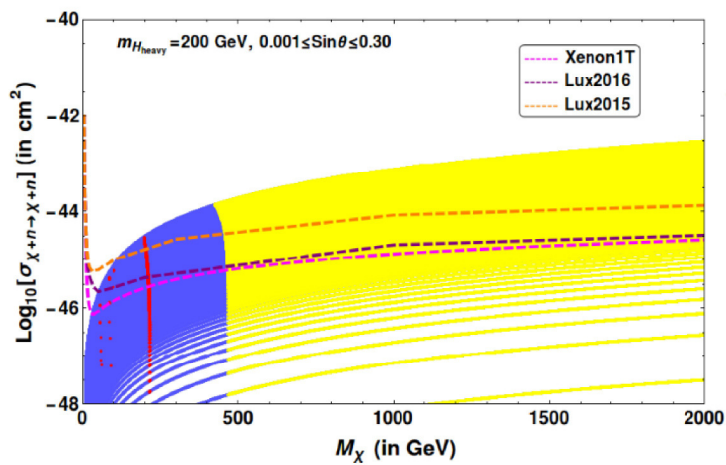
2.











Some viable benchmark points

Mass of the Scalar	$\sin \theta$	λ	λ_{12}	u GeV	y	M_χ GeV	Ωh^2	$\text{Log}_{10}[\sigma_{\text{SI}}] \times 10^{-45} \text{ cm}^2$
1. $m_{H_{\text{light}}} = 100$ GeV	0.993	0.13	0.019	196.99	0.236	46.59	0.118	-46.10
	0.996	0.13	0.011	196.45	0.292	57.46	0.121	-46.15
	0.998	0.13	0.008	196.08	0.496	97.34	0.121	-45.99
	0.999	0.13	0.005	195.89	0.497	97.40	0.119	-46.29
2. $m_{H_{\text{heavy}}} = 200$ GeV	0.069	0.133	0.017	389.43	0.154	60	0.122	-46.90
	0.031	0.131	.008	391.01	0.233	91	0.119	-47.23
	0.011	0.131	0.003	391.35	0.552	216	0.121	-47.37
$m_{H_{\text{heavy}}} = 400$ GeV	0.129	0.150	0.104	723.90	0.083	60	0.120	-46.55
	0.115	0.146	0.091	735.04	0.278	204	0.118	-45.60
	0.011	0.131	0.008	782.34	1.600	1251	0.120	-46.10
$m_{H_{\text{heavy}}} = 600$ GeV	0.165	0.208	0.248	918.13	0.065	60	0.119	-46.50
	0.093	0.155	0.121	1072.67	0.283	304	0.118	-45.70
	0.011	0.131	0.013	1172.61	2.400	2815	0.120	-45.69

Table 6: Benchmark points for both low and high mass regions satisfying dark matter relic density and direct search constraints.

Seesaw Mechanism

$$m_\nu \propto \frac{\langle \phi \rangle^2 \langle H \rangle^2}{\Lambda^2 M_N} \leftarrow \phi \rightarrow M_\chi \propto \langle \phi \rangle$$

$$m_\nu = \frac{v^2 u^2}{\Lambda^2 M_N} = \frac{v^2 (M_\chi / \Lambda)^2}{y^2 M_N}$$

