

Synergy of collider and gravitational waves to explore the Higgs sector

Shinya KANEMURA



Multi Higgs Models 2018, Sep 2-7, 2018, Lisbon

Higgs as a Probe of New Physics 2019

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“Higgs as a Probe of New Physics”

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URL : <http://www3.u-toyama.ac.jp/theory/HPNP2019/>



Introduction

Although a Higgs boson was found at LHC, the origin of EWSB remains mystery. Unlike the gauge sector, the Higgs sector is not uniquely determined from the theory.

(Dirty! Expecting a beautiful principle for EWSB behind)

There can still be many possibilities for non-minimal Higgs sectors. Phenomena beyond the SM may be related to such an extended Higgs sector

At LHC, measured production and decay of the Higgs boson are consistent with the SM predictions. SM is a good description of nature below 100 GeV.

Introduction

SM is enough?

Of course **not**. There are many reasons to consider BSM.

- Hierarchy, Nature of Higgs, Strong CP, GUT, Gravity, ...
- Dark matter, Baryogenesis, Neutrino mass, Inflation, ...

The SM Higgs sector causes the hierarchy problem. Paradigms such as SUSY have been proposed, but new particles such as SUSY particles have not been discovered yet. ...

New physics must exist. But we do not know at which scale it appears. **How we can approach to new physics?**

Higgs sector is Key

In addition to direct searches of new particles at LHC,
we can measure Higgs couplings precisely at a Higgs factory

Precision of the measured Higgs couplings

$hVV^*, hff, hgg, h\gamma\gamma, hZ\gamma$

10-20 % (Run 2) $\rightarrow$ several % (HL-LHC)

sub % (ILC250)

Higgs potential (remains untested)

hhh $\rightarrow$ O(100)% (HL-LHC)

$\rightarrow$ impossible (ILC250)

$\rightarrow$ O(10) % (ILC1TeV)

Instead of hhh coupling, we may use gravitational waves (GWs)

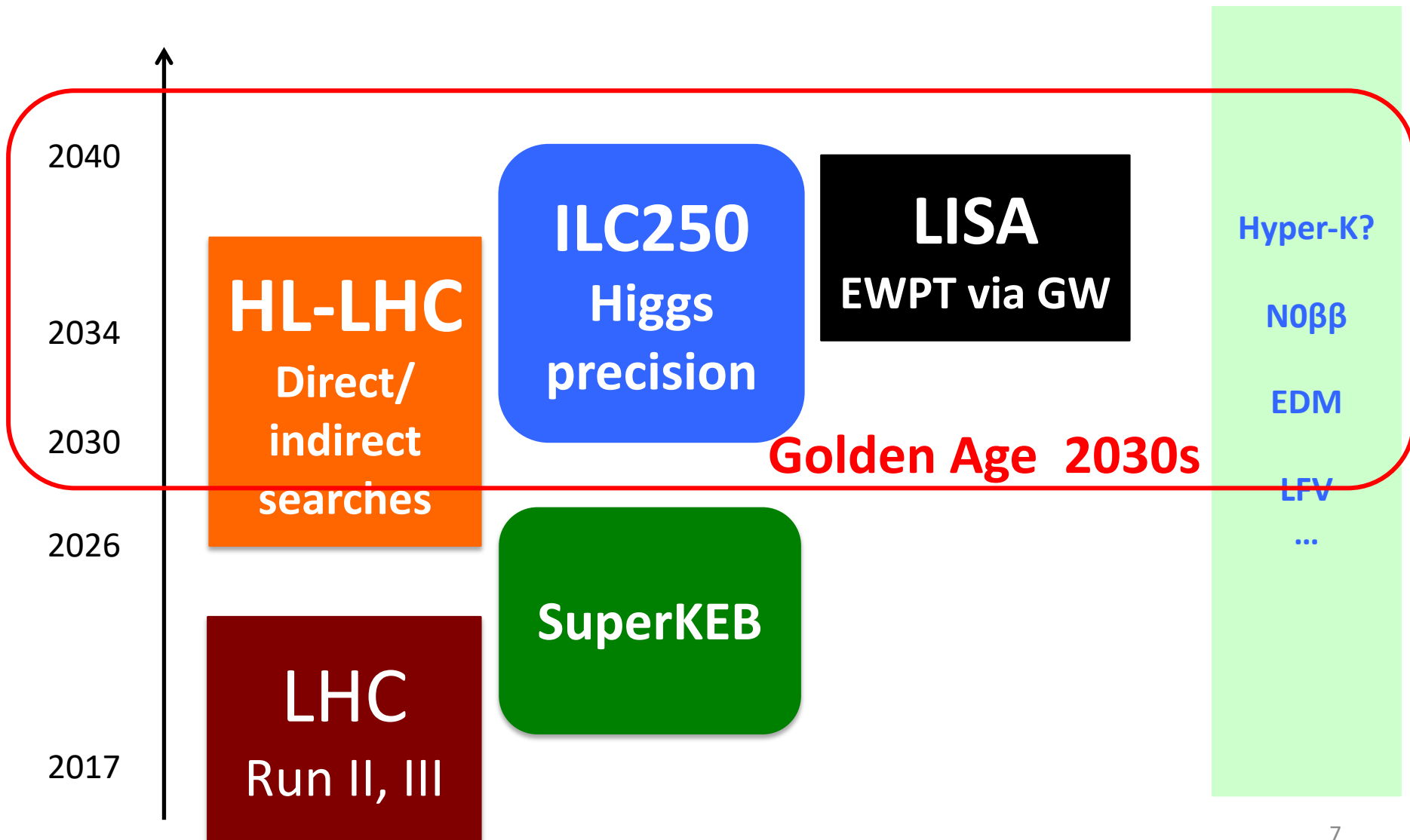
EW phase transition via GW (LISA/DECIGO/BBO)

Main Points

Slide by
Hitoshi Yamamoto
for the status of ILC

- ILC has been designed to lead the new era of particle physics opened up by the discovery of Higgs.
- ILC250 Higgs Factory reduces the cost by up to 40%.
- For precision Higgs measurements, ILC ~ several tens of HL-LHC running simultaneously.
- New particles: at LHC, ~1 million Higgs were produced and then discovered. At ILC, a handful will do.
- Japanese government is about to finish evaluating the case for ILC (ILC 250 Higgs Factory).
- The deadline for inputs to the European Strategy Discussion is the end of this year – important that a positive statement comes from Japanese government in that time scale.

Future experiments



Contents

Introduction (done)

**Fingerprinting of extended Higgs sectors
by precision measurements**

Higgs potential (GW from EW phase transition)

**Physics case of probing a model using the synergy of
HL-LHC, ILC250 and LISA in 2030s**

Summary

Extended Higgs sectors

Multiplet Structure (with additional scalars)

Φ_{SM} +Isospin **Singlet**,
 Φ_{SM} +**Doublet** (2HDM),
 Φ_{SM} +**Triplet**, ...

Additional Symmetry

Discrete or Continuous?
Exact or Softly broken?

Interaction

Weakly coupled or Strongly Coupled?

Hint for
BSM
models

Era of Precision Measurement again

Direct search at LHC

reach 1-2TeV → 3 TeV (HL-LHC)

at most a factor improvement

Indirect test

10-30% → 1% (ILC, other Higgs factories)

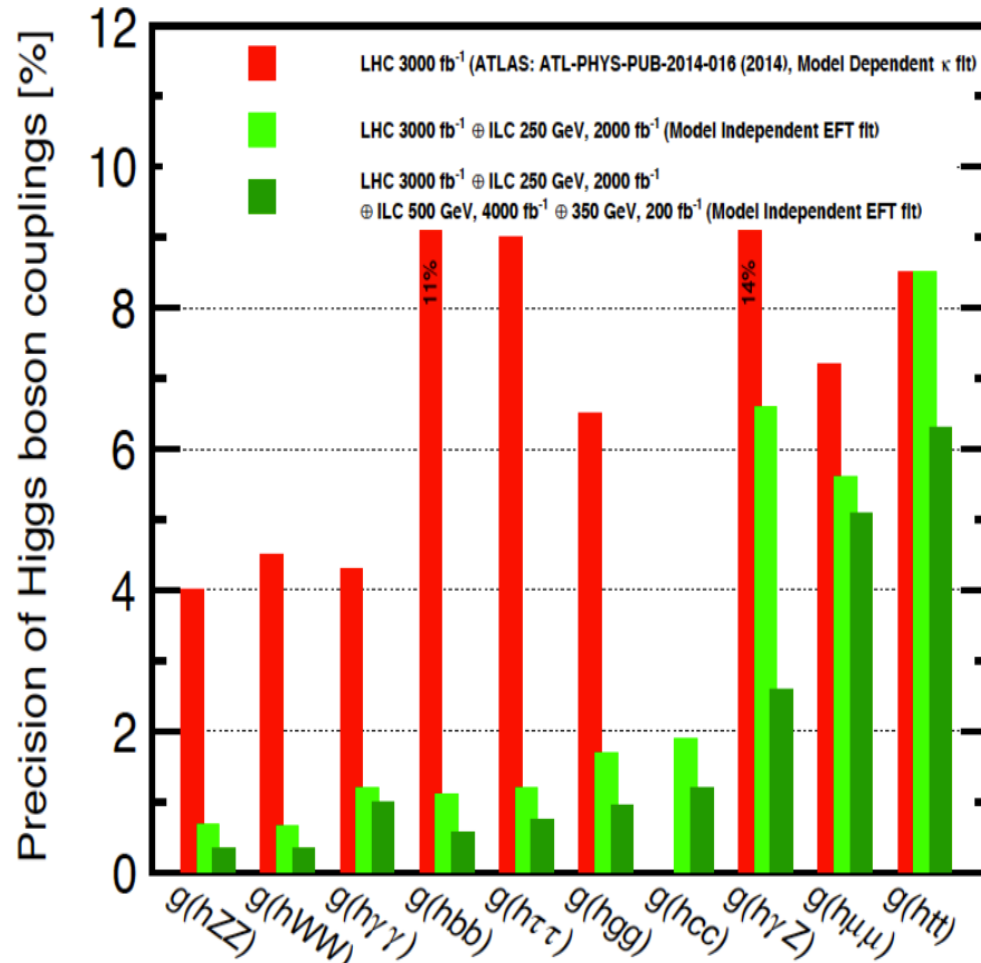
at least 1 order improvements

Higgs factory: lepton collider [ILC, CEPC, FCCee, CLIC]

With such future precision studies, we try to find deviation from SM.
Once detected, we can determine the Higgs sector
and get information for direction of new physics

Higgs Precision at HL-LHC, ILC250, ...

[K. Fujii, et al., arXiv:1710.07621]



Deviation = New Physics Scale

Scaling factor κ_i : factor of deviation from the SM value

Coupling of $h(125)$ and weak bosons

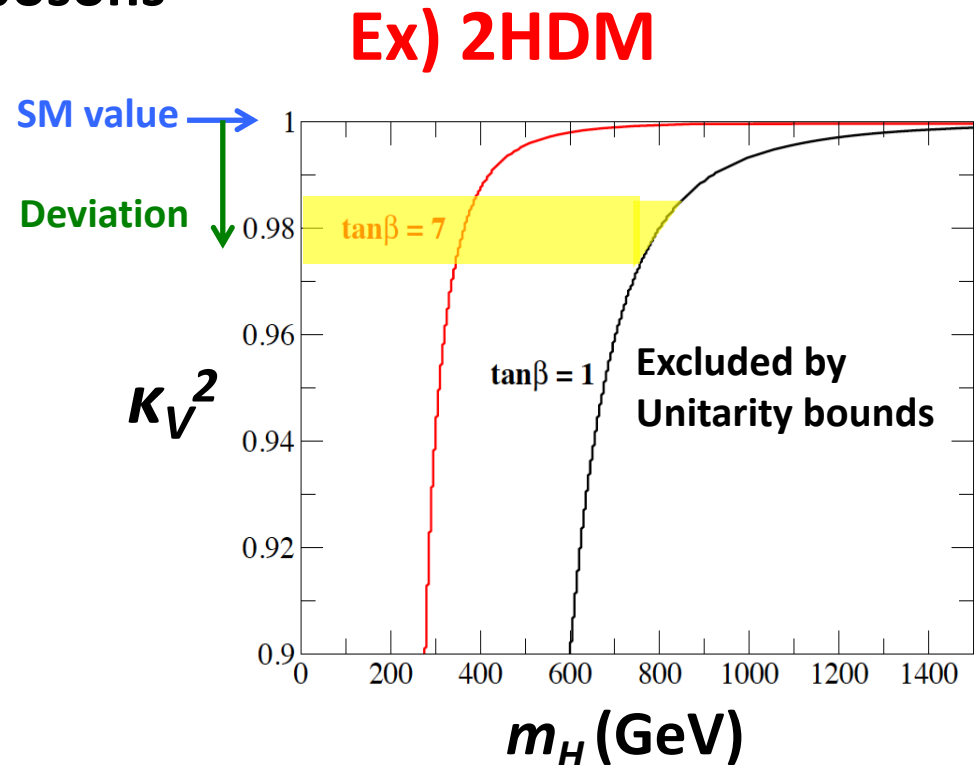
$V (=W, Z)$ hVV

$$\kappa_V^2 = \sin^2(\beta - \alpha)$$

If a **2%** deviation in κ_V^2



The second Higgs **H** must be lighter than **800 GeV**



Precision test has the similar power to the direct search

Patterns of deviations

	Gauge couplings		Yukawa couplings		
	hVV	$h\tau\tau$	hbb	hcc	$\cos(\beta-\alpha) < 0$
	K_V	K_τ	K_b	K_c	
Type-I	↓	↓	↓	↓	
Type-II	↓	↑	↑	↓	Direction of deviation in each coupling
Type-X	↓	↑	↓	↓	
Type-Y	↓	↓	↑	↓	

We can fingerprint extended Higgs models from the pattern of deviation in Higgs couplings

Fingerprinting the model

$$\kappa_V \equiv \frac{g_{hVV}(2HDM)}{g_{hVV}(SM)} = \sin(\beta - \alpha)$$

$x = \cos(\beta - \alpha)$ **SM-like: $|x| \ll 1$**

$$\kappa_V = 1 - (1/2) x^2 + \dots$$

When a **Fermion** couples to Φ_1

$$K_f = 1 + \cot\beta x + \dots$$

and if it couples to Φ_2

$$K_f = 1 - \tan\beta x + \dots$$

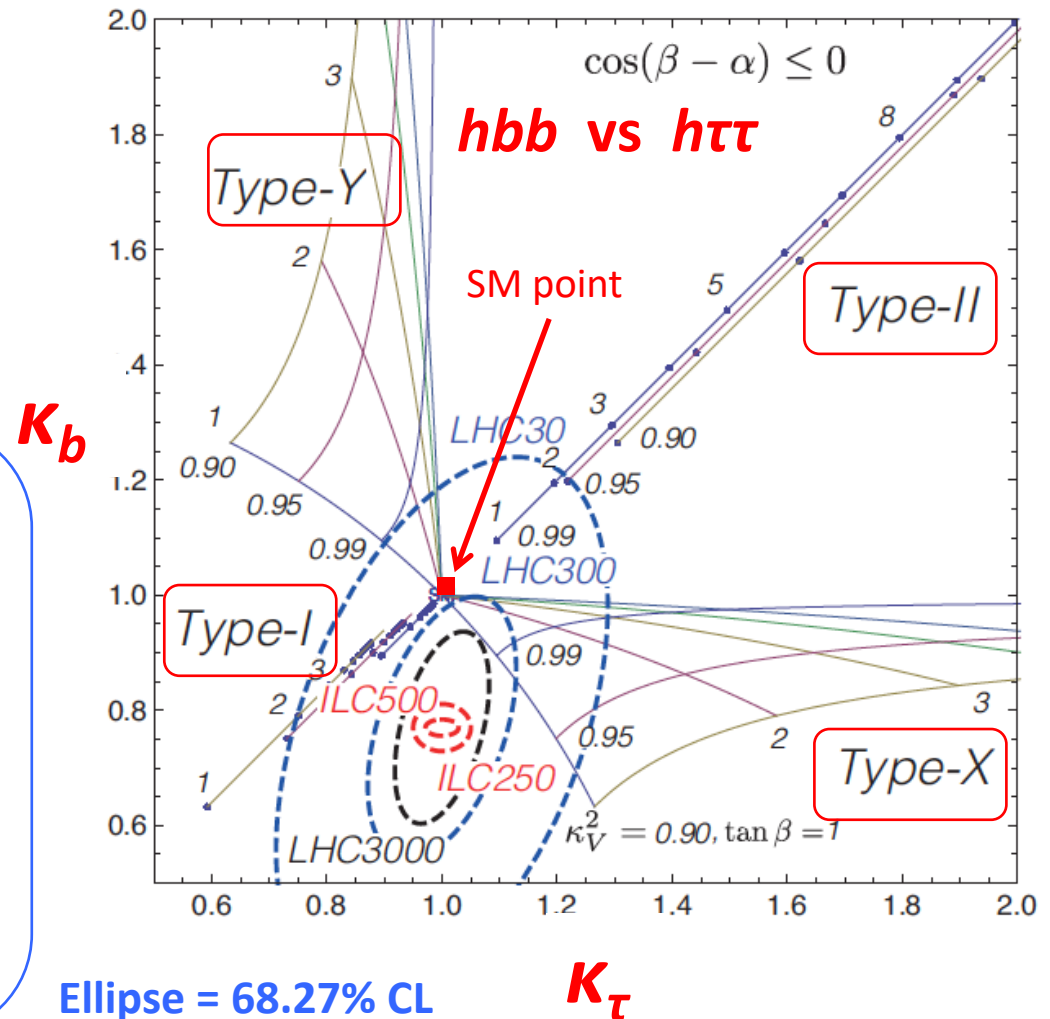
If deviation in κ_V^2 can be large enough to be detected at future collider



4-models can be separated by looking at deviations in Yukawa couplings K_τ, K_b, K_c ,

...

