

# Impact of $SU(2)$ representation in models for B and $g-2$ anomalies from Dark Loops

**Rodrigo Capucha**

**Collaboration:** Da Huang, Tomás Lopes, Rui Santos



**Workshop on Multi-Higgs Models, 30 August 2022**

**Financial support by:** FCT grant 2020.08221.BD

FCT projects UIDB/00618/2020, UIDP/00618/2020, PTDC/FISPAR/31000/2017, CERN/FISPAR/0014/2019

# Overview

- In 2012, a new scalar particle with a mass close to 125 GeV, later identified as the **Higgs boson**, was discovered at the **Large Hadron Collider (LHC)**. Electroweak symmetry breaking confirmed and **SM completed**.
- Most experimental results agree with the SM predictions, but there are exceptions: **B meson decays** and **muon's anomalous magnetic moment**. Also, the **SM cannot be the final theory** – no explanation for **dark matter (DM)**, not enough CP-violation to explain **matter-antimatter asymmetry**.
- We must explore **new physics beyond the SM** to address these issues. **Models for B and  $(g-2)_\mu$  anomalies from dark loops**:
  - Motivation;
  - Theoretical framework;
  - Flavor, DM and EW constraints;
  - Results;
  - Conclusions.

# Motivation

- Hints of NP come from the observed **anomalies in the semileptonic decay rates of the B meson**:

$$R(K^{(*)}) = \mathcal{B}(B \rightarrow K^{(*)} \mu^+ \mu^-) / \mathcal{B}(B \rightarrow K^{(*)} e^+ e^-)$$

**LHCb Collaboration** [JHEP08\(2017\)055](#), [Nature Phys. 18, 277 \(2022\)](#)

$$R(K) = 0.846_{-0.039-0.012}^{+0.042+0.013}, \quad q^2 \in [1.1, 6] \text{ GeV}^2$$

$$R(K^*) = \begin{cases} 0.660_{-0.070}^{+0.110} \pm 0.024, & q^2 \in [0.045, 1.1] \text{ GeV}^2, \\ 0.685_{-0.069}^{+0.113} \pm 0.047, & q^2 \in [1.1, 6] \text{ GeV}^2. \end{cases}$$

**SM predictions** [Hiller et al., PhysRevD.69.074020](#)  
[Bordone et al., Eur. Phys. J. C 76, 440 \(2016\)](#)

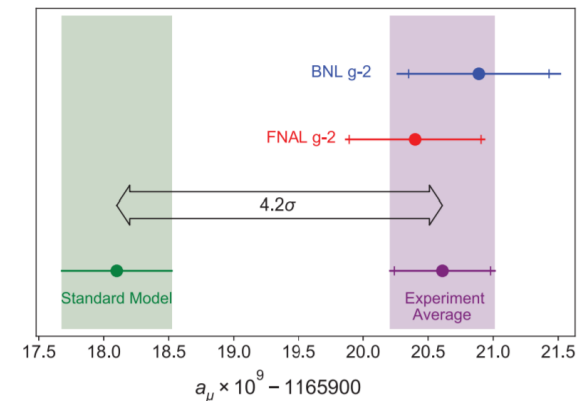
$$R(K) = 1.0004(8), \quad q^2 \in [1.1, 6] \text{ GeV}^2,$$

$$R(K^*) = \begin{cases} 0.920 \pm 0.007, & q^2 \in [0.045, 1.1] \text{ GeV}^2, \\ 0.996 \pm 0.002, & q^2 \in [1.1, 6] \text{ GeV}^2. \end{cases}$$

- Another NP important hint comes from the measurement of the **(g - 2) of the muon**, showing a **4.2σ discrepancy** relative to the SM prediction:

$$\Delta a_\mu = a_\mu^{\text{Exp}} - a_\mu^{\text{SM}} \approx (251 \pm 59) \times 10^{-11}$$

[Muon g-2 Collaboration, PhysRevLett.126.141801](#)



- Further demand for NP arises from several observations pointing to the existence of **dark matter** (galaxy rotation curves, galaxy clusters, CMB, gravitational lensing, structure formation, others), whose nature remains a mystery.