← y
because I know u

→ $M_\chi = y u$
(u depends on V parameters)
 M_χ from Relic density

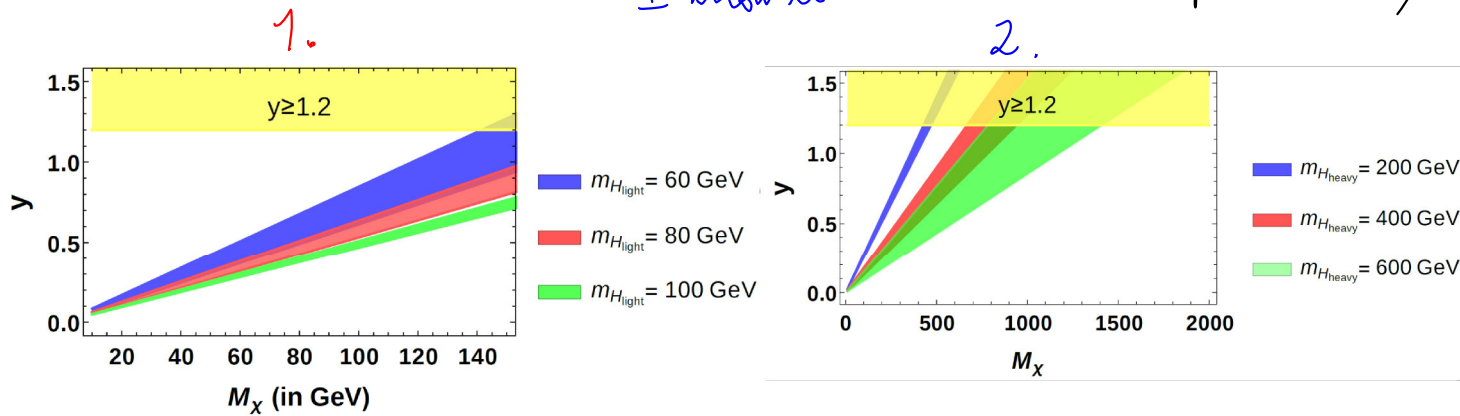
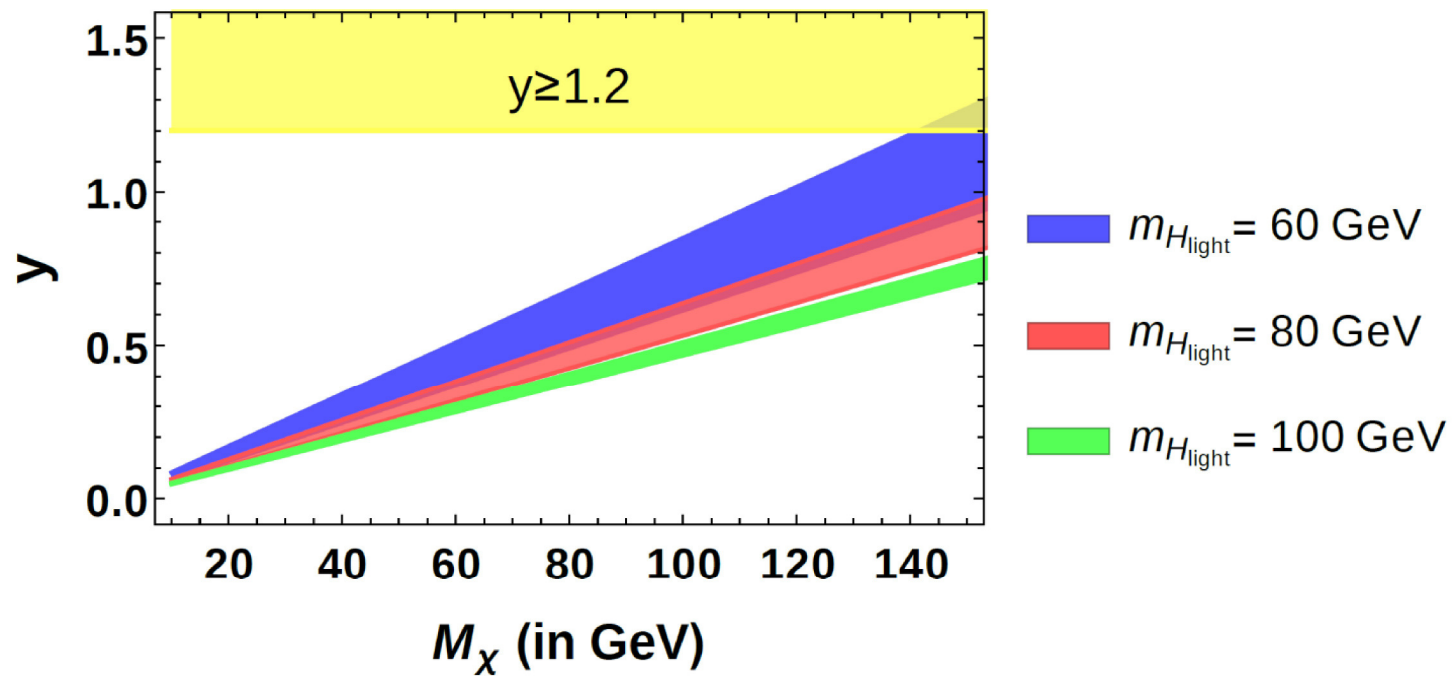
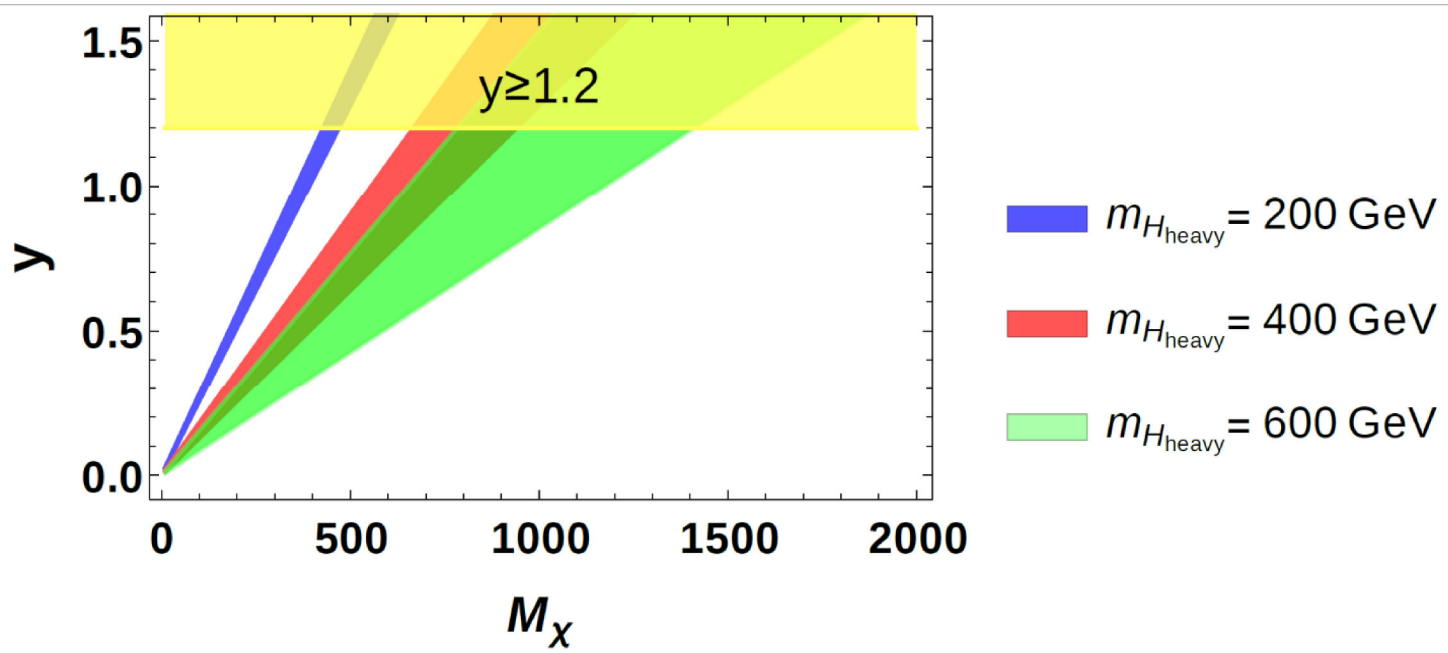


Figure 10: Left: Yukawa coupling (y) vs DM mass M_χ in the low mass region for $m_{H_{\text{light}}} = 60, 80$ and 100 GeV with $0.90 \leq \sin \theta \leq 0.999$. Right: y vs M_χ for high mass region with $m_{H_{\text{heavy}}} = 200, 400, 600, 800$ and 1000 GeV for $0.001 \leq \sin \theta \leq 0.3$.