SK, K. Tsumura, K. Yagyu, H. Yokoya, 2014

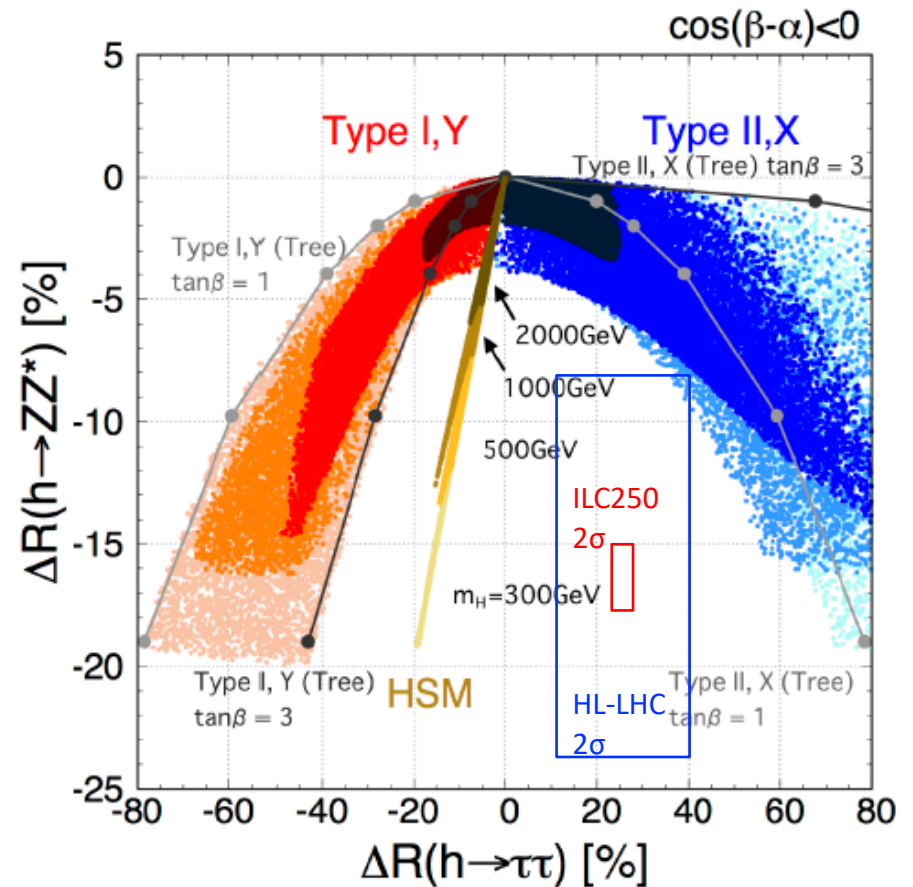
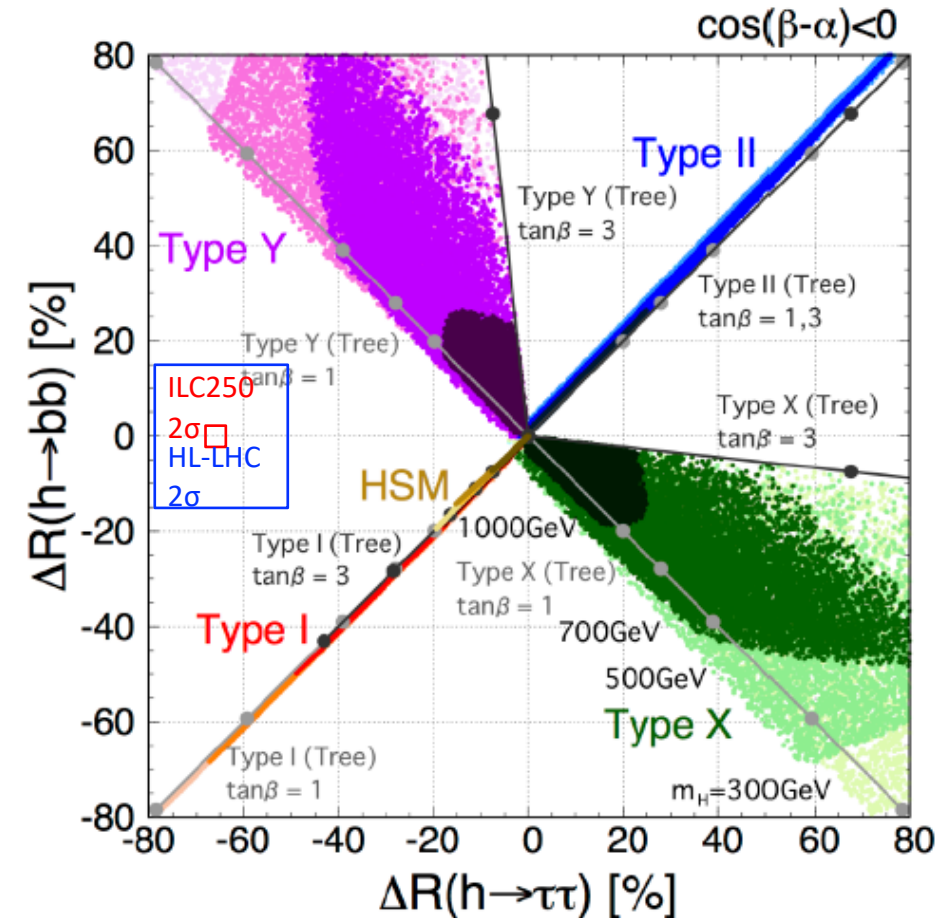


$$\Delta R(h \rightarrow XX) = \frac{\Gamma_{\text{NP}}(h \rightarrow XX)}{\Gamma_{\text{SM}}(h \rightarrow XX)} - 1$$

H-COUP Project

SK, Kikuchi, Mawatari, Sakurai, Yagyu 2018

See also Sakurai's talk.



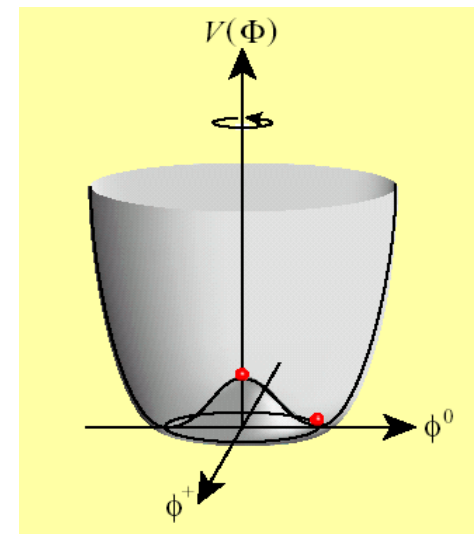
Full set of 1-loop corrections (EW + QCD + Higgs) to the decay rates in various Higgs sectors and future precision measurements at ILC250 make us possible to fingerprint models and also to get information of inner parameters such as mass of the second Higgs boson

Higgs potential

Most important part for the EW symmetry breaking
(Yet to be tested)

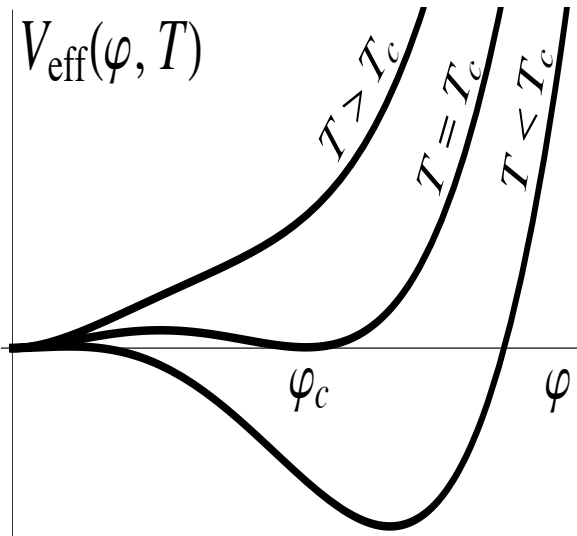
$$V(\Phi) = +\mu^2|\Phi|^2 + \lambda|\Phi|^4$$

- **Physics behind EWSB**
 - Where come from $\mu^2 < 0$
 - What is the origin of λ
 - Dynamics, nature
- **Electroweak Phase Transition**
 - Aspect of Transition, 1st order or not?
 - Mechanism of Phase Transition
 - Relation to EW baryogenesis



Electroweak Baryogenesis

1st OPT is required



Sakharov 3rd condition

Departure from Thermal Equilibrium

Sphaleron Decoupling

$$\Gamma_{\text{sph}} < H(T_c)$$

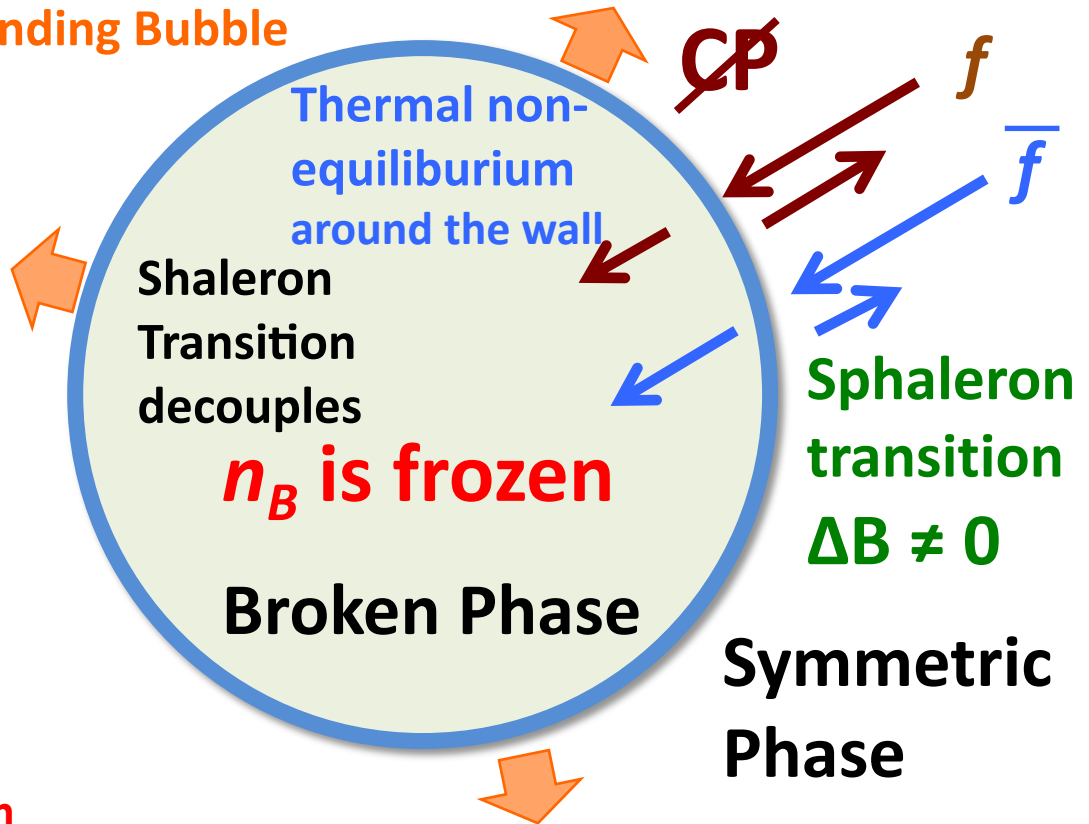
$$\begin{aligned} \Gamma_{\text{sph}} &\sim e^{-E_{\text{sph}}/T_c} \\ &\sim e^{-\alpha' \varphi_c/T_c} \end{aligned}$$



$$\frac{\varphi_c}{T_c} \gtrsim 1$$

Physics of the Higgs potential

Expanding Bubble



1st OPT possible in extended Higgs

Potential at finite
temperatures (HTE)

$$V_{\text{eff}}(\varphi, T) \simeq D(T^2 - T_0^2)\varphi^2 - ET\varphi^3 + \frac{\lambda_T}{4}\varphi^4 + \dots$$

SM 1st OPT not realized

$$\frac{\varphi_C}{T_C} = \frac{2E}{\lambda_T} = \frac{6m_W^3 + 3m_Z^3 + \dots}{3\pi v m_h^2} \ll 1$$

1st OPT possible in extended Higgs

Potential at finite temperatures (HTE)

$$V_{\text{eff}}(\varphi, T) \simeq D(T^2 - T_0^2)\varphi^2 - ET\varphi^3 + \frac{\lambda_T}{4}\varphi^4 + \dots$$

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Extended Higgs: Strongly 1st OPT possible **Quantum effect of additional Scalar field Φ ($= H, A, H^+, \dots$)**

Realized by Quantum Effect by Φ ($= H, A, H^+, \dots$)

$$\frac{\varphi_C}{T_C} \simeq \frac{1}{3\pi v m_h^2} \left\{ 6m_W^3 + 3m_Z^3 + \sum_{\Phi} m_{\Phi}^3 \left(1 - \frac{M^2}{m_{\Phi}^2} \right)^3 \left(1 + \frac{3M^2}{2m_{\Phi}^2} \right) \right\} > \mathbf{1}$$

1st OPT possible in extended Higgs

Potential at finite temperatures (HTE)

$$V_{\text{eff}}(\varphi, T) \simeq D(T^2 - T_0^2)\varphi^2 - ET\varphi^3 + \frac{\lambda_T}{4}\varphi^4 + \dots$$

SM 1st OPT not realized

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Extended Higgs: Strongly 1st OPT possible Quantum effect of additional Scalar field Φ ($= H, A, H^+, \dots$)

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Prediction: a large deviation on the hhh coupling

$$\lambda_{hhh} \simeq \frac{3m_h^2}{v^2} \left\{ 1 - \frac{m_t^4}{\pi^2 v^2 m_h^2} + \sum_{\Phi} \frac{m_{\Phi}^4}{12\pi^2 v^2 m_h^2} \left(1 - \frac{M^2}{m_{\Phi}^2}\right)^3 \right\} > \lambda_{hhh}^{\text{SM}}$$

1st OPT and the hhh coupling

Strong 1st OPT ($\Phi_c/T_c > 1$)
 $\Leftrightarrow$ Deviation in the hhh coupling

EW Baryogenesis can be tested
by detecting a large deviation
in the hhh coupling

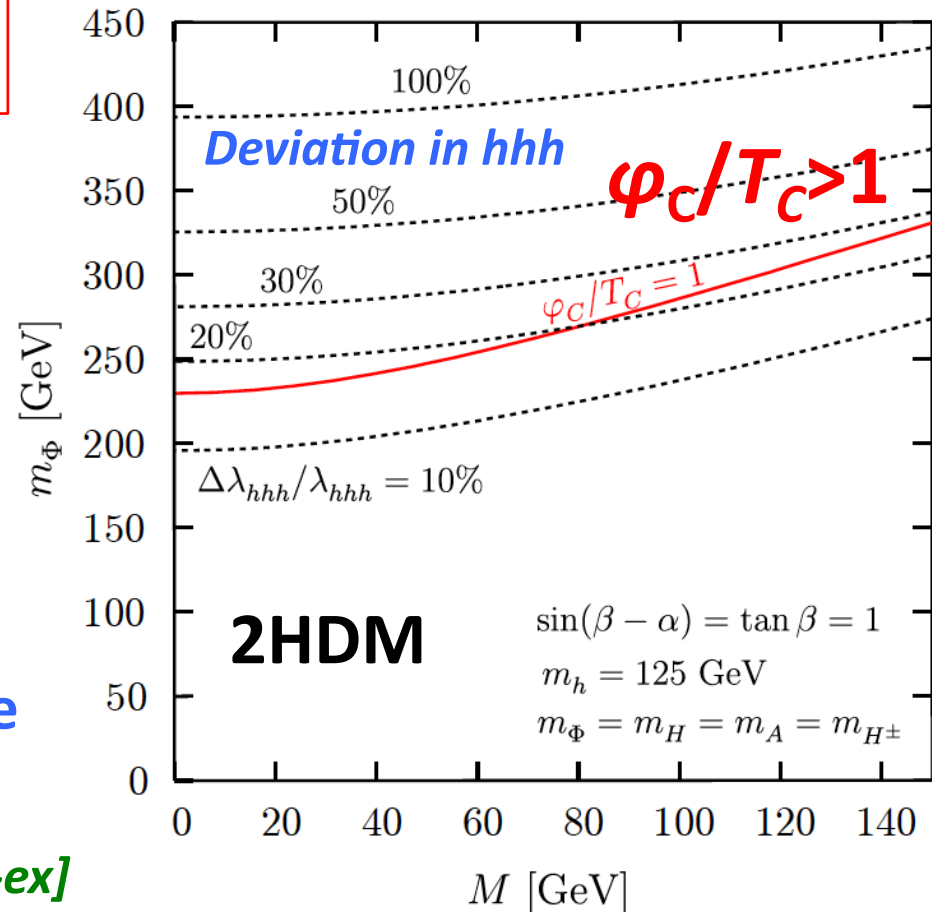
Which collider?