# Theoretical framework

- All three previous issues can be solved by a class of models with several new particles: **one vectorlike fermion** ( $\chi$ ), and **two extra scalar fields**, one  $SU(3)_c$  colored ( $\Phi_3$ ) and the other colorless ( $\Phi_2$ ). Anomalies in B meson decays and g-2 solved by one-loop contributions involving these fields, one of which is the **DM candidate**.
- $SU(2)_L$  representation** of new particles is either **singlet, doublet, or triplet**. All new particles belong to the  **$Z_2$  odd sector**. Vectorlike fermions have electric charge 0 or  $\pm 1$ . Charges of remaining new fields determined by the Yukawa interaction:

$$\mathcal{L}_{Yuk}^{NP} = y_{Q_i} \bar{Q}_{Li} \Phi_3 \chi_R + y_{L_i} \bar{L}_{Li} \Phi_2 \chi_R + H.c.$$

- In total there are 8 possible models. We will study **Model 3**, and compare it to the previously studied **Model 5** [Huang, Moraes and Santos, PhysRevD.102.075009](#)

**Model 3**

|          | $SU(3)_c$ | $SU(2)_L$ | $U(1)_Y$ |
|----------|-----------|-----------|----------|
| $\chi_R$ | 1         | 1         | -1       |
| $\Phi_2$ | 1         | 2         | 1/2      |
| $\Phi_3$ | 3         | 2         | 7/6      |

**Model 5**

|          | $SU(3)_c$ | $SU(2)_L$ | $U(1)_Y$ |
|----------|-----------|-----------|----------|
| $\chi_R$ | 1         | 2         | -1/2     |
| $\Phi_2$ | 1         | 1         | 0        |
| $\Phi_3$ | 3         | 1         | 2/3      |

# Theoretical framework

- The **Higgs potential** for Model 3 is:

$$\begin{aligned}
 V = & -m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 + m_{33}^2 \Phi_3^\dagger \Phi_3 + \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \lambda_2 (\Phi_2^\dagger \Phi_2)^2 - \lambda_3 (\Phi_{3,a}^\dagger \Phi_{3,a}) (\Phi_{3,b}^\dagger \Phi_{3,b}) \\
 & + \lambda_{12} (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_{13} (\Phi_1^\dagger \Phi_1) (\Phi_3^\dagger \Phi_3) + \lambda_{23} (\Phi_2^\dagger \Phi_2) (\Phi_3^\dagger \Phi_3) + \lambda_5 [(\Phi_1^\dagger \Phi_2)^2 + (\Phi_2^\dagger \Phi_1)^2] \\
 & + \lambda'_{12} (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \lambda'_{13} (\Phi_1^\dagger \Phi_3) (\Phi_3^\dagger \Phi_1) + \lambda'_{23} (\Phi_2^\dagger \Phi_3) (\Phi_3^\dagger \Phi_2) \\
 & + y_{13} (\Phi_1^T i \sigma_2 \Phi_3)^\dagger (\Phi_1^T i \sigma_2 \Phi_3) + y_{23} (\Phi_2^T i \sigma_2 \Phi_3)^\dagger (\Phi_2^T i \sigma_2 \Phi_3)
 \end{aligned}$$

- Scalar fields** (in the unitary gauge):

$$\Phi_1 = \begin{bmatrix} 0 \\ \frac{1}{\sqrt{2}} (v + h) \end{bmatrix}, \quad \Phi_2 = \begin{bmatrix} \phi_l^+ \\ \frac{1}{\sqrt{2}} (S + iA) \end{bmatrix}, \quad \Phi_3 = \begin{bmatrix} \phi_q^{+5/3} \\ \phi_q^{+2/3} \end{bmatrix}$$

- Two potential DM candidates**: the neutral scalar S or the pseudoscalar A. We chose **S** as the **DM particle** (results unchanged if we chose A). Same choice made in Model 5.
- The **Z<sub>2</sub> odd particles** **only couple to down-quarks of the last two generations** and **second-generation leptons** (only  $y_b$ ,  $y_s$  and  $y_\mu$  are relevant), to suppress the strong flavor constraints on the first-generation of quarks and leptons and simplify the analysis.

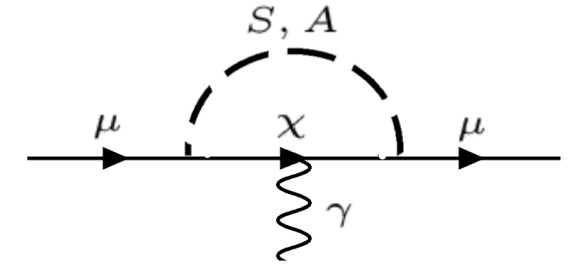
$$\mathcal{L} = y_{di} (\bar{u}_{Lj} V_{ji} \chi_R^- \phi_q^{+5/3} + \bar{d}_{Li} \chi_R^- \phi_q^{+2/3}) + y_{Li} (\bar{\nu}_{Li} \chi_R^- \phi_l^+ + \frac{\bar{e}_{Li}}{\sqrt{2}} \chi_R^- (S + iA)) + H.c.$$