Cosmological bound: Relate M_N & Λ (for fixed M_X, κ, ν, y)

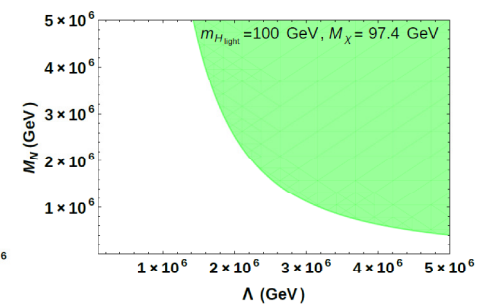
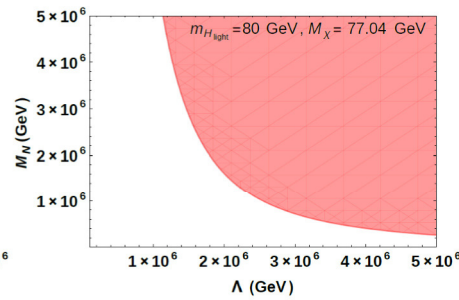
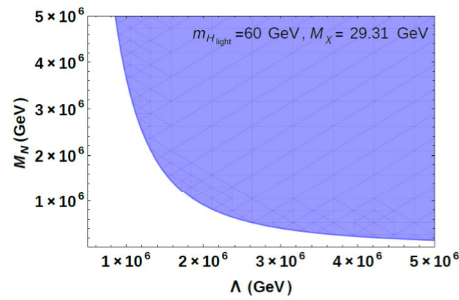
$$m_\nu = \frac{v^2 u^2}{\Lambda^2 M_N} = \frac{v^2 (M_X/\Lambda)^2}{y^2 M_N} \rightarrow \frac{v^2 M_X^2}{y^2 \Lambda^2 M_N} \leq 0.23 \text{ eV.}$$

$m_{\text{light}} = 60$

80

100

1.



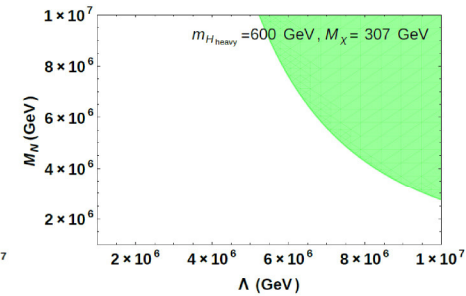
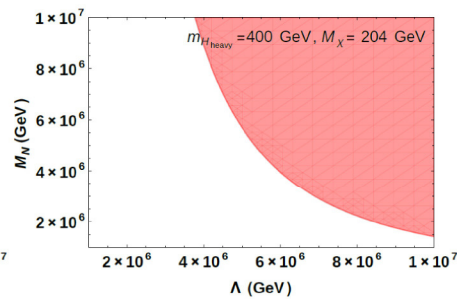
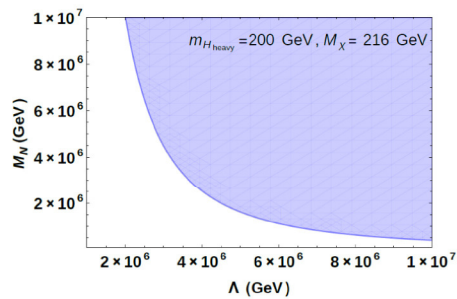
$m_{\text{heavy}} =$

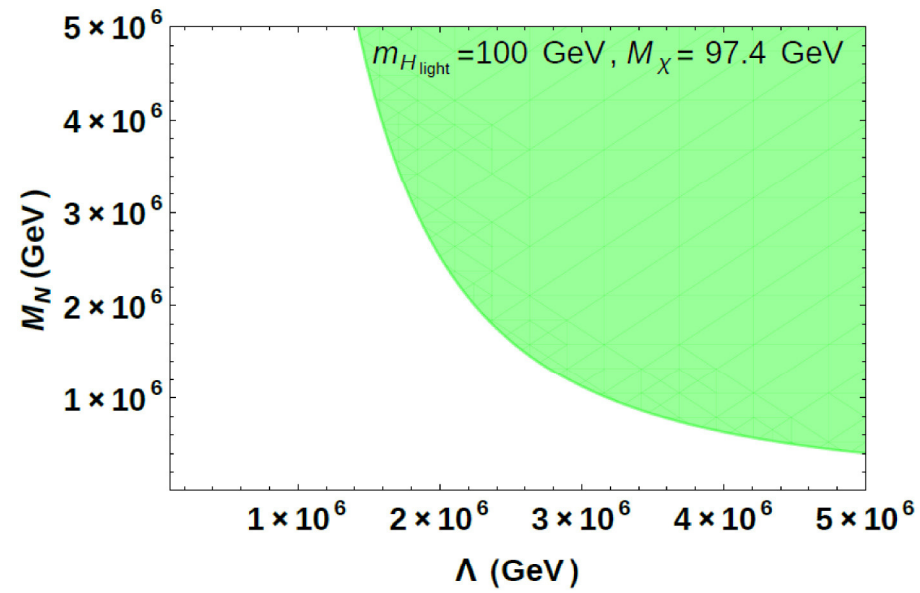
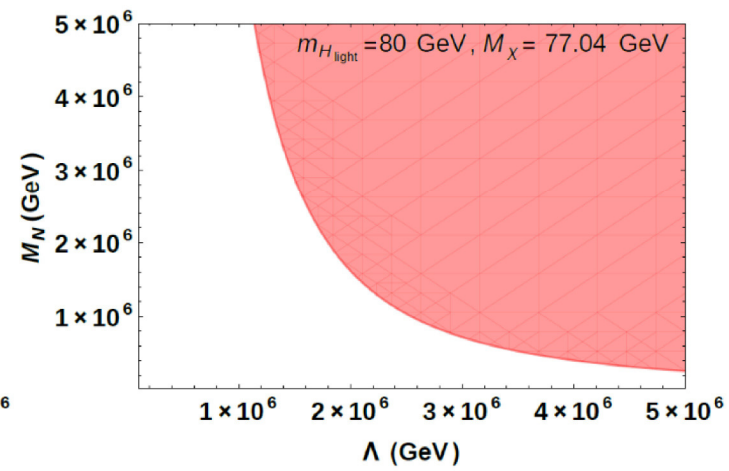
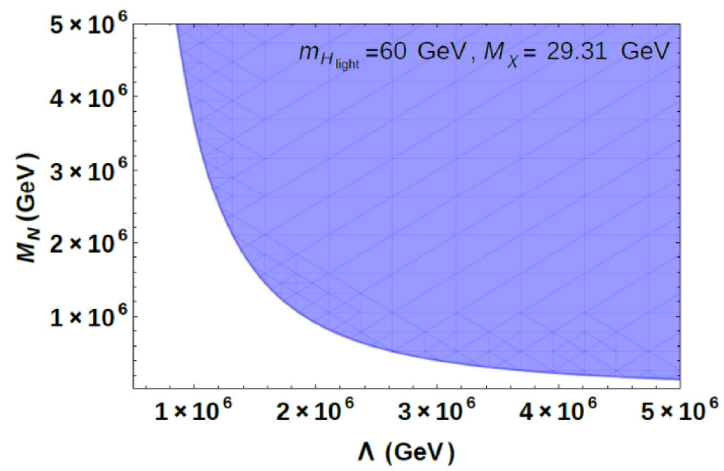
200