(HL-)LHC cannot do it

ILC(1 TeV) [and CLIC] can measure
it by O(10) %

K.Fujii et al., arXiv:1506.05992 [hep-ex]

S.K., Y. Okada, E. Senaha (2005)

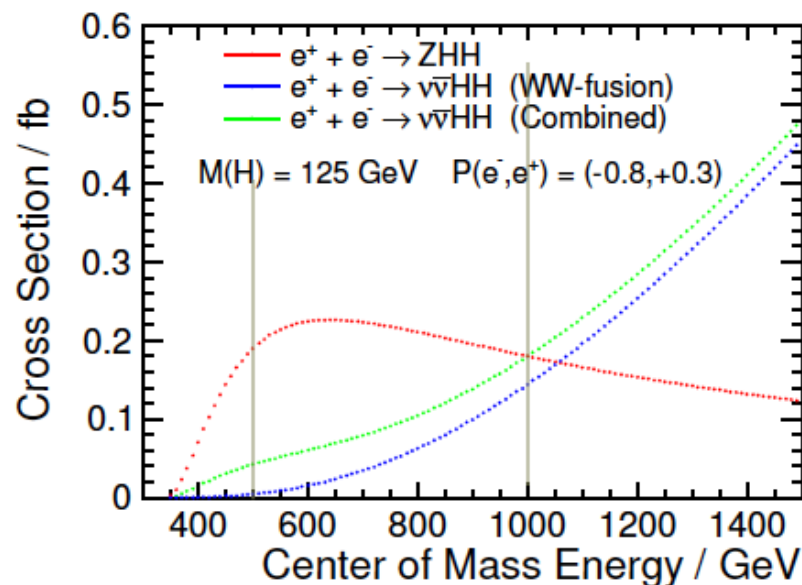
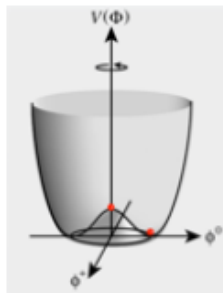
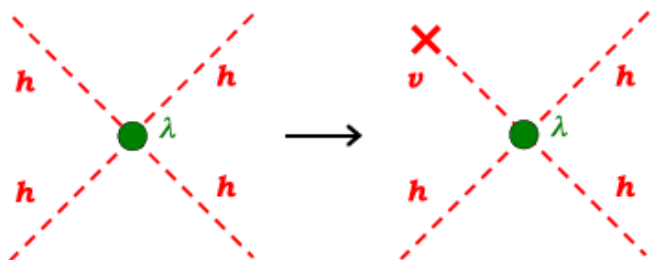


Clearly, ILC250 is not useful for this purpose

Higgs Self-Coupling

Slide by Keisuke Fujii

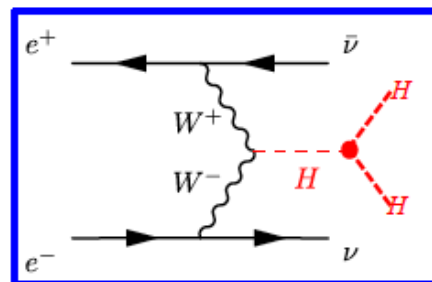
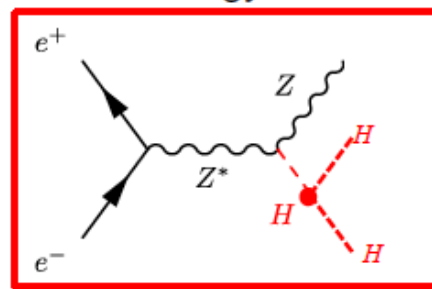
hhh coupling =
consequence of vacuum condensation



Challenging measurement because of:

- Small cross section (Zhh 0.2 fb at 500 GeV)
- Many jets in the final state
- **Presence of irreducible BG diagrams**

arXiv:1310.0763	ILC500	ILC500-up	ILC1000	ILC1000-up
$\sqrt{s}$ (GeV)	500	500	500/1000	500/1000
$\int \mathcal{L} dt$ (fb ⁻¹)	500	1600 [‡]	500+1000	1600+2500 [‡]
$P(e^-, e^+)$	(-0.8, 0.3)	(-0.8, 0.3)	(-0.8, 0.3/0.2)	(-0.8, 0.3/0.2)
$\sigma(ZHH)$	42.7%		42.7%	23.7%
$\sigma(\nu\bar{\nu}HH)$	—	—	26.3%	16.7%
λ	83%	46%	21%	13%



Ongoing analysis improvements **towards $O(10)\%$ measurement**

See J.Tian's Poster

Alternative tool to explore EWPT

At HL-LHC, ILC250, FCCee, ...

the hhh coupling cannot be measured efficiently

We cannot test the Higgs potential in the near future?

Fortunately,

Gravitational Waves can be a new tool to explore physics
at the early Universe

(Inflation, EW phase transition, Topological defects ...)

Higgs potential via GWs

In 2016, LIGO reported the first direct observation of GWs from merge of a BH Binary (~ 100 Hz) $\rightarrow$ **Era of GW astronomy started**
Ground based experiments
aLIGO, KAGRA, aVirgo...

GW Physics

GW from 1st OPT: **homogeneous, isotropic, stationary, unpolarized**
Relic GWs are characterized only by frequency

Transition temperature gives typical frequencies

$T_t = 100\text{GeV} \rightarrow f = 10^{-1} - 10^{-3} \text{ Hz}$ **Out of sensitivity**
at LIGO/KAGRA ($10-10^3\text{Hz}$)

Future **space based** GW experiments

LISA Sensitivity around 10^{-3} (mili) Hz (will start in 2034)

DECIGO Sensitivity around 10^{-1} (deci) Hz

We can explore GWs from the early Universe! *Grojean, Survant, ...*

GWs from 1st OPT

Bubble Collisions

“Turbulences in the plasma”

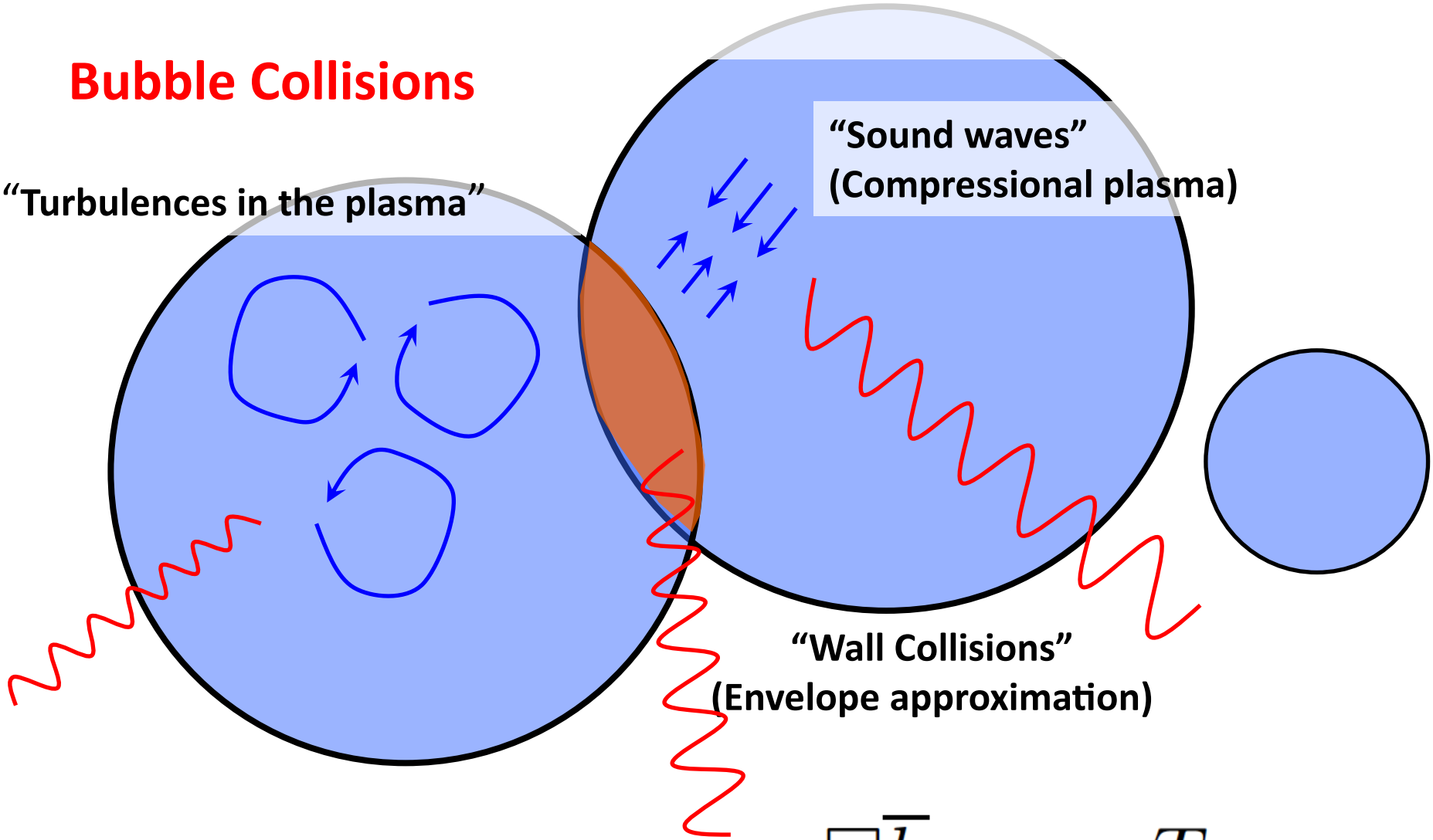
“Sound waves”
(Compressional plasma)

“Wall Collisions”
(Envelope approximation)

Spherical symmetry is violated
by bubble collisions → GW occurs

$$\square \bar{h}_{\mu\nu} = \kappa \underline{T_{\mu\nu}}$$

Source of GW



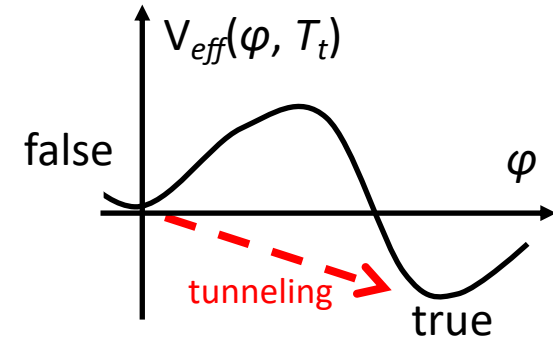
From bubble dynamics to GW spectrum

Bubble Nucleation Rate

$$\Gamma(T) = \Gamma_0 \exp(-S_3/T)$$

With the phase transition condition

$$\Gamma(T)/H^4 = 1 \text{ we can determine}$$



α Latent heat (released energy from the PT)

Depth of the potential

β Inverse of the time variation of 1stOPT

Speed of phase transition

$$\alpha = \frac{\epsilon(T_*)}{\rho_{\text{rad}}(T_*)}$$

$$\beta = - \left. \frac{dS_E}{dt} \right|_{t=t_*} \simeq \frac{1}{\Gamma} \left. \frac{d\Gamma}{dt} \right|_{t=t_*}$$

From these parameters we can calculate GW spectra.

Ex) GW spectrum from Sound Wave (Compressional wave)

$$\tilde{\Omega}_{\text{sw}} h^2 \simeq 2.65 \times 10^{-6} \frac{v_b}{\tilde{\beta}} \left(\frac{\kappa(v_b, \alpha) \alpha}{1 + \alpha} \right)^2 \quad \tilde{f}_{\text{sw}} \simeq 1.9 \times 10^{-5} \text{Hz} \frac{\tilde{\beta}}{v_b}$$

C.Caprini et al., arXiv:1512.06239

Various models for 1st OPT

Thermal loop effect ↓

$$V_{\text{eff}} = D(T^2 - T_0^2)\varphi^2 - (ET - \underline{e})\varphi^3 + \frac{\lambda(T)}{4}\varphi^4$$

Non-thermal effect ↑

- **1st OPT by thermal loop effects**
 - MSSM (excluded)
 - N-Scalar singlets (incl. 2HDM) *Kakizaki, SK, Matsui, 2015*
 - Those with classical scale invariance *Hashino, Kakizaki, SK, Matsui, 2016*
- **1st OPT by non-thermal mixing effects**
 - Doublet-Singlet mixing model *Hashino, Kakizaki, SK, Ko Matsui, 2017*
 - NMSSM (underway)

Ex) Higgs model with N singlet scalars

M. Kakizaki, SK, T. Matsui, Phys. Rev. D92 (2015) no.11,115007

Imposed $O(N)$ for simplicity $S^T = (S_1, \dots, S_N)$

$$V_0 = -\mu^2 |\Phi|^2 + \frac{\mu_S^2}{2} |S|^2 + \frac{\lambda}{2} |\Phi|^4 + \frac{\lambda_S}{4} |S|^4 + \frac{c}{2} |\Phi|^2 |S|^2$$

Mass of scalar fields: $m_S^2 = \mu_S^2 + \frac{c}{2} v^2$

$\varphi_c/T_c > 1$ is satisfied by the nondecoupling effect of the singlet fields (compatible with $m_h=125\text{GeV}$)

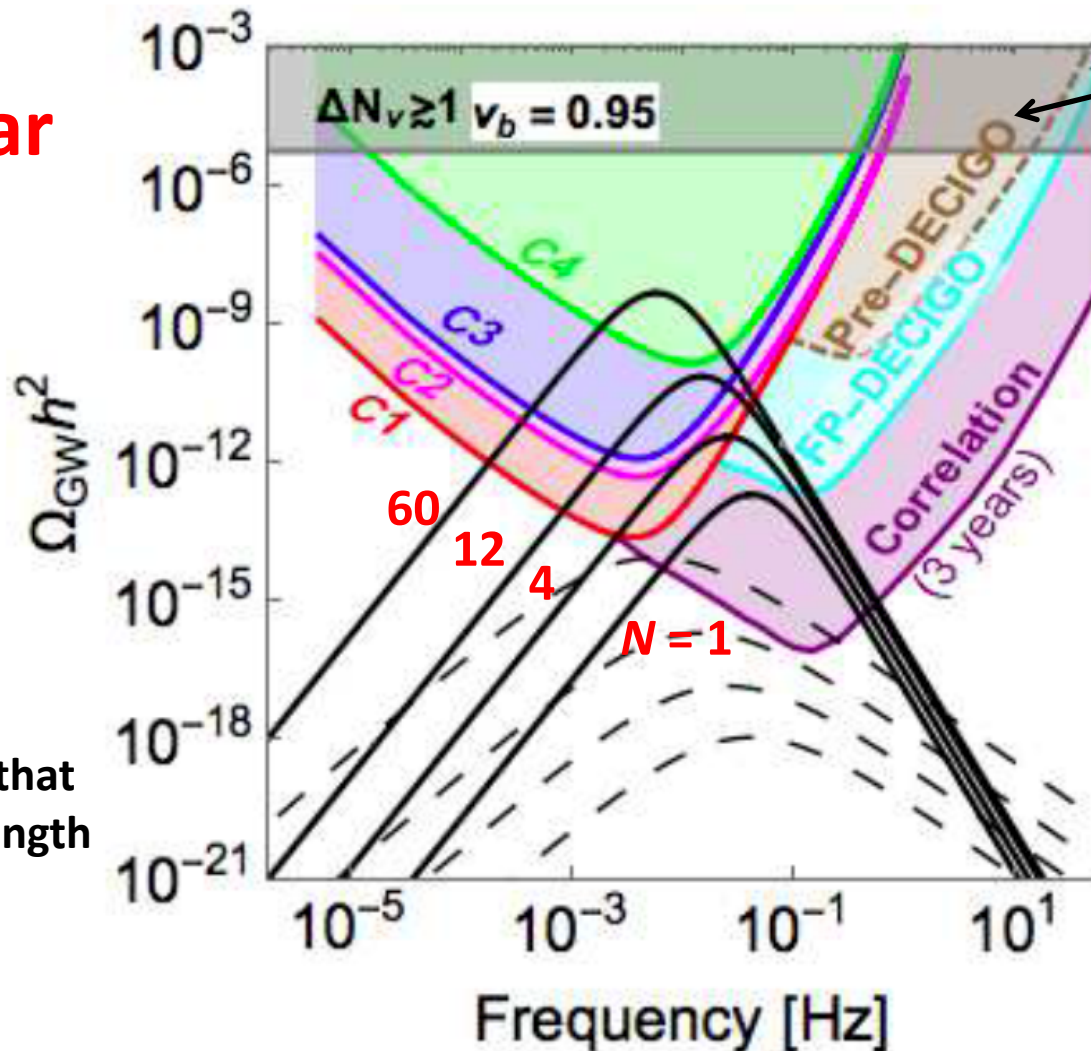
$$\frac{\varphi_C}{T_C} \simeq \frac{1}{3\pi v m_h^2} \left\{ 6m_W^3 + 3m_Z^3 + \underbrace{N m_S^3 \left(1 - \frac{\mu_S^2}{m_S^2}\right)^3 \left(1 + \frac{3\mu_S^2}{2m_S^2}\right)} \right\} > 1$$

$$\lambda_{hhh}^{O(N)} \simeq \frac{3m_h^2}{v^2} \left\{ 1 - \frac{m_t^4}{\pi^2 v^2 m_h^2} + \underbrace{N \frac{m_S^4}{12\pi^2 v^2 m_h^2} \left(1 - \frac{\mu_S^2}{m_S^2}\right)^3} \right\} > \lambda_{hhh}^{\text{SM}}$$

GW spectrum from 1st OPT

**N scalar
model**

Mass m_s is
chosen such that
the peak strength
is maximal



Bound from
Non-observation of energy
density of extra radiation

— sw
... env
- - $turb$

Sensitivities

eLISA

arXiv:1512.06239

DECIGO

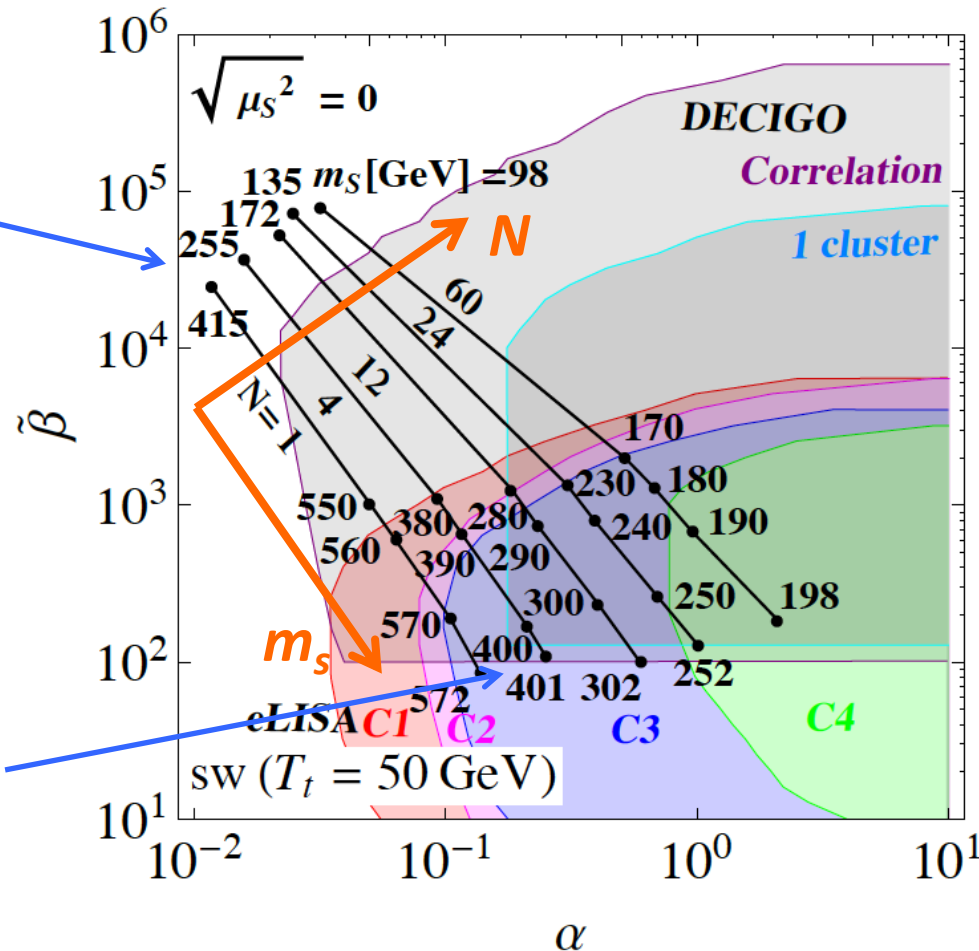
Class. Quant. Grav.
28, 094011 (2011)