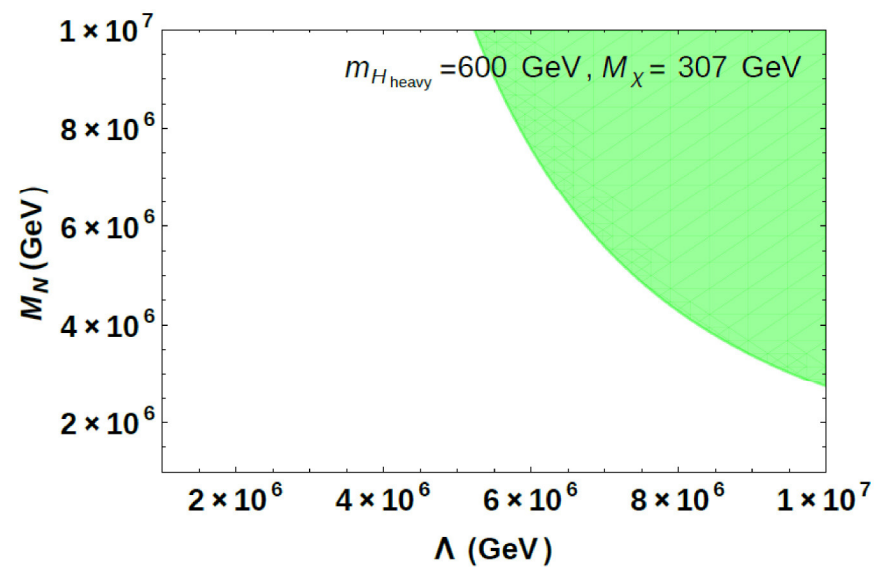
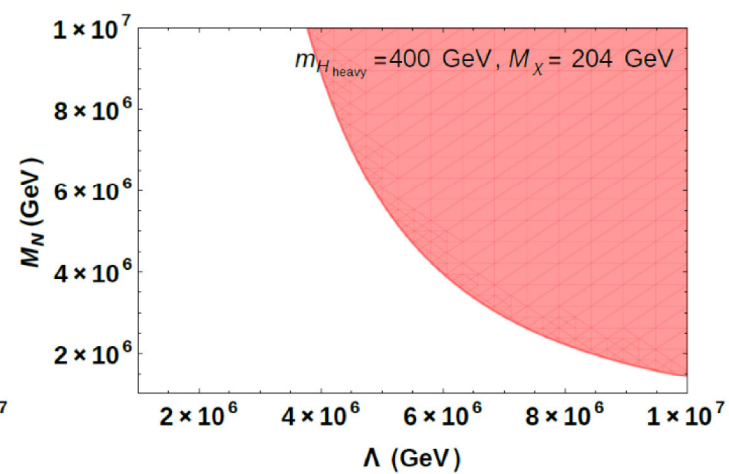
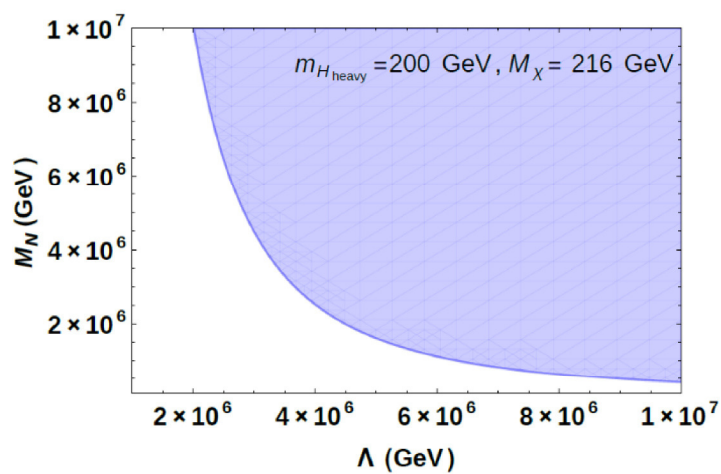
400

600

2.







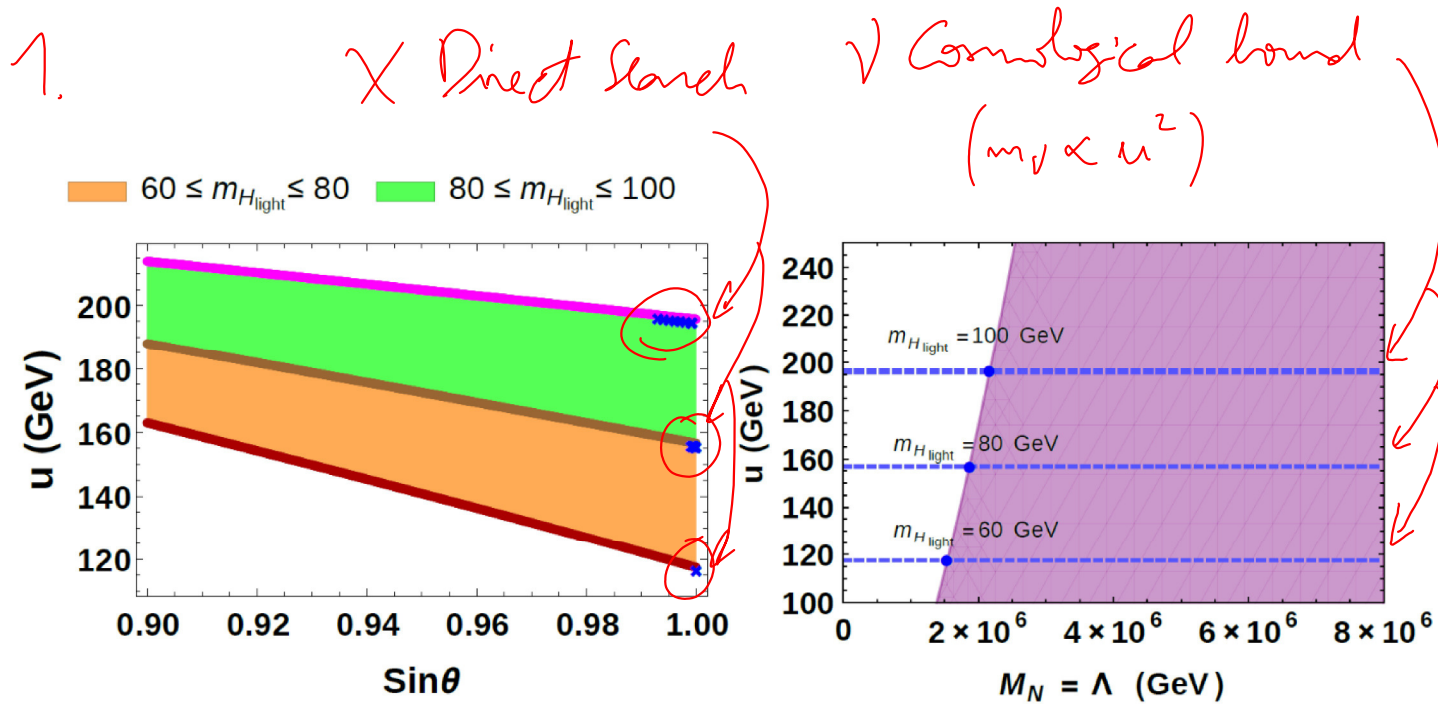


Figure 13: Left panel: $u(= M_\chi/y)$ vs $\sin\theta$ plot for $\lambda_1 = \lambda_2 = \lambda$ for various range of $m_{H_{\text{light}}}$. Here the magenta, brown and dark red dots represent allowed points obtained (from Fig. [5]) relic density only for $m_{H_{\text{light}}} = 100, 80$ and 60 GeV. Blue dots on each line are actual allowed points which also satisfies direct search limit. Right panel: $u(= M_\chi/y)$ as a function of Λ (or M_N) considering $M_N = \Lambda$ in Eq. [21] and [22]. Purple shaded region represents $m_\nu \leq 0.23$ eV with $M_N = \Lambda$ and the horizontal blue patch represents the allowed region of $u(= M_\chi/y)$ obtained the left panel. This imposes a stringent constraint on the lower limit of the cut-off scale Λ (and RH neutrino mass M_N).