(N, m_s) may be determined from GWs

O(N) singlet model with the mass m_s

For smaller m_s
 $\varphi_c/T_c > 1$
 cannot be satisfied

For larger m_s
 $\Gamma/H^4 = 1$ cannot
 be satisfied



Sensitivities

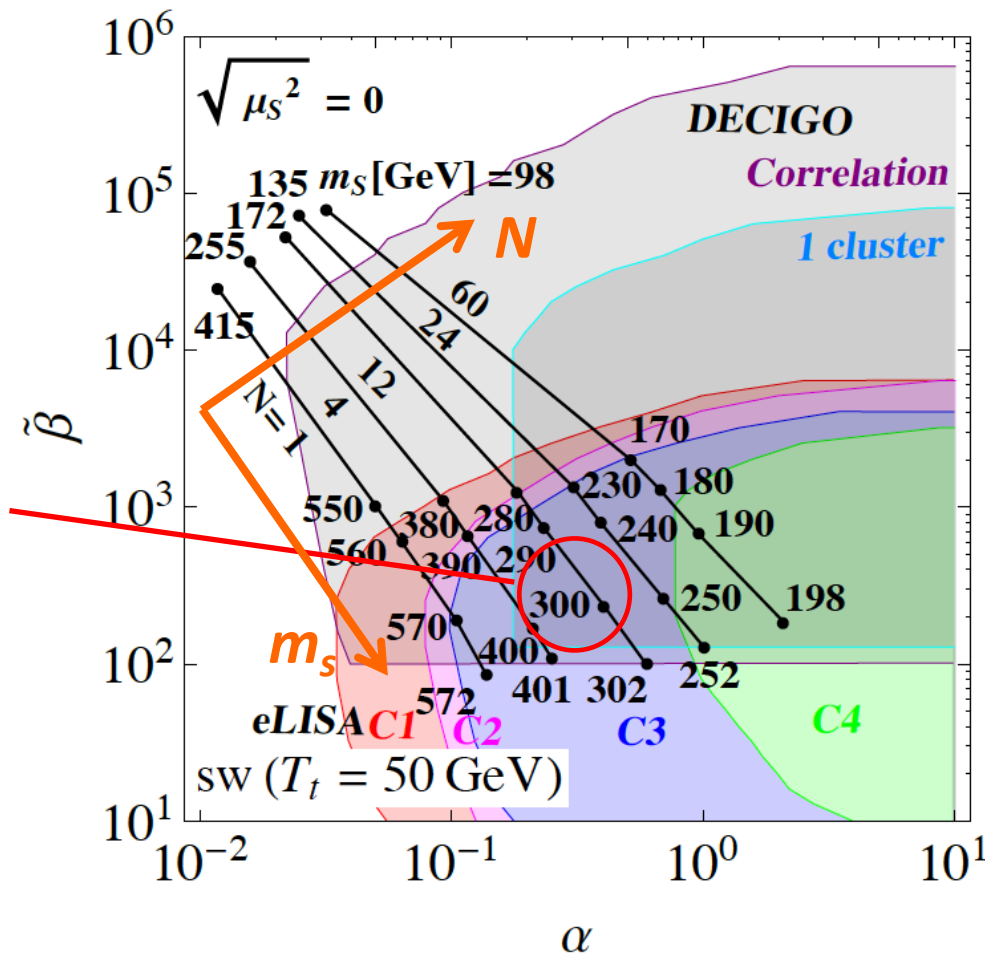
eLISA
 arXiv:1512.06239
 DECIGO,
 Class. Quant. Grav.
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M. Kakizaki, SK, T. Matsui, Phys. Rev. D92 (2015) no.11,115007

(N, m_s) may be determined from GWs

$O(N)$ singlet model with the mass m_s

If α and β are determined with a resolution,
We may be able to fingerprint the model with (N, m_s)



Sensitivities

eLISA
arXiv:1512.06239

DECIGO,
Class. Quant. Grav.
28, 094011 (2011)

M. Kakizaki, SK, T. Matsui, Phys. Rev. D92 (2015) no.11,115007

Fisher Analysis

GW spectrum for
parameter set $\{p\}$

GW spectrum for
fiducial parameter set $\{\hat{p}\}$

Likelihood function

$$\delta\chi^2(\{p\}, \{\hat{p}\}) = 2T_{\text{obs}} \int_0^\infty df \frac{[S_h(f, \{p\}) - S_h(f, \{\hat{p}\})]^2}{[S_{\text{eff}}(f) + S_h(f, \{\hat{p}\})]^2}$$

Observation period

Effective sensitivity of interferometer

↓ Taylor expansion at $\{p\} = \{\hat{p}\}$

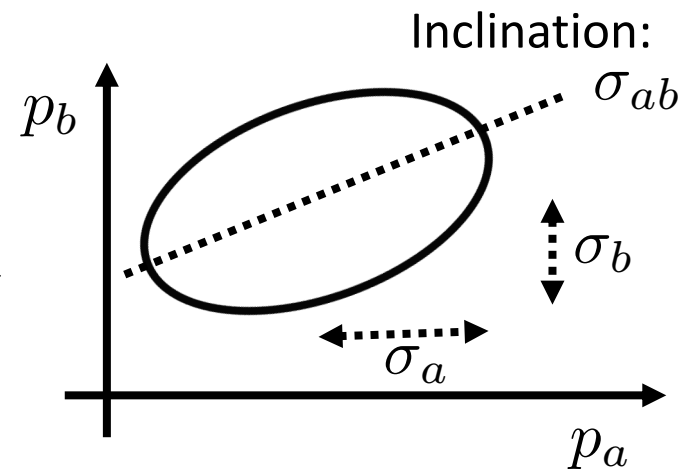
$$\delta\chi^2(\{p\}, \{\hat{p}\}) \simeq \mathcal{F}_{ab}(p_a - \hat{p}_a)(p_b - \hat{p}_b)$$

Fisher information matrix

$$\mathcal{F}_{ab} = 2T_{\text{obs}} \int_0^\infty df \frac{\partial_{p_a} S_h(f, \{\hat{p}\}) \partial_{p_b} S_h(f, \{\hat{p}\})}{[S_{\text{eff}}(f) + S_h(f, \{\hat{p}\})]^2}$$

The inverse $\mathcal{F}_{ab}^{-1}$ is the covariance matrix

Confidence ellipse



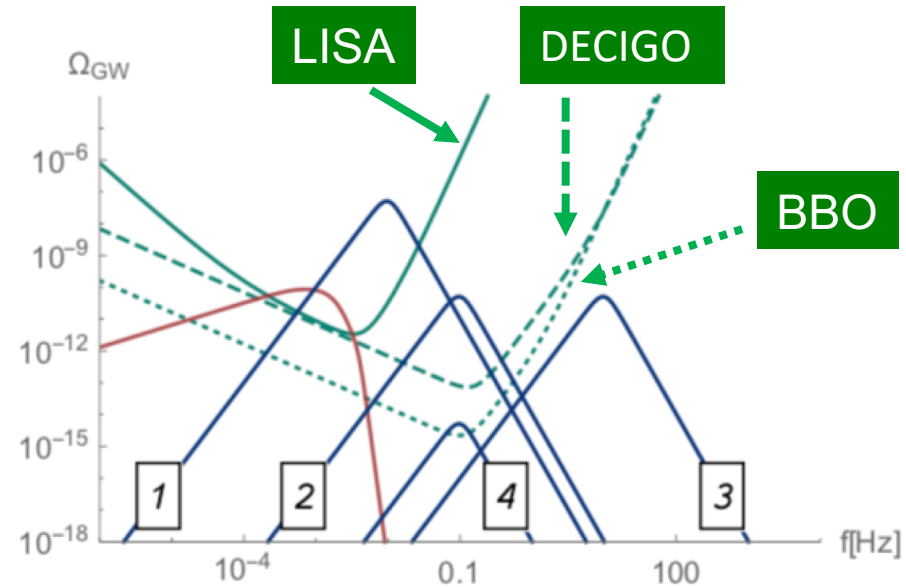
We assume that these expressions are applicable to a single-detector like LISA

Constraints on the shape of spectrum

GW spectrum

Fiducial values

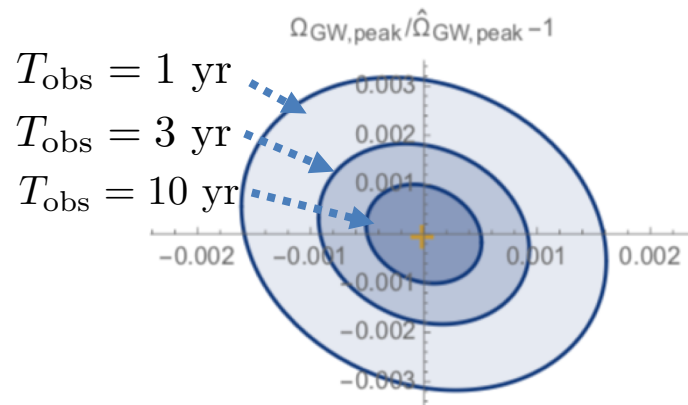
- Point 1: $(f_{\text{peak}}, \Omega_{\text{peak}}) = (10^{-2} \text{ Hz}, 10^{-7})$,
- Point 2: $(f_{\text{peak}}, \Omega_{\text{peak}}) = (10^{-1} \text{ Hz}, 10^{-10})$,
- Point 3: $(f_{\text{peak}}, \Omega_{\text{peak}}) = (10 \text{ Hz}, 10^{-10})$,
- Point 4: $(f_{\text{peak}}, \Omega_{\text{peak}}) = (10^{-1} \text{ Hz}, 10^{-14})$.



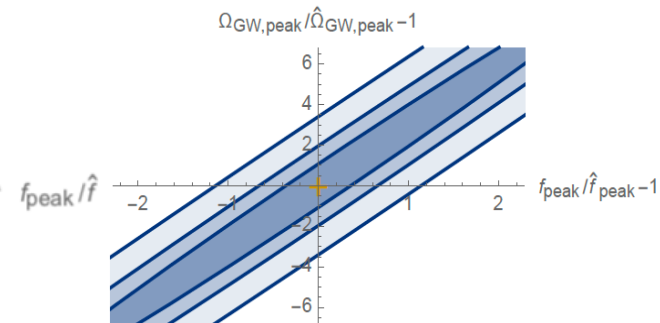
Expected constraints on the GW spectrum

LISA

1 σ confidence ellipse in $(f_{\text{peak}}, \Omega_{\text{peak}})$ for P1 and P2



Point 1



Point 2

A physics case for the synergy of HL-LHC, ILC250 and LISA

Constraints on the model parameters

Case of the singlet-doublet mix model

$$V_{\text{eff}} = D(T^2 - T_0^2)\varphi^2 - \underbrace{(ET - e)}_{\text{Non-thermal effect } \uparrow} \varphi^3 + \frac{\lambda(T)}{4} \varphi^4$$

Thermal loop effect $\downarrow$

Higgs singlet model

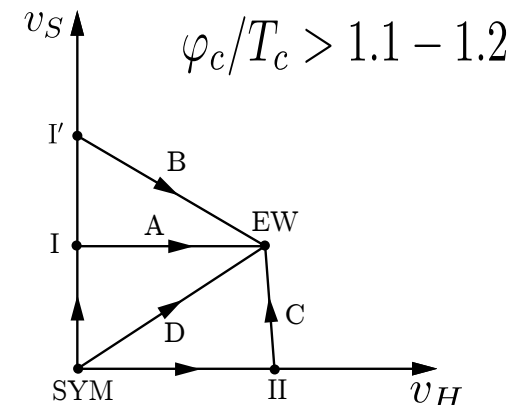
$$V_0 = -\mu_\Phi^2 |\Phi|^2 + \lambda_\Phi |\Phi|^4 + \mu_{\Phi S} |\Phi|^2 S + \frac{\lambda_{\Phi S}}{2} |\Phi|^2 S^2 + \mu_S^3 S + \frac{m_S^2}{2} S^2 + \frac{\mu'_S}{3} S^3 + \frac{\lambda_S}{4} S^4$$

$$\Phi = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}}(v_\Phi + \phi_1 + iG^0) \end{pmatrix}, \quad S = v_S + \phi_2 \quad (\phi_1, \phi_2) \rightarrow (h, H) \text{ with } \theta$$

Multi-field analysis of EWPT is necessary

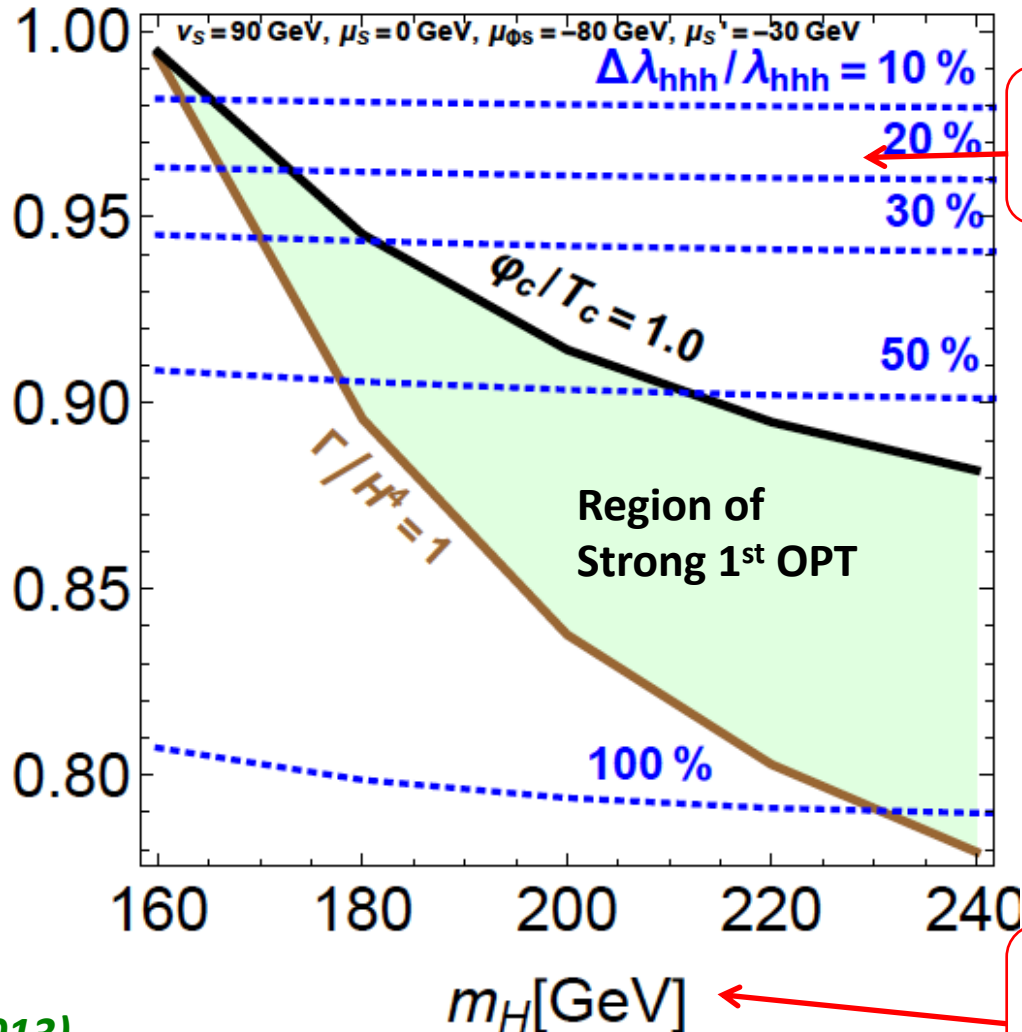
$$(v_\Phi, v_S)$$

Public tool “[CosmoTransition](#)” is used.



$$K = K_V = K_f = \cos\theta$$

Precision measurement at ILC/LHC



Self-coupling hhh measurement at ILC

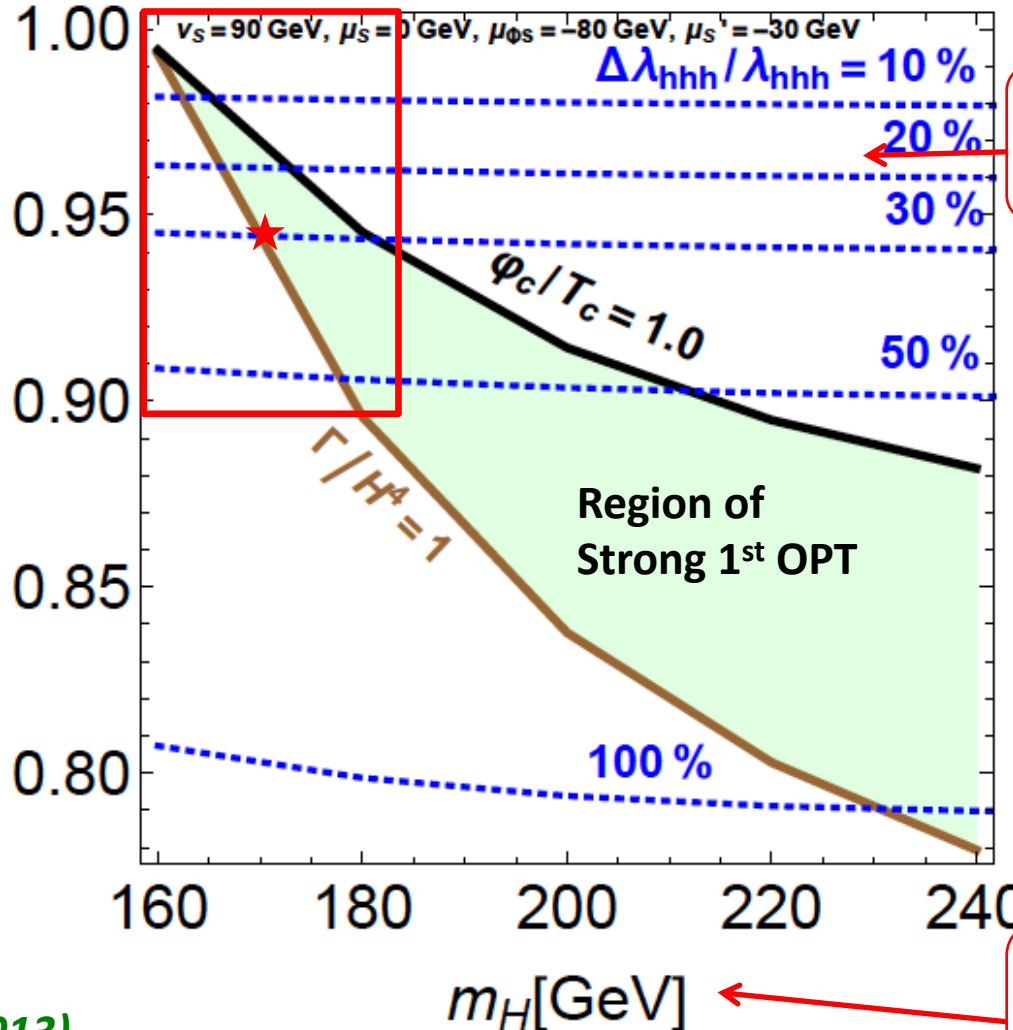
Direct searches of the second Higgs at LHC

Fuyuto, Senaha (2013)

K. Hashino, M. Kakizaki, S.K., T. Matsui, P. Ko, Phys. Lett. B 766, 49 (2017)

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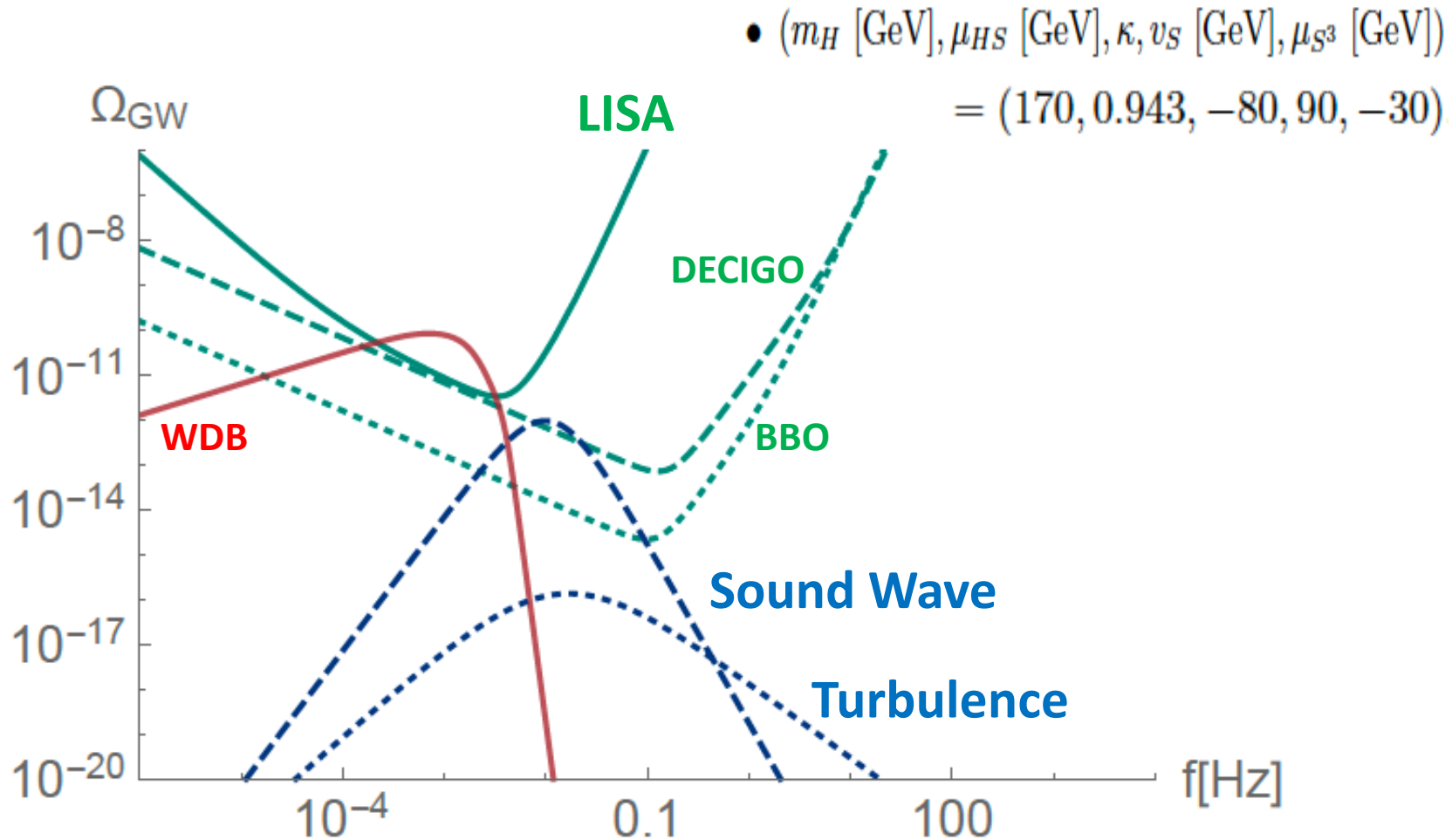
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K. Hashino, M. Kakizaki, S.K., T. Matsui, P. Ko, Phys. Lett. B 766, 49 (2017)

Calculated Spectrum of GW at a fiducial point (DS mixing model)



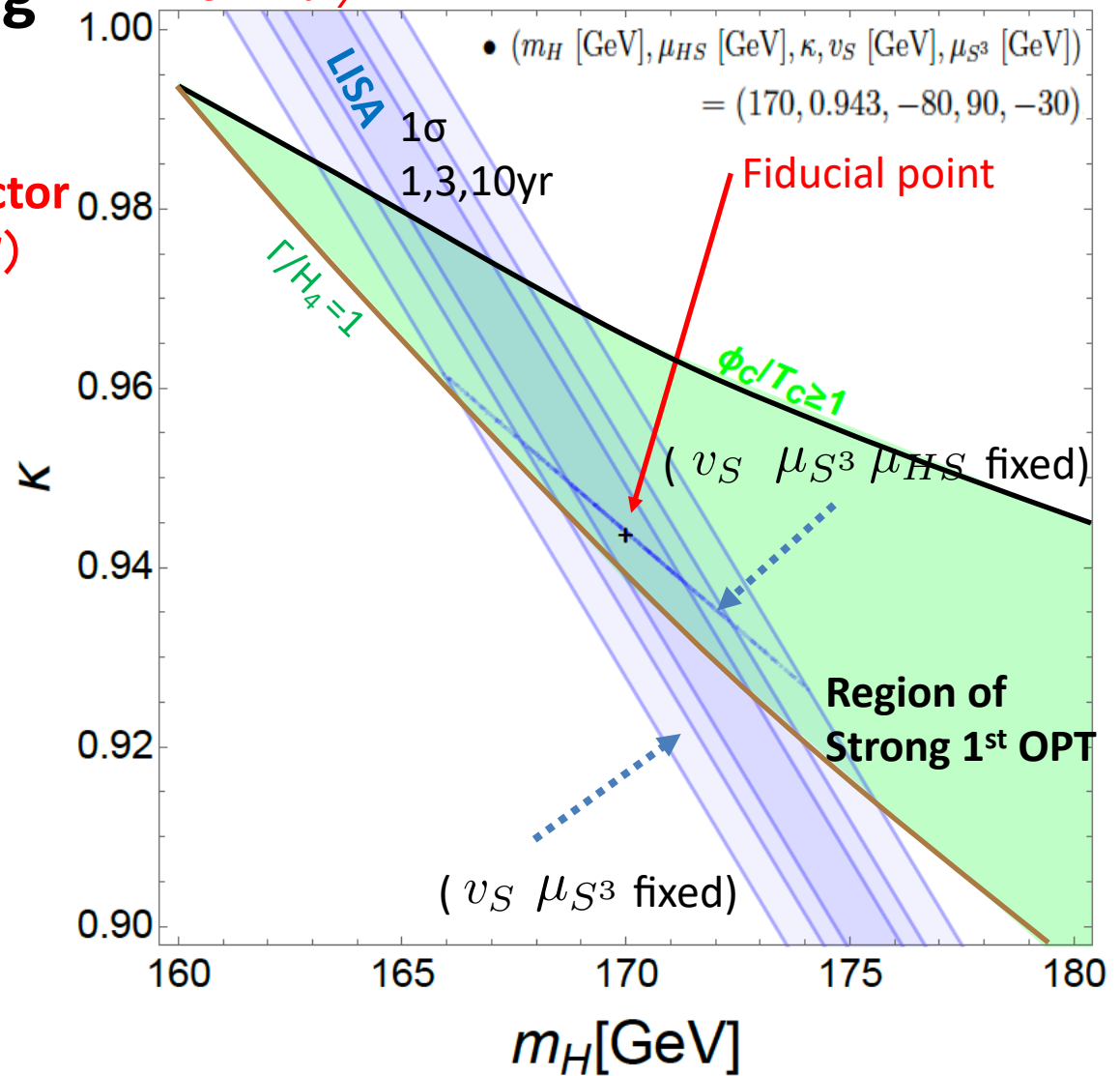
Doublet-Singlet Mixing model

$K (= K_f = K_V = \cos\theta)$: Scaling Factor
 m_H : Mass of the 2nd Higgs (H)

Green:
 area where 1st OPT is
 strongly enough for
 EW baryogenesis

Blue: Constrained area
 from GW at LISA

By Hashino, Jinno, Kakizaki, SK, Takahashi, Takimoto
 Preliminary



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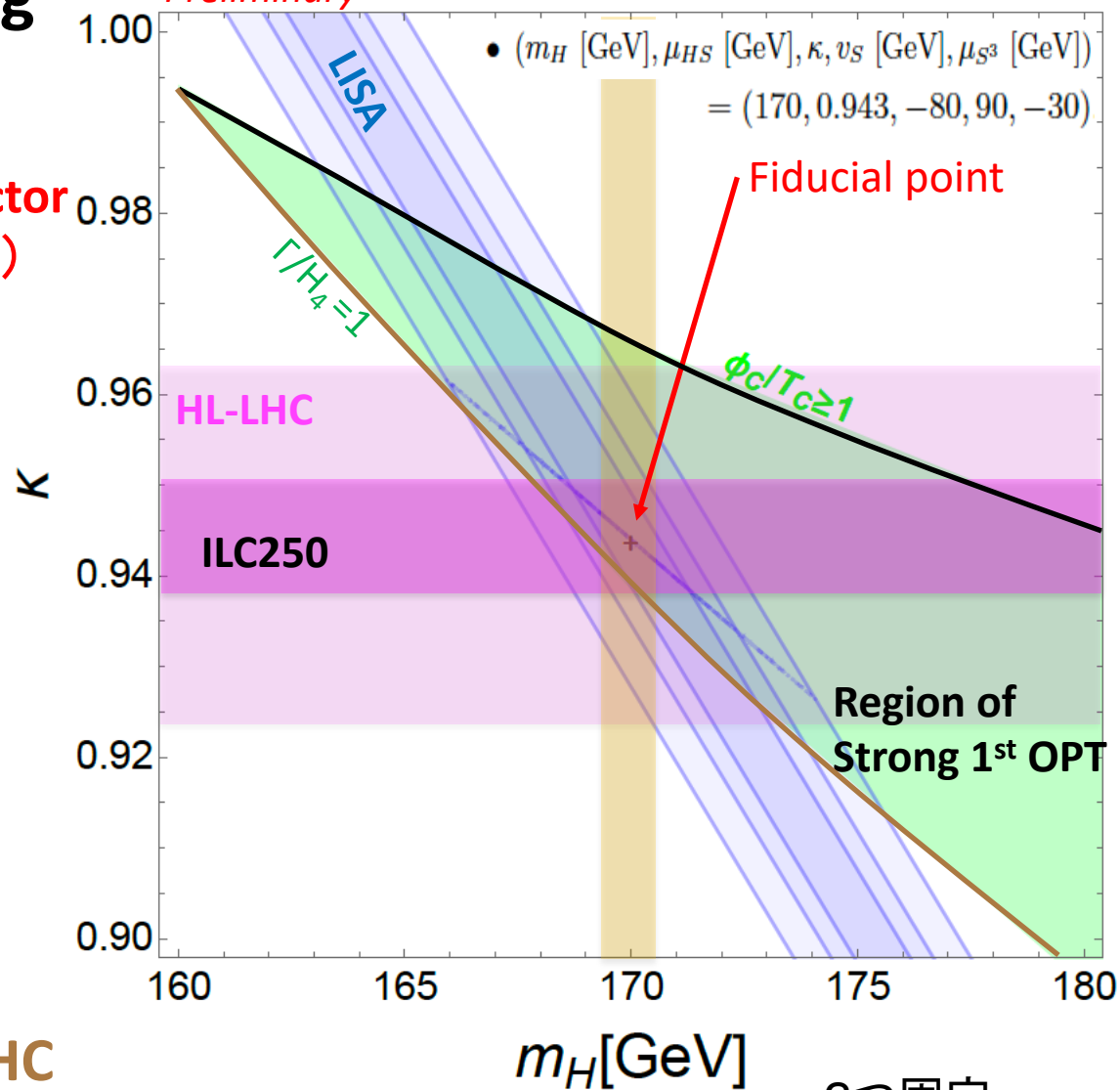
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$\Delta\kappa \sim 2\%$ (HL-LHC)
 0.6% (ILC250)

$\Delta m_H \sim 1 \text{ GeV(?)}$ at (HL-)LHC

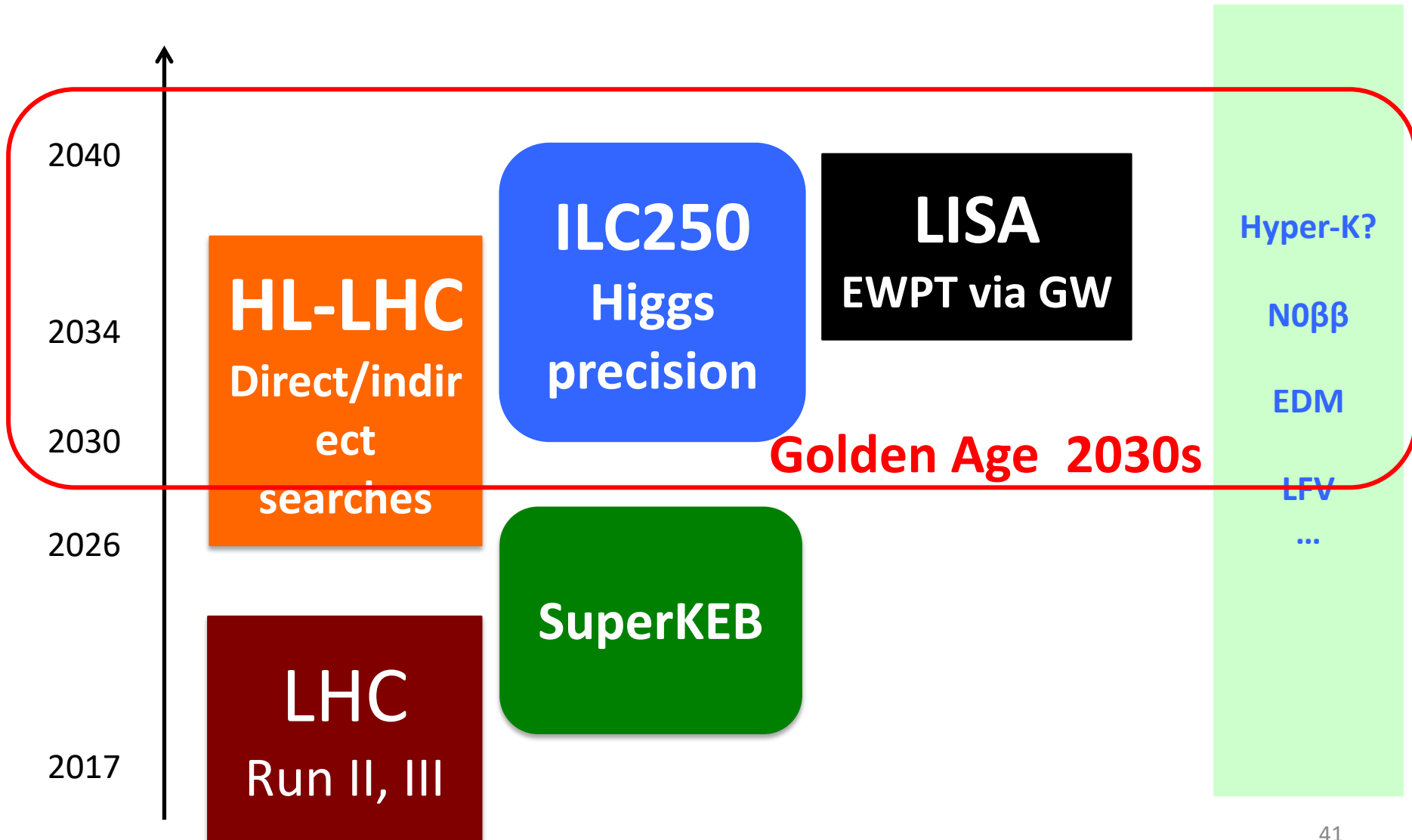
The model can be well tested by the synergy of
 HL-LHC, ILC250 and LISA