2 X Direct search

V Cosmological bound

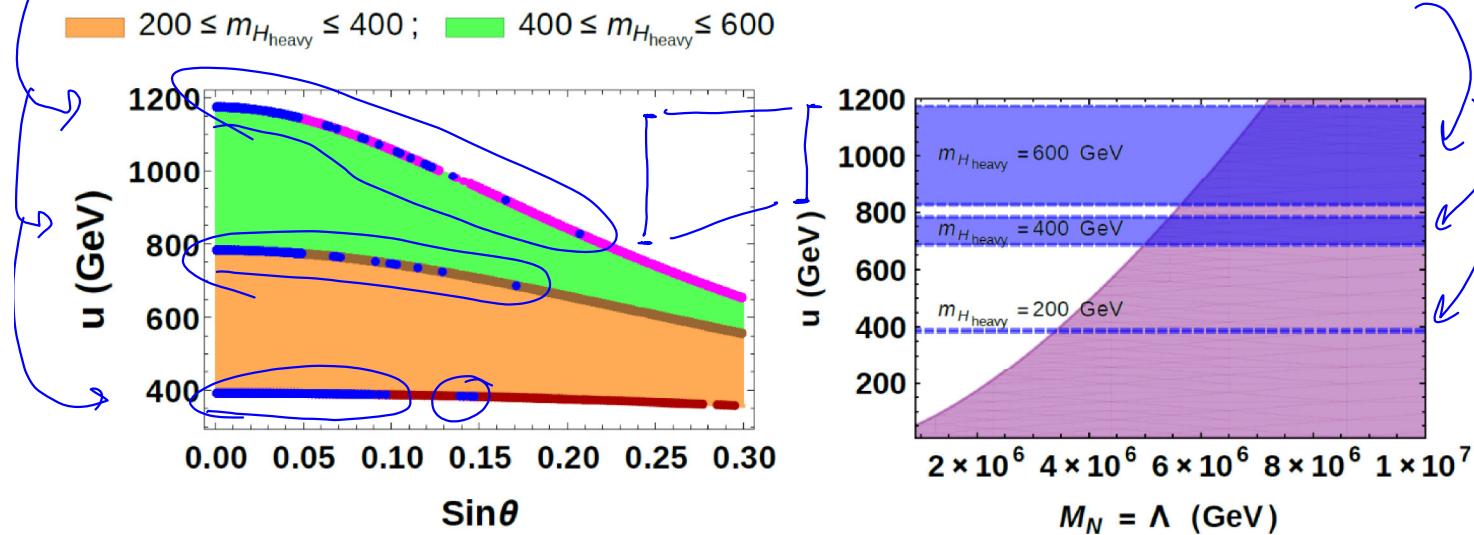
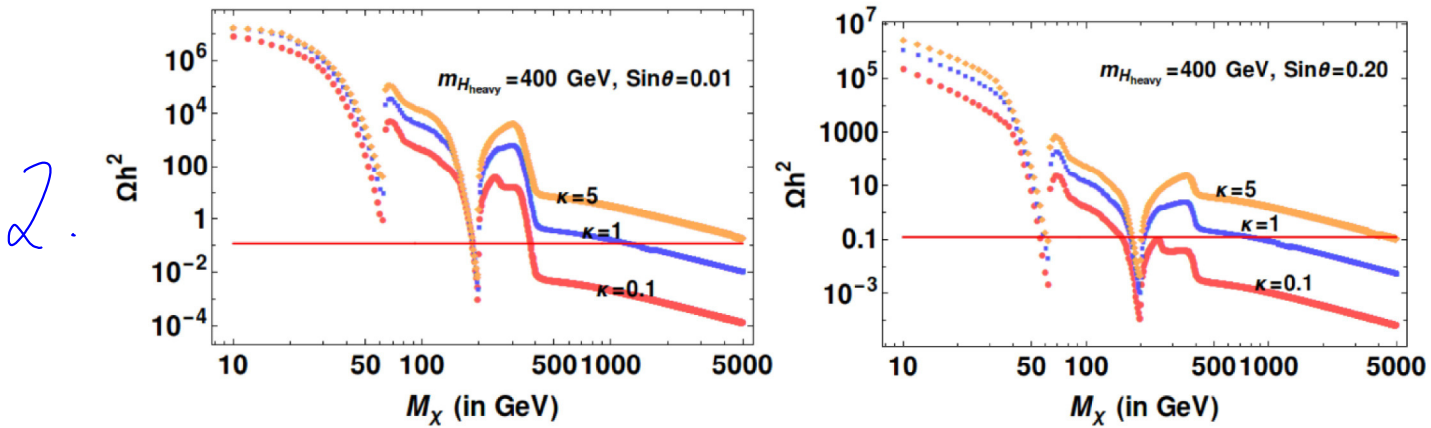
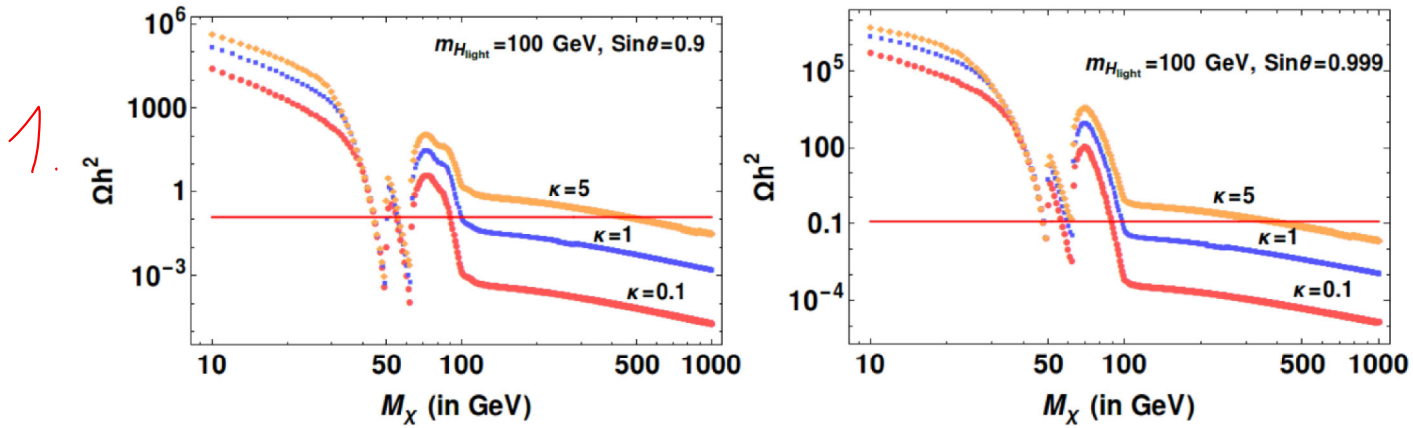


Figure 14: Left panel: $u(= M_\chi/y)$ vs $\sin\theta$ plot for $\lambda_1 = \lambda_2 = \lambda$ for $200 \leq m_{H_{\text{heavy}}} \leq 400$ GeV (orange shaded region) and $400 \leq m_{H_{\text{heavy}}} \leq 600$ GeV (green shaded region) respectively. Here the magenta, brown and deep red dots represent allowed points obtained (from Fig. [8]) relic density only, for $m_{H_{\text{light}}} = 100, 80$ and 60 GeV. Blue dots on each line are actual allowed points which also satisfies direct search limit. Right panel: $u(= M_\chi/y)$ as a function of Λ (or M_N) considering $M_N = \Lambda$ in Eq. [21] and [22]. Purple shaded region represents $m_\nu \leq 0.23$ eV with $M_N = \Lambda$ and the horizontal blue patch represents the allowed region of $u(= M_\chi/y)$ obtained the left panel. This imposes a constraint on the lower limit of the cut-off scale Λ (and RH neutrino mass M_N).

$\lambda_1 \neq \lambda_2$; $\kappa \equiv \lambda_1/\lambda_2 \rightarrow$ Allows bigger ranges of M_X



Conclusions

Dark side of the seesaw relates ν & DMB through ϕ
DMB phenomenology then gives information about
 $M_{N_i} \gtrsim 10^6 \text{ GeV}$

1. "Low mass region", $M_X \sim M_{\text{Hlight}}$, constrained
2. "High mass region", more parameter space

Conclusions

Dark side of the seesaw relates ν & DM through ϕ
DM phenomenology then gives information about
 $M_{N_i} \gtrsim 10^6 \text{ GeV}$

1. "Low mass region", $M_X \sim M_{\text{Hlight}}$, constrained
2. "High mass region", more parameter space

The End?



The End
... OR IS IT?



Non-Abelian family symmetries as portals to dark matter

Ivo de Medeiros Varzielas, Oliver Fischer

(Submitted on 2 Dec 2015)

Non-Abelian family symmetries offer a very promising explanation for the flavour structure in the Standard Model and its extensions. We explore the possibility that dark matter consists in fermions that transform under a family symmetry, such that the visible and dark sector are linked by the familons - Standard Model gauge singlet scalars, responsible for spontaneously breaking the family symmetry. We study three representative models with non-Abelian family symmetries that have been shown capable to explain the masses and mixing of the Standard Model fermions. One of our central results is the possibility to have dark matter fermions and at least one familon with masses on and even below the experimentally accessible TeV scale. In particular we discuss the characteristic signatures in collider experiments from light familon Fields with a non-Abelian family symmetry, and we show that run I of the LHC is already testing this class of models.

Comments: 16 pages plus references

Subjects: **High Energy Physics - Phenomenology (hep-ph)**; Cosmology and Nongalactic Astrophysics (astro-ph.CO)

DOI: [10.1007/JHEP01\(2016\)160](https://doi.org/10.1007/JHEP01(2016)160)

Cite as: [arXiv:1512.00869](https://arxiv.org/abs/1512.00869) [**hep-ph**]

(or [arXiv:1512.00869v1](https://arxiv.org/abs/1512.00869v1) [**hep-ph**] for this version)

Somewhat similar ideas, but with NADS (A_4)

2 Models: ϕ_l & ϕ_ν

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_\chi + \mathcal{L}_\phi.$$

$$\mathcal{L}_\phi = -c_{\phi,s}[\phi_l\phi_l^\dagger]_s[\phi_l\phi_l^\dagger]_s - c_1[\phi_l\phi_l^\dagger]_1[\phi_l\phi_l^\dagger]_1 - c_2[\phi_l\phi_l^\dagger]_{1'}[\phi_l\phi_l^\dagger]_{1''} - c_{\phi_e H}[\phi_l\phi_l^\dagger]\underbrace{H^\dagger H}_{\text{Portal}}$$



	χ	χ_1^c	χ_2^c	χ_3^c	ν^c	L	e^c	μ^c	τ^c	H	ϕ_ℓ
A_4	3	1	1''	1'	3	3	1	1''	1'	1	1
$U(1)_{B-L}$	0	0	0	0	1	-1	1	1	1	0	0

Table I: Field assignment within $A_4 \times U(1)_{B-L}$. New fields are gauge singlets with respect to the SM gauge group. The SM gauge charges for the SM fields are unchanged.

$$A_4 : \langle \phi_l \rangle = (u, 0, 0)$$

$$O_{eff}^{d=5} \supset \frac{H}{\Lambda} (y_e [\phi_\ell L_i] e^c + y_\mu [\phi_\ell L_i]' \mu^c + y_\tau [\phi_\ell L_i]'' \tau^c)$$

$$\mathcal{L}_\chi \supset -y_{\chi_1} [\phi_\ell \chi] \chi_1^c - y_{\chi_2} [\phi_\ell \chi]' \chi_2^c - y_{\chi_3} [\phi_\ell \chi]'' \chi_3^c$$

$$\begin{array}{c}
 m_f \propto \mu \\
 \uparrow \\
 \langle \phi_f \rangle \\
 \downarrow \\
 M_\chi \propto \mu
 \end{array}$$



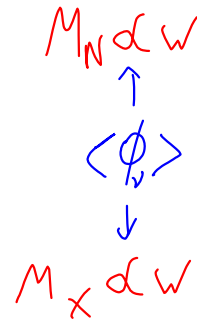
	χ	χ^c	ν^c	L	e^c	μ^c	τ^c	H	ϕ_ν
A_4	3	1	3	3	1	1''	1'	1	3
$U(1)_{B-L}$	0	2	1	-1	1	1	1	0	-2

Table II: Field assignment within $A_4 \times U(1)_{B-L}$. New fields are gauge singlets with respect to the SM gauge group. The SM gauge charges for the SM fields are unchanged.

~~A_4~~ : $\langle \phi_\nu \rangle = (w, w, w)$.

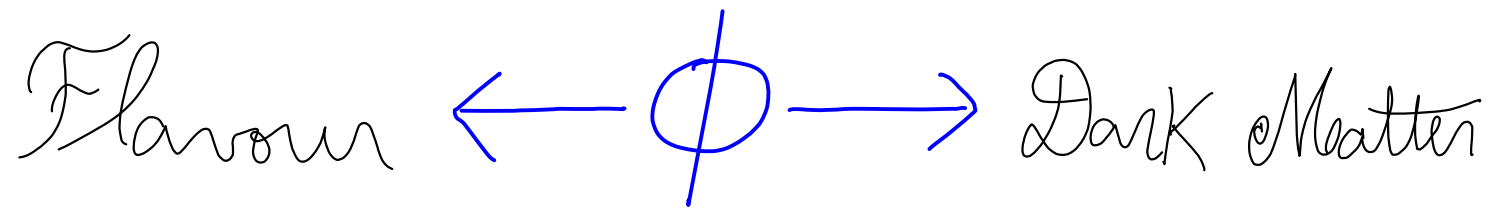
$$\mathcal{L}_\nu \supset -y_\phi \phi_\nu [\nu^c \nu^c]_s - y_H \tilde{H} [L \nu^c]_s$$

$$\mathcal{L}_{\phi_\nu \chi \chi} = y_\chi [\phi_\nu \chi] \chi^c = y_\chi \phi_{\nu_1} \chi_1 \chi^c + y_\chi \phi_{\nu_2} \chi_3 \chi^c + y_\chi \phi_{\nu_3} \chi_2 \chi^c.$$



Conclusions

Interesting connections between



Thanks

Extra stuff

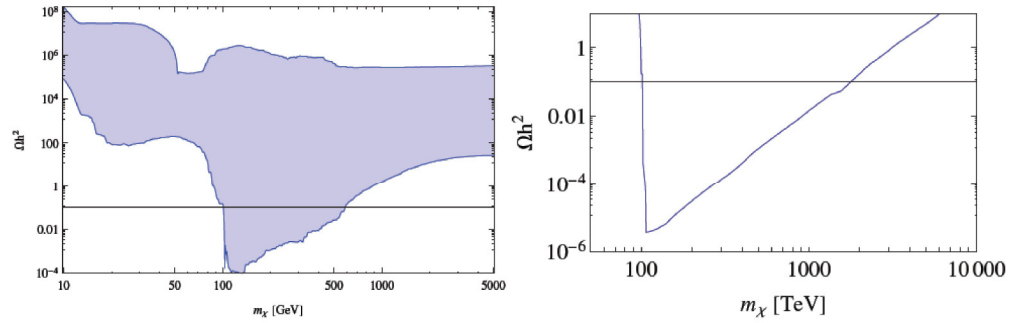


Figure 2: *Left*: Overview of the produced relic density. The model parameters were marginalised within the numerical domains defined in eq. (10). *Right*: Minimal relic density, imposing the parameters $y_{\chi_i} = c_{\phi H} = 1$ and the relation $m_\chi \simeq 0.5 m_{\phi_0}$ for resonant s-channel annihilation. Furthermore, $m_\chi := m_{\chi_1}$ and $m_{\chi_{2,3}} = 10$ TeV. The resulting relic density yields the maximum value for m_χ , such that the observation can be matched.