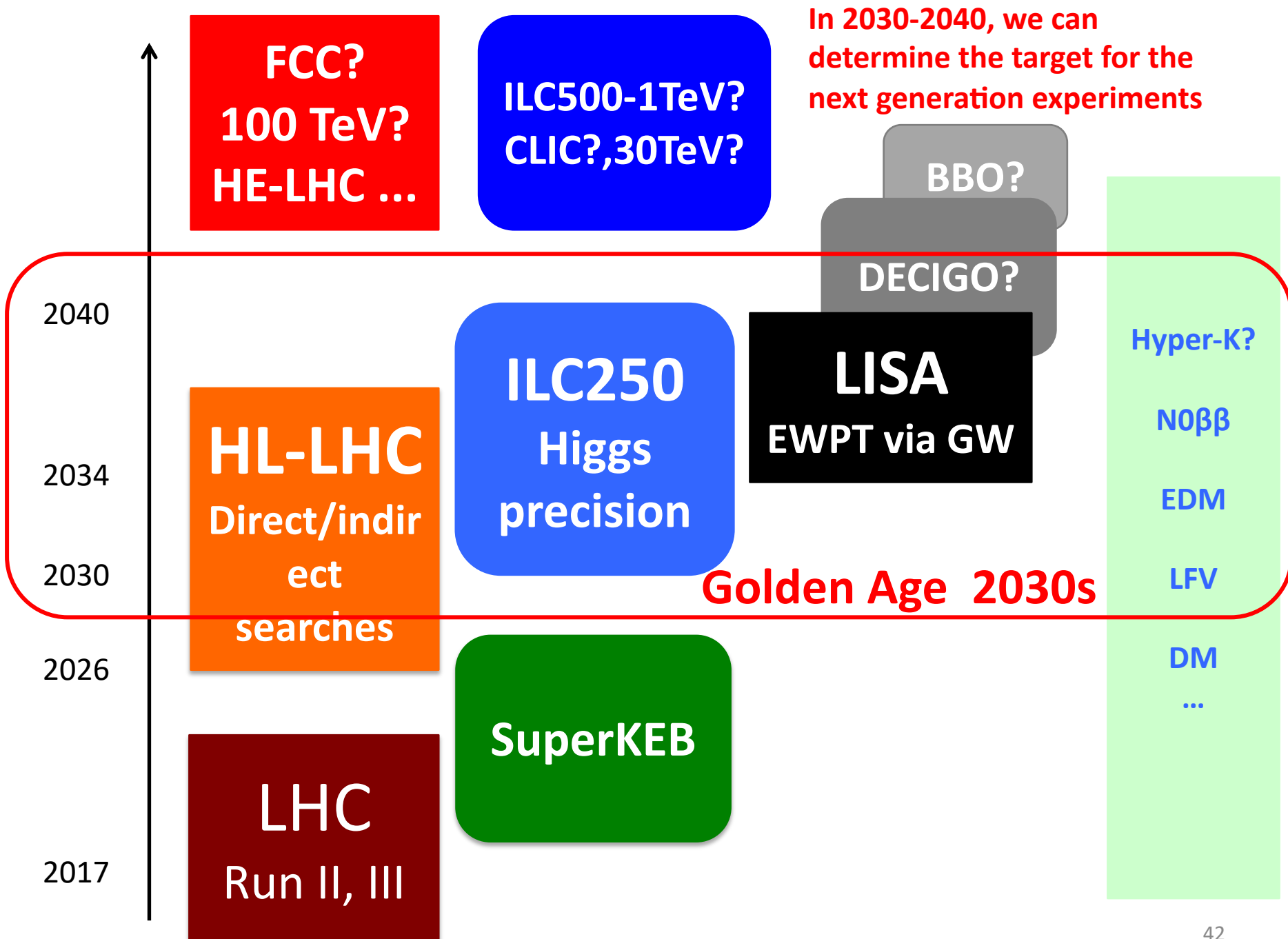
By Hashino, Jinno, Kakizaki, SK, Takahashi, Takimoto
 Preliminary



2つ固定
 と3つ固定

Future experiments





Summary

Although a Higgs boson was found in 2012, the origin of EW symmetry breaking remains unknown. (Dynamics, nature, physics behind, ...)

The non-minimal Higgs sector might be related to phenomena which cannot be explained in the SM.

→ Higgs sector is an important probe of new physics.

By the synergy of

1. Search of the 2nd Higgs bosons at HL-LHC (Hadron Collider),
2. Precision studies of Higgs sectors at ILC250 (Lepton Collider),
3. gravitational wave experiments at LISA

we can thoroughly explore the detail of the Higgs sector in 2030-40s.

→ We showed physics case (an extended Higgs model for 1st OPT)

By knowing the Higgs sector, we can approach to new physics beyond SM.

Summary

Although a Higgs boson was found in 2012, the origin of EW symmetry breaking remains unknown. (Dynamics, nature, physics behind, ...)

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By knowing the Higgs sector, we can approach to new physics beyond SM.

We need ILC

Back up slides

Higgs singlet extension (HSM)

$$V_0 = -\mu_\Phi^2 |\Phi|^2 + \lambda_\Phi |\Phi|^4 + \mu_{\Phi S} |\Phi|^2 S + \frac{\lambda_{\Phi S}}{2} |\Phi|^2 S^2 + \mu_S^3 S + \frac{m_S^2}{2} S^2 + \frac{\mu'_S}{3} S^3 + \frac{\lambda_S}{4} S^4$$

$$\Phi = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}}(v_\Phi + \phi_1 + iG^0) \end{pmatrix}, \quad S = v_S + \phi_2 \quad (\phi_1, \phi_2) \rightarrow (h, H) \text{ with } \theta$$

Two Higgs doublet model (2HDM)

$$V_{\text{THDM}} = m_1^2 |\Phi_1|^2 + m_2^2 |\Phi_2|^2 - (m_3^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}) + \frac{1}{2} \lambda_1 |\Phi_1|^4 + \frac{1}{2} \lambda_2 |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 \\ + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \frac{1}{2} [\lambda_5 (\Phi_1^\dagger \Phi_2)^2 + \lambda_6 |\Phi_1|^2 \Phi_1^\dagger \Phi_2 + \lambda_7 |\Phi_2|^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}],$$

$$\Phi_i = \begin{pmatrix} \omega_i^\pm \\ \frac{1}{\sqrt{2}}(v_i + h_i + iz_i) \end{pmatrix} \quad (i = 1, 2)$$

$$\begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = \begin{pmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} H \\ h \end{pmatrix} \quad \begin{pmatrix} z_1 \\ z_2 \end{pmatrix} = \begin{pmatrix} \cos \beta & -\sin \beta \\ \sin \beta & \cos \beta \end{pmatrix} \begin{pmatrix} z \\ A \end{pmatrix}$$

$\underbrace{h \quad H \quad A \quad H^\pm}_{\text{Additional bosons}}$
 $\uparrow$
 $h(125)$

$\underbrace{H \quad A \quad H^\pm}_{\text{Additional bosons}}$
 $\uparrow$
 $h(125)$

$\underbrace{H \quad A \quad H^\pm}_{\text{Additional bosons}}$
 $\uparrow$
 $h(125)$

With the softly broken Z_2 symmetry (FCNC) $\lambda_6 = \lambda_7 = 0$

4 types of Yukawa interaction (Type I, II, X, Y)

	ξ_h^u	ξ_h^d	ξ_h^ℓ	ξ_H^u	ξ_H^d	ξ_H^ℓ	ξ_A^u	ξ_A^d	ξ_A^ℓ
Type-I	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$	$\sin \alpha / \sin \beta$	$\sin \alpha / \sin \beta$	$\sin \alpha / \sin \beta$	$\cot \beta$	$-\cot \beta$	$-\cot \beta$
Type-II	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$	$-\sin \alpha / \cos \beta$	$\sin \alpha / \sin \beta$	$\cos \alpha / \cos \beta$	$\cos \alpha / \cos \beta$	$\cot \beta$	$\tan \beta$	$\tan \beta$
Type-X	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$	$\sin \alpha / \sin \beta$	$\sin \alpha / \sin \beta$	$\cos \alpha / \cos \beta$	$\cot \beta$	$-\cot \beta$	$\tan \beta$
Type-Y	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$	$\cos \alpha / \sin \beta$	$\sin \alpha / \sin \beta$	$\cos \alpha / \cos \beta$	$\sin \alpha / \sin \beta$	$\cot \beta$	$\tan \beta$	$-\cot \beta$

TABLE II: The mixing factors in each type of Yukawa interactions in the THDMs [40].

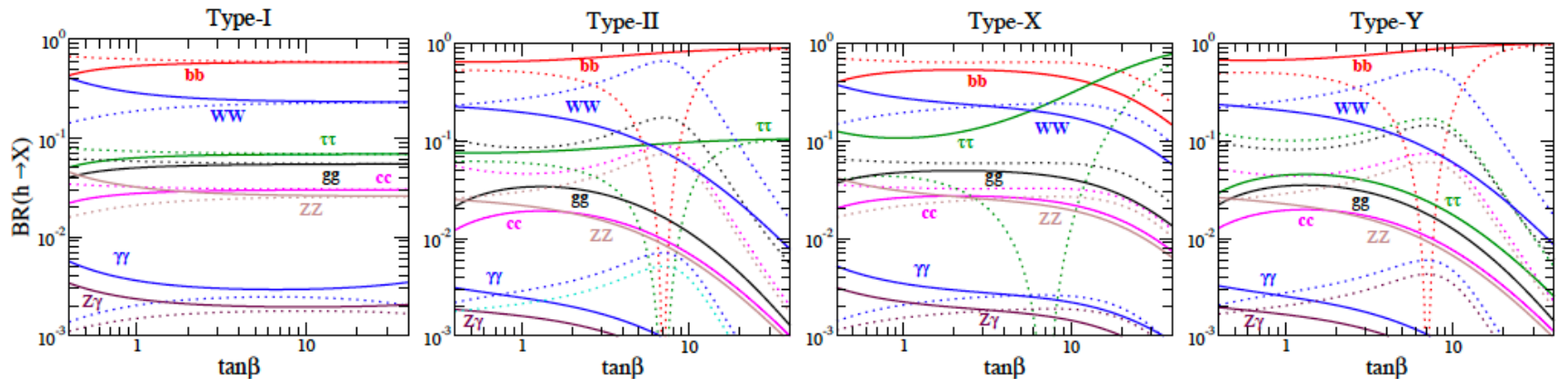
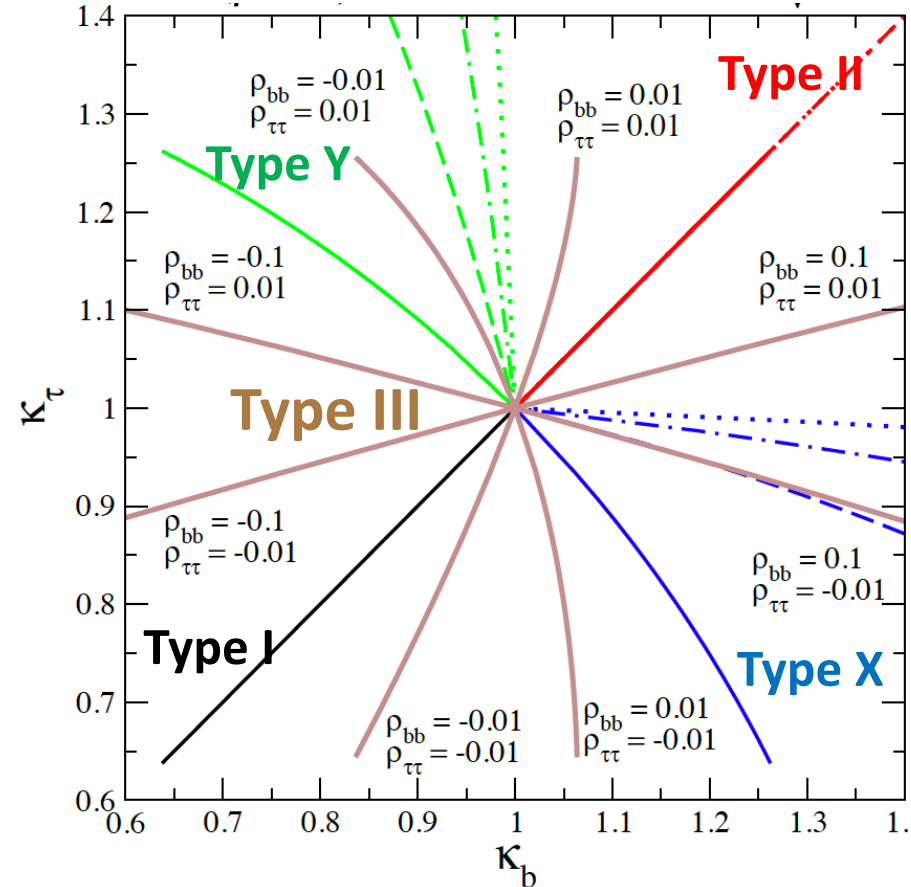


FIG. 6: Decay branching ratios for h as a function of $\tan \beta$ in the case of $m_\Phi = M = 200$ GeV and $\sin(\beta - \alpha) = 0.99$. The solid and dashed curves respectively show the cases with $\cos(\beta - \alpha) < 0$ and $\cos(\beta - \alpha) > 0$.

General 2HDM without the Z_2 symmetry (Type III)

$$\mathcal{L}_Y = -\bar{Q}_{L,i}\tilde{\Phi}\kappa_{ij}^{0,u}u_{R,j}^0 - \bar{Q}_{L,i}\Phi\kappa_{ij}^{0,d}d_{R,j} - \bar{Q}_{L,i}\tilde{\Phi}'\rho_{ij}^{0,u}u_{R,j}^0 - \bar{Q}_{L,i}\Phi'\rho_{ij}^{0,d}d_{R,j} + h.c.$$

Models	κ_V	κ_c	κ_b	κ_τ
Type-I	$s_{\beta-\alpha}$	$s_{\beta-\alpha} + \cot\beta c_{\beta-\alpha}$	$s_{\beta-\alpha} + \cot\beta c_{\beta-\alpha}$	$s_{\beta-\alpha} + \cot\beta c_{\beta-\alpha}$
Type-II	$s_{\beta-\alpha}$	$s_{\beta-\alpha} + \cot\beta c_{\beta-\alpha}$	$s_{\beta-\alpha} - \tan\beta c_{\beta-\alpha}$	$s_{\beta-\alpha} - \tan\beta c_{\beta-\alpha}$
Type-X	$s_{\beta-\alpha}$	$s_{\beta-\alpha} + \cot\beta c_{\beta-\alpha}$	$s_{\beta-\alpha} + \cot\beta c_{\beta-\alpha}$	$s_{\beta-\alpha} - \tan\beta c_{\beta-\alpha}$
Type-Y	$s_{\beta-\alpha}$	$s_{\beta-\alpha} + \cot\beta c_{\beta-\alpha}$	$s_{\beta-\alpha} - \tan\beta c_{\beta-\alpha}$	$s_{\beta-\alpha} + \cot\beta c_{\beta-\alpha}$
Type-III	$s_{-\gamma}$	$s_{-\gamma} + \frac{v}{\sqrt{2}m_c}\rho_{cc}c_\gamma$	$s_{-\gamma} + \frac{v}{\sqrt{2}m_b}\rho_{bb}c_\gamma$	$s_{-\gamma} + \frac{v}{\sqrt{2}m_\tau}\rho_{\tau\tau}c_\gamma$

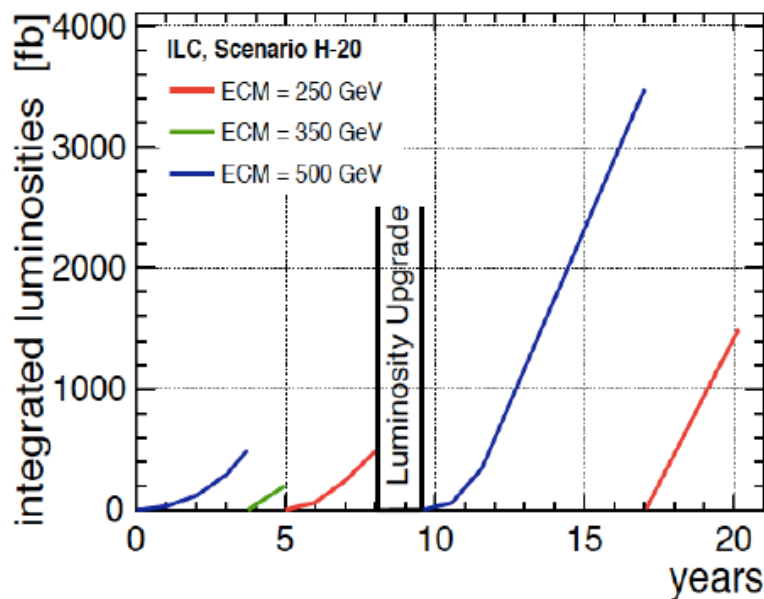


Mariko Kikuchi

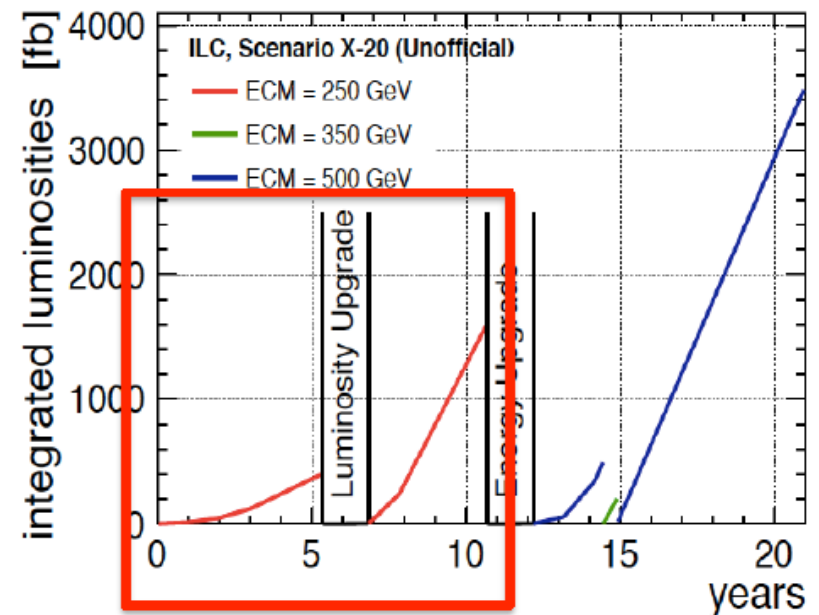
Staging: ILC250 Higgs Factory

Up to Dec. 2016 (LCWS Morioka)
500 GeV start sample scenario

Integrated Luminosities [fb]



After Dec. 2016
Generally agreed by ILC community
To be formalized this fall



ILC250 Higgs Factory

Build the ILC250 Higgs factory as the first stage 'program'

Main Points

Slide by
Hitoshi Yamamoto

- ILC has been designed to lead the new era of particle physics opened up by the discovery of Higgs.
- ILC250 Higgs Factory reduces the cost by up to 40%.
- For precision Higgs measurements, ILC ~ several tens of HL-LHC running simultaneously.
- New particles: at LHC, ~1 million Higgs were produced and then discovered. At ILC, a handful will do.
- Japanese government is about to finish evaluating the case for ILC (ILC 250 Higgs Factory).
- The deadline for inputs to the European Strategy Discussion is the end of this year – important that a positive statement comes from Japanese government in that time scale.

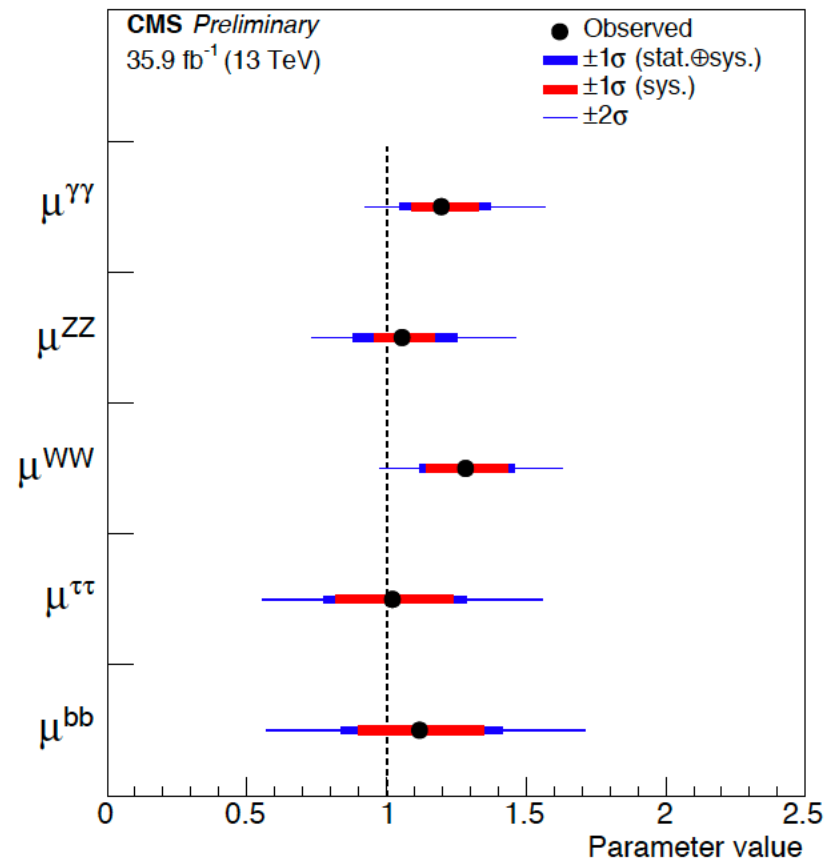
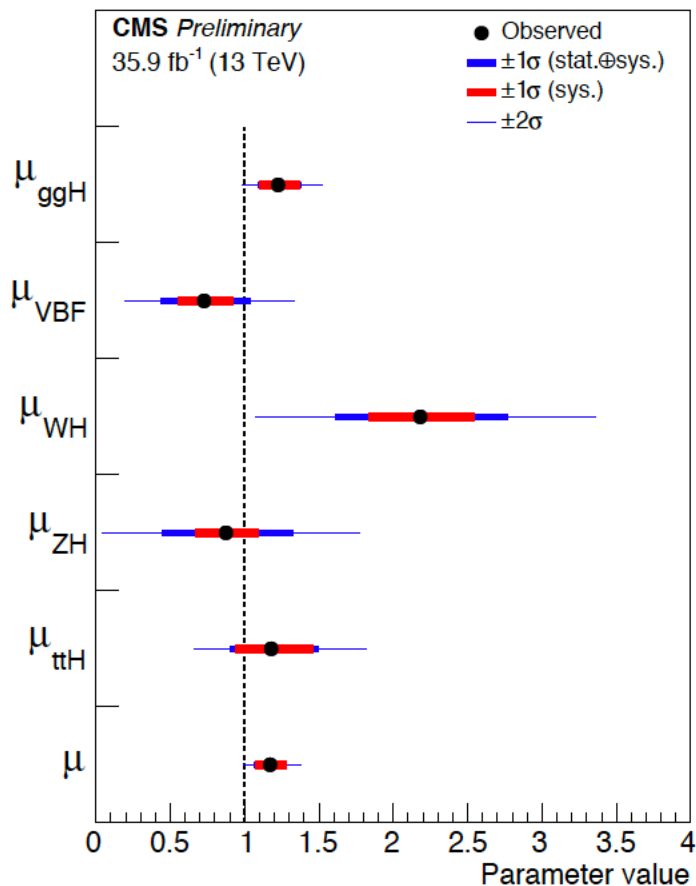


Figure 5: Summary plot of the fit to the per-production mode (left) and per-decay mode (right) signal strength modifiers μ_i . The thick and thin horizontal bars indicate the $\pm 1\sigma$ and $\pm 2\sigma$ uncertainties, respectively. Also shown are the $\pm 1\sigma$ systematic components of the uncertainties. The last point in the per-production mode summary plot is taken from a separate fit and indicates the result of the combined overall signal strength μ .

1st Order Phase Transition

Effective potential at one-loop

$$V_{\text{eff}}(\varphi) = -\frac{\mu^2}{2}\varphi^2 + \frac{\lambda}{4}\varphi^4 + \sum_i \frac{n_i}{64\pi^2} M_i^4(\varphi) \left(\ln \frac{M_i^2(\varphi)}{Q^2} - \frac{3}{2} \right)$$

Finite temperature parts

$$\Delta V_T(\varphi, T) = \frac{T^4}{2\pi^2} \left[\sum_{i=\text{bosons}} n_i I_B(a^2) + \sum_{i=\text{fermions}} n_i I_F(a^2) \right]$$

$$I_{B/F}(a^2) = \int_0^\infty dx x^2 \ln \left(1 \mp e^{-\sqrt{x^2+a^2}} \right) \quad a^2 = \frac{M^2(\varphi, T)}{T^2}$$

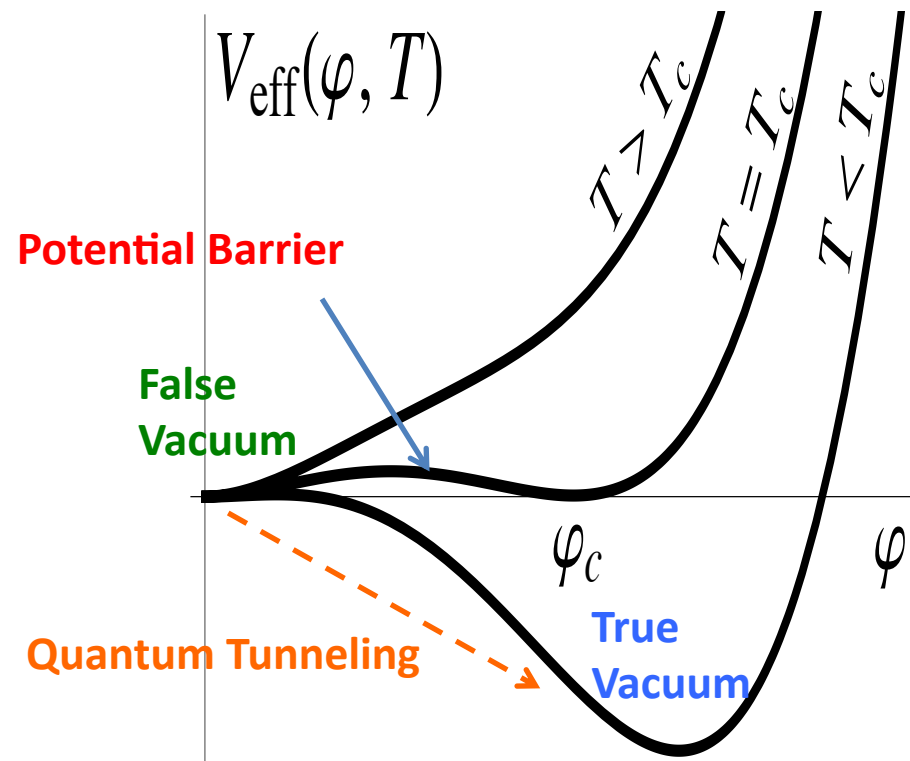
High temperature expansion

$$V_{\text{eff}}(\varphi, T) \simeq D(T^2 - T_0^2)\varphi^2 - \underline{ET}\varphi^3 + \frac{\lambda_T}{4}\varphi^4 + \dots$$

Bosonic loop contribute to the cubic term $\rightarrow$ 1st OPT stronger

$$I_B(a^2) = -\frac{\pi^4}{45} + \frac{\pi^2}{12}a^2 - \frac{\pi}{6}(a^2)^{3/2} - \frac{a^4}{32} \left(\ln \frac{a^2}{\alpha_B} - 3/2 \right) + \mathcal{O}(a^6)$$

$$I_F(a^2) = \frac{7\pi^4}{360} - \frac{\pi^2}{24}a^2 - \frac{a^4}{32} \left(\ln \frac{a^2}{\alpha_F} - 3/2 \right) + \mathcal{O}(a^6)$$



$$\varphi_c/T_c \propto E$$

$$\log \alpha_B = 2 \log 4\pi - 2\gamma_E$$

$$\log \alpha_F = 2 \log \pi - 2\gamma_E$$

$$\gamma_E = 0.5772 \dots$$

Constraints on transition parameters

Constraining parameters

- The GW spectrum is determined by f_{peak} , Ω_{peak}

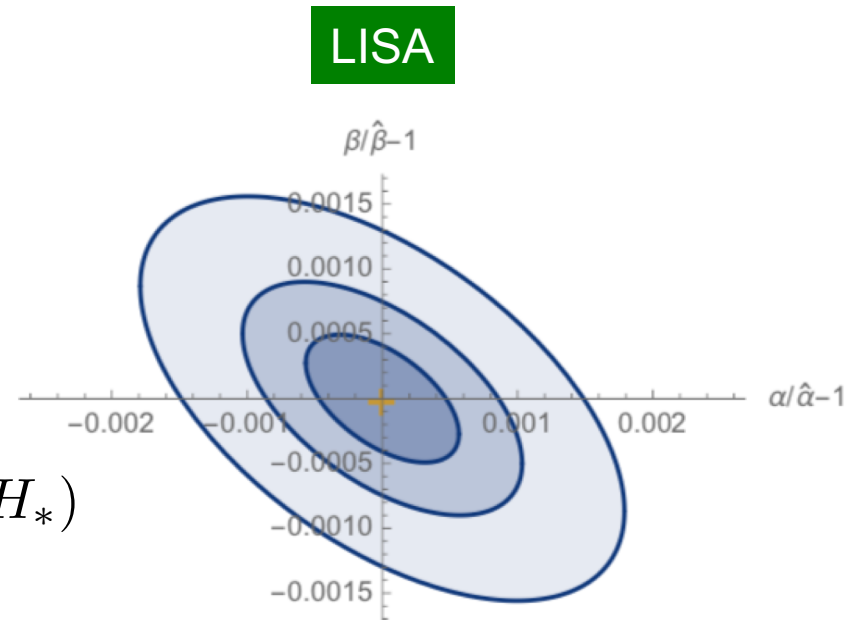
→ Our Fisher analysis generically constrain
2 combinations of underlying parameters

Quantities describing transition dynamics

$$T_*, \quad v_w, \quad \alpha, \quad \frac{\beta}{H_*}$$

Expected constraints on the transition parameters

- Fiducial values
 $(\alpha, \beta/H_*, v_w, T_*) = (1, 100, 1, 100 \text{ GeV})$
- 1σ confidence ellipse in $(\alpha, \beta/H_*)$
for fixed T_* and v_w



Doublet-Singlet Mixing model

$K (= \cos\theta)$: Scaling Factor

m_H : Mass of the 2nd Higgs H

Green:

area where 1st OPT is strongly enough for EW baryogenesis

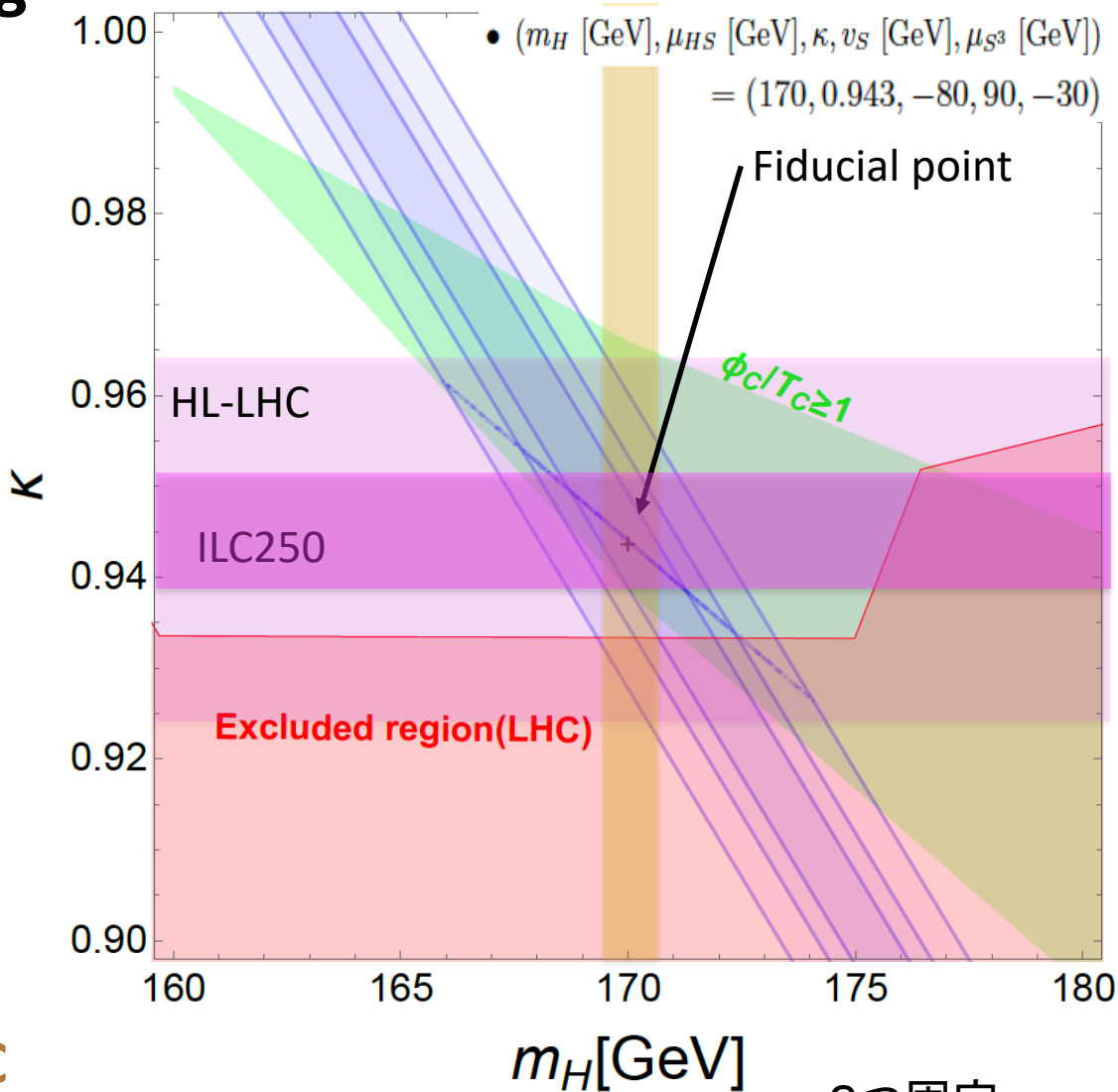
Blue: Constrained area from GW at LISA

$\Delta\kappa \sim 2\%$ (HL-LHC)
 0.6% (ILC250)

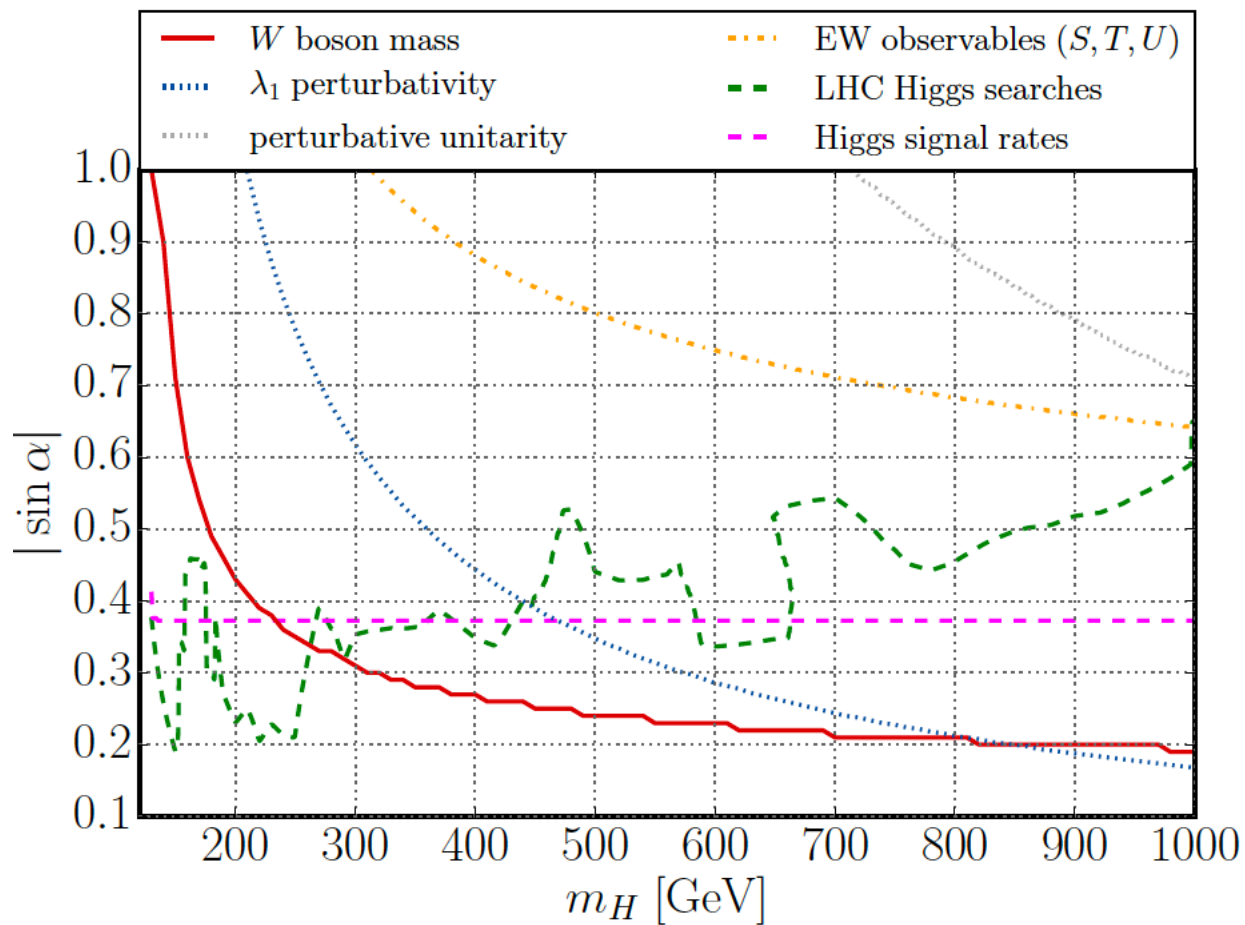
$\Delta m_H \sim 1 \text{ GeV(?)}$ at HL-LHC