(10)

$$0.01 \leq y_{\chi_1} = y_{\chi_2} = y_{\chi_3}, c_{\phi H} \leq 2$$

$$10 \text{ GeV} \leq m_{\chi_1}, m_{\chi_2}, m_{\chi_3} \leq 10 \text{ TeV}$$

$$100 \text{ GeV} \leq m_{\phi_{2,3}} \leq 1 \text{ TeV}$$

$$m_{\phi_1} = \sqrt{2} m_{\phi_{2,3}}$$

$$u = \Lambda = 10 \text{ TeV}$$

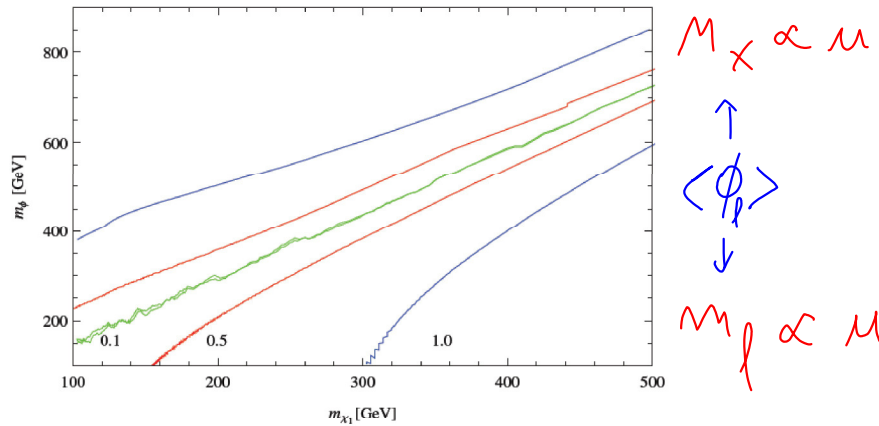


Figure 3: Relation between familion and DM masses from the observed relic density, for the familion fields with fixed mass ratios: m_ϕ is the mass of $\phi_{2,3}$ and $m_{\phi_1} = \sqrt{2} m_\phi$. Fixed $u = \Lambda = 1000$ GeV and $m_{\chi_{2,3}} = 10 \times m_{\chi_1}$. The numbers in the plot refer to $y_{\chi_i} = c_{\phi H} = 1.0, 0.5, 0.1$.

(19)

$$\begin{aligned}
 &10 \text{ GeV} \leq m_\chi \leq 10 \text{ TeV} \\
 &100 \text{ GeV} \leq m_{\phi_\nu^{\text{light}}} \leq 1 \text{ TeV} \\
 &0.01 \leq y_\chi, y_{\phi\nu}, c_{\phi H} \leq 2 \\
 &m_N = 100 \text{ GeV}, m_{\phi_\nu^{\text{heavy}}} = 10 \text{ TeV}
 \end{aligned}$$

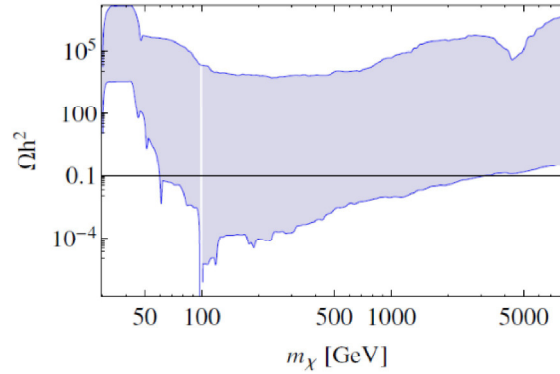


Figure 4: Overview of the produced relic density with the non-Abelian familon portal given by ϕ_ν . The model parameters were marginalised within the numerical domains defined in (19).

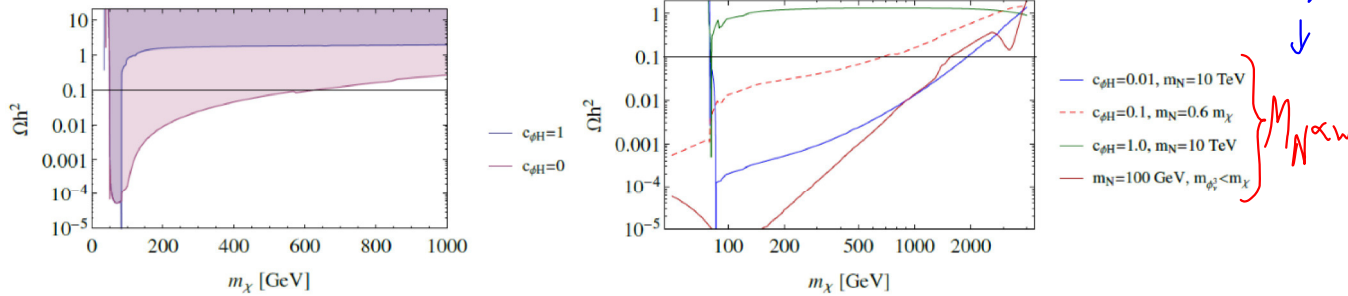


Figure 5: *Left*: Red line: $c_{\phi H} = 1$, Blue line: $c_{\phi H} = 0.01$. All Yukawa couplings equal one, $m_N = 100 \text{ GeV}$. *Right*: The blue line is the lower limit on the abundance. It is given by resonant s-channel production of two heavy neutrinos (being lighter than the DM). Relevant parameters controlling the cross section are the respective Yukawa couplings. The two other colored lines are the same, just with $c_{\phi H} = 0.01, 0.1$, respectively. In this case, the scalar parameters are dominating in importance over the neutrino ones.