The model can be well tested by the synergy of HL-LHC, ILC250 and LISA

Hashino, Jinno, Kakizaki, SK, Takahashi, Takimoto

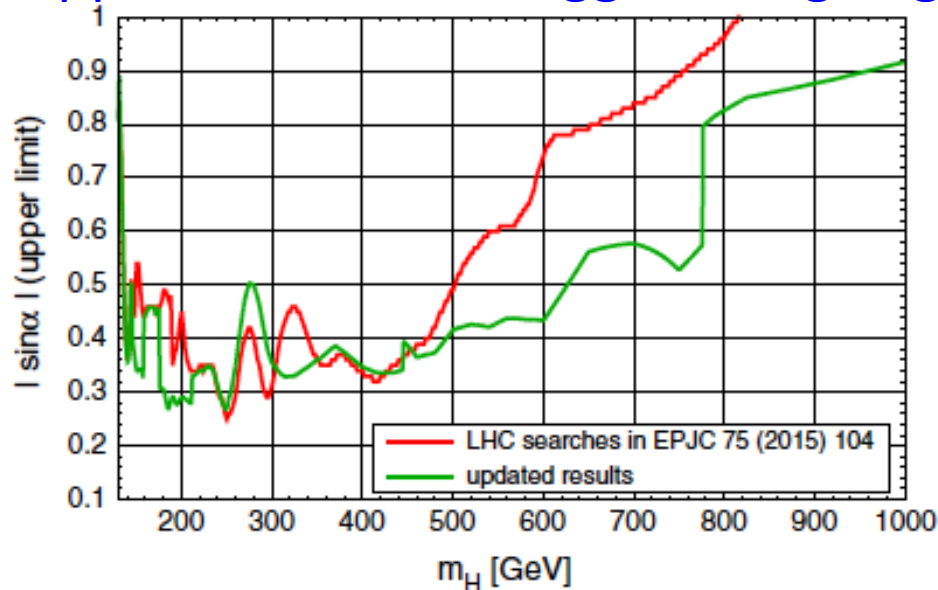


2つ固定
と3つ固定



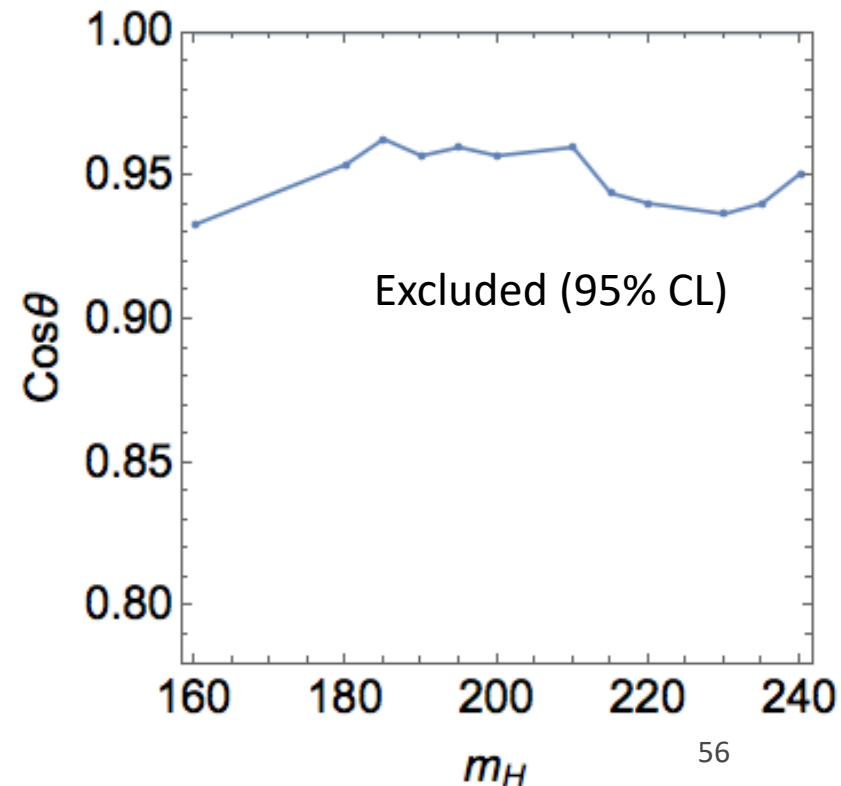
Direct searches for the additional Higgs boson in the HSM at the LHC

Upper limit on the Higgs mixing angle $|\sin \theta|$
 [Robens, Stefaniak (2016)]



Range of m_H [GeV]	Search channel
130–145	$H \rightarrow ZZ \rightarrow 4l$
145–158	$H \rightarrow VV$ ($V=W,Z$)
158–163	SM comb.
163–170	$H \rightarrow WW$
170–176	SM comb.
176–211	$H \rightarrow VV$ ($V=W,Z$)
211–225	$H \rightarrow ZZ \rightarrow 4l$
225–445	$H \rightarrow VV$ ($V=W,Z$)

→ Constraints on the Higgs boson coupling $\kappa (= \cos \theta)$

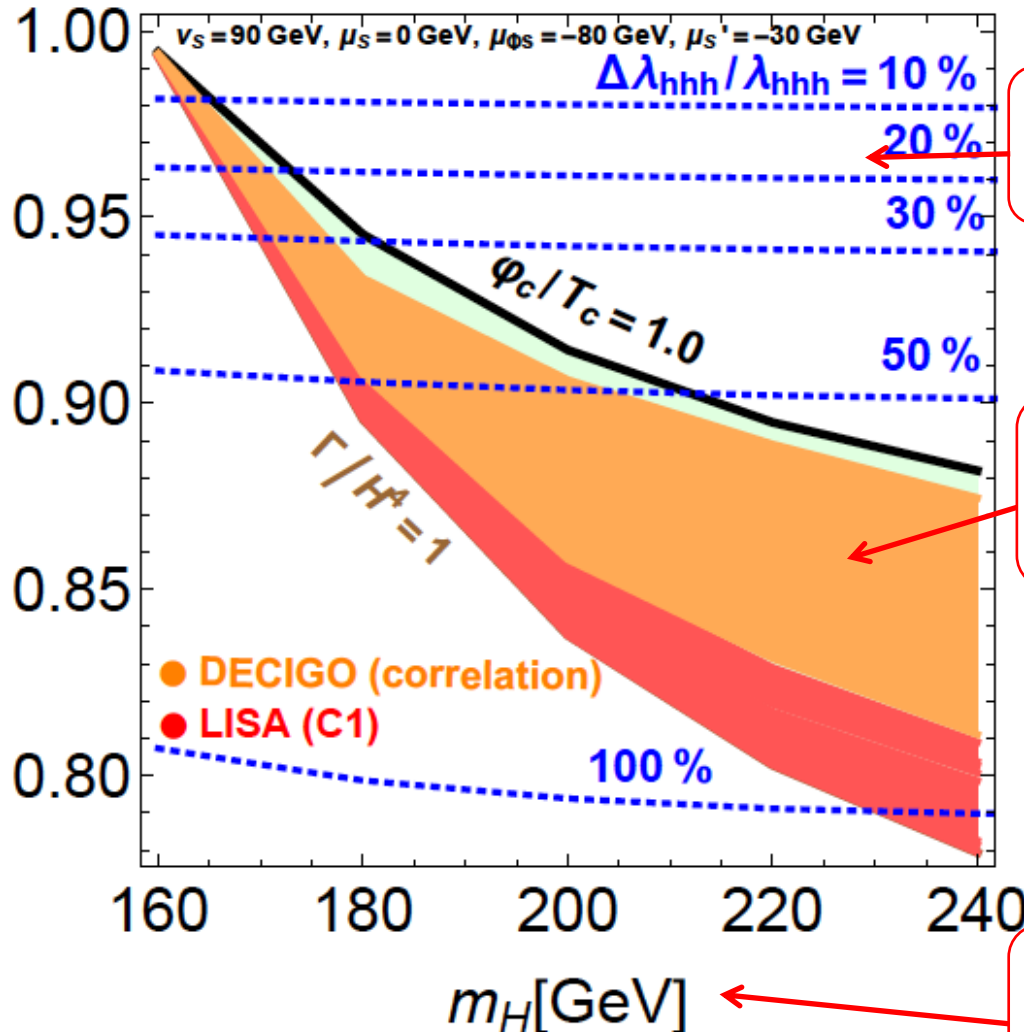


Model of EW Baryogenesis will be well tested by the synergy of HL-LHC, **ILC250**, LISA/DECIGO,

$$K = K_V = K_f$$

$$= \cos\theta$$

Precision measurement at ILC250

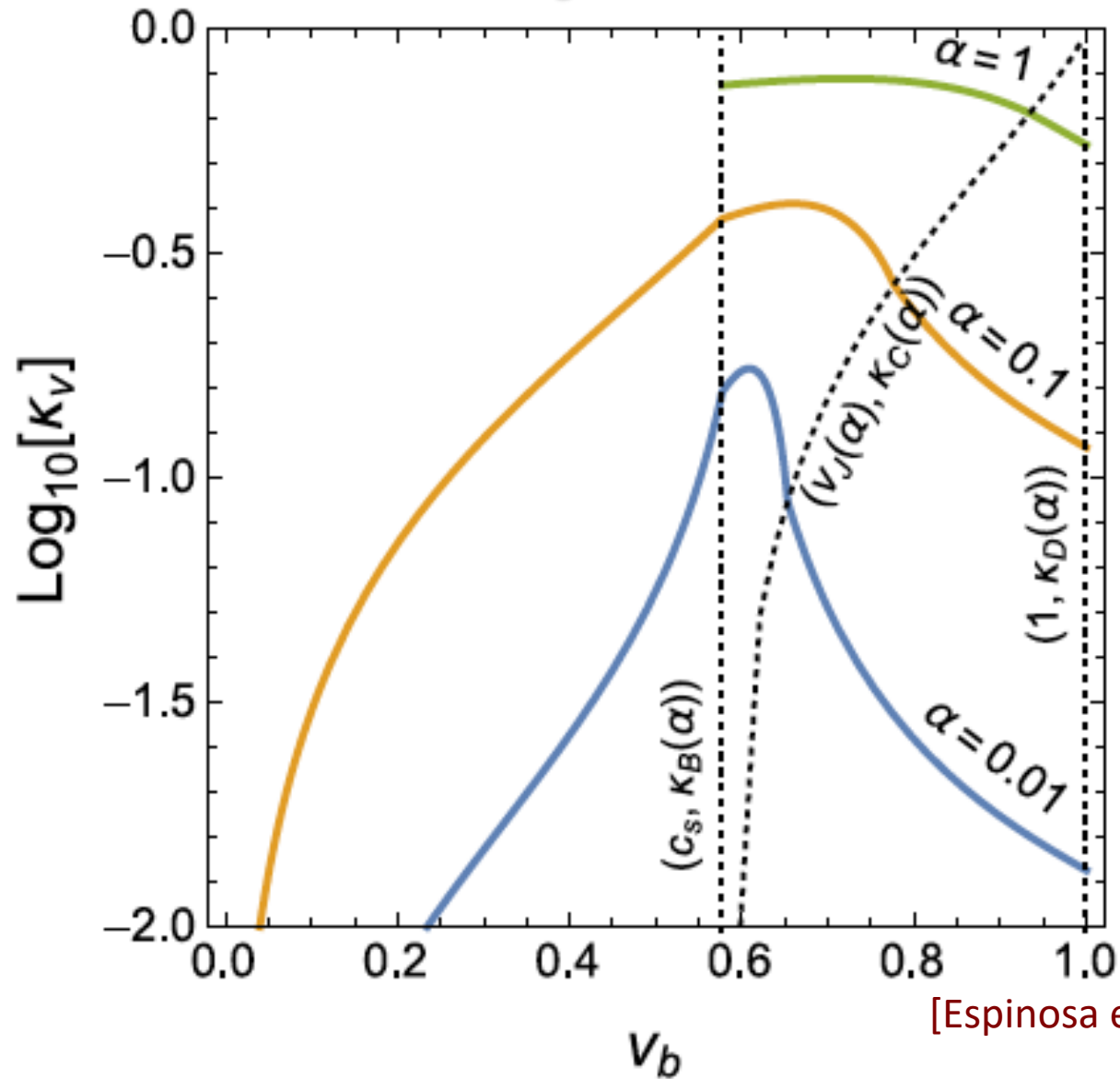


Self-coupling hhh measurement at ILC

Measurement of Gravitational Waves at LISA/DECIGO

Direct searches of the second Higgs at LHC

Efficiency factor



[Espinosa et al. (2010)]

Red-shifted frequency

$$f_0 = \frac{a_t}{a_0} f_t$$

a_t : scale factor
 f_t : frequency
at the transition

Conservation of the entropy per comoving volume

$$sa^3 = \frac{2\pi^2}{45} g_s T^3 a^3 = \text{const}$$

$$\frac{a_t}{a_0} = \left(\frac{g_{s0}}{g_s^t} \right)^{1/3} \frac{T_0}{T_t}$$

Radiation dominant Universe

$$H = \sqrt{\frac{4\pi^3}{45}} g_*^{1/2} \frac{T^2}{M_{\text{Pl}}}$$

We obtain

$$f_0 \simeq 1.7 \times 10^{-5} \left(\frac{g_*^t}{100} \right)^{1/6} \left(\frac{T_t}{100 \text{ GeV}} \right) \frac{f_t}{H_t} \text{ Hz}$$

f_t/H_t must be > 1 , typically 10^2 (10^2 - 10^4)

$1/f_t$ Wavelength of GWs at the PT

$1/H_t$ Size of the universe (horizon) at the PT

$$f_0 = 10^{-3} - 10^{-1} \text{ Hz}$$

Characteristic GW Abundance from the strong EW 1st OPT

Normalized energy density

$$\Omega_{\text{GW}}(f) \equiv \frac{1}{\rho_c} \frac{d\rho_{\text{GW}}}{d \ln f}$$

$$\left\{ \begin{array}{l} \rho_{\text{GW}} = \frac{1}{32\pi G} \langle \dot{h}_{ij} \dot{h}_{ij} \rangle \\ \rho_c = \frac{3H_0^2}{8\pi G} \end{array} \right.$$

$$h_{\mu\nu}^{\text{TT}} = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & h_+ & h_\times & 0 \\ 0 & h_\times & -h_+ & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

Transverse-Traceless gauge

Red shifted abundance

Scaling $\rho_{\text{GW}} = \left(\frac{a_t}{a_0} \right)^4 \rho_{\text{GW}}^t \quad \rho_c = \left(\frac{H_0}{H_t} \right)^2 \rho_c^t$

$$\Omega_{\text{GW}} h^2 \simeq 1.7 \times 10^{-5} \left(\frac{100}{g_*^t} \right)^{1/3} \Omega_{\text{GW}}^t$$

Characteristic GW Abundance from the strong EW 1st OPT

At the phase transition, we have $\rho_{\text{GW}}^t \sim \frac{\dot{h}_{ij}^2}{G}$ $\rho_c^t \sim \frac{H_t^2}{G}$

Einstein Equation

$$\square h_{ij} \sim GT_{ij}$$

Typical duration of the phase transition: $1/\beta$

$$\beta^2 h_{ij} \sim GT_{ij}$$

$$\dot{h}_{ij} \sim \beta h_{ij} \sim \frac{GT_{ij}}{\beta}$$

Eenergy density at PT

$$\Omega_{\text{GW}}^t = \frac{\rho_{\text{GW}}^t}{\rho_c^t} \sim \frac{H_t^2}{\beta^2} \frac{T_{ij}^2}{(\rho_c^t)^2} \sim \frac{H_t^2}{\beta^2} \frac{\rho_{\text{kin}}^2}{(\rho_{\text{vac}} + \rho_{\text{rad}}^t)^2}$$

$$\Omega_{\text{GW}}^t \sim \frac{H_t^2}{\beta^2} \frac{\kappa^2 \alpha^2}{(1 + \alpha)^2}$$

$$\alpha = \rho_{\text{vac}} / \rho_{\text{rad}}^t$$

$$\kappa = \rho_{\text{kin}} / \rho_{\text{vac}}$$

Characteristic GW Abundance from the strong EW 1st OPT

Abundance of GWs

$$\Omega_{\text{GW}} h^2 \simeq 1.7 \times 10^{-5} \frac{H_t^2}{\beta^2} \frac{\kappa^2 \alpha^2}{(1 + \alpha)^2}$$

$$\alpha = \rho_{\text{vac}} / \rho_{\text{rad}}^t$$

Energy density of false vacuum
released by PT

$$\kappa = \rho_{\text{kin}} / \rho_{\text{vac}}$$

Efficiency of kinetic energy of walls
in the release energy.

The spectrum is determined by

α (latent heat), β (duration of PT), κ (Efficiency)

They can be basically calculated if a model is given.

This rough estimation is applicable to GWs from the wall collision. However, Ωh^2 is enhanced by β/H_t for GWs from the motion of thermal plasma fluid (sound waves and turbulence). *Hindmarsh*

Properties of the representative **LISA** configurations

C.Caprini *et al.*, arXiv:1512.06239

Name	C1	C2	C3	C4
Full name	N2A5M5L6	N2A1M5L6	N2A2M5L4	N1A1M2L4
# links	6	6	4	4
Arm length [km]	5M	1M	2M	1M
Duration [years]	5	5	5	2
Noise level	N2	N2	N2	N1

LISA has been approved in 2016
It will start from 2034

FP (Fabry-Perot)-**DECIGO**

1 cluster (arm length 1000km)

Correlation between 2 cluster

S. Kawamura et al, Class. Quant. Grav. 28, 094011 (2011)