# Flavor, dark matter and electroweak constraints

- **Model 3 contribution to (g-2)** (same as Model 5):

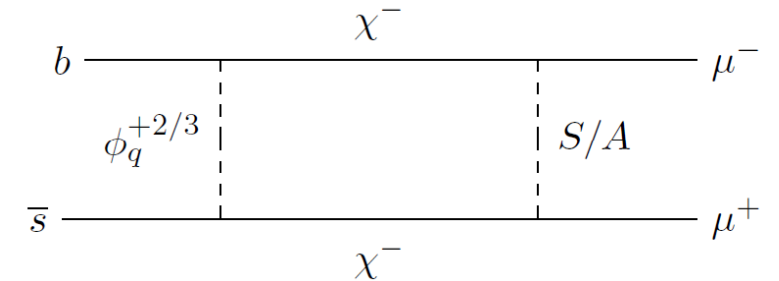
[Arnan, Crivellin, Hofer and Mescia, JHEP04\(2017\)043](#)

$$\Delta a_\mu = \frac{m_\mu^2 |y_\mu|^2}{16\pi^2 m_\chi^2} (\tilde{F}_7(x_S) + \tilde{F}_7(x_A))$$



- **Model 3 contribution to  $B \rightarrow K^{(*)} \mu^+ \mu^-$  ( $b \rightarrow s \mu^+ \mu^-$ ) decays** (same as Model 5):

$$C_9^{NP} = -C_{10}^{NP} = \frac{\sqrt{2}}{4G_F V_{tb} V_{ts}^*} \frac{y_s y_b^* |y_\mu|^2}{64\pi\alpha m_\chi^2} (F(x_{\phi_q^{+2/3}}, x_S) + F(x_{\phi_q^{+2/3}}, x_A))$$



- $C_9^{NP} = -C_{10}^{NP} = [-0.59, -0.30]$ , [Algueró et al., Eur. Phys. J. C 82, 326 \(2022\)](#). In our numerical scan, all points must generate these Wilson coefficients within their  $2\sigma$  range.

- **Model 3 contribution to  $Bs - \bar{B}s$  mixing** (same as Model 5):

$$C_{B\bar{B}} = \frac{(y_s y_b^*)^2}{128\pi^2 m_\chi^2} F(x_{\phi_q^{+2/3}}, x_{\phi_q^{+2/3}}) \quad R_{\Delta M_s} = \frac{\Delta M_s^{Exp}}{\Delta M_s^{SM}} - 1 = -0.09 \pm 0.08 \quad R_{\Delta M_s} = \left| 1 + \frac{0.8 C_{B\bar{B}}(\mu_H)}{C_{B\bar{B}}^{SM}(\mu_b)} - 1 \right|$$

- We constrain  $C_{B\bar{B}}$  by requiring  $R_{\Delta M_s}$  to lie in its  $2\sigma$  range. [Arnan, Crivellin, Fedele and Mescia, JHEP06\(2019\)118](#)

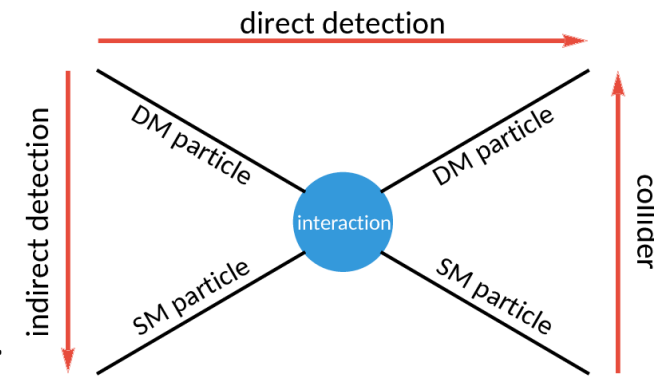
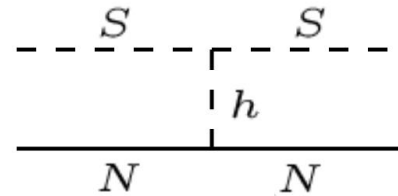
# Flavor, dark matter and electroweak constraints

- **DM relic density:**  $\Omega_{\text{DM}} h^2 = 0.120 \pm 0.001$ , [Planck Collaboration et al., A&A 641, A6 \(2020\)](#). Assuming the **freeze-out** mechanism, the relic abundance is determined by solving the Boltzmann equation which we do numerically using **MICROMEAS**.

$$\frac{dn_S}{dt} + 3Hn_S = -\langle\sigma v\rangle(n_S^2 - n_S^{\text{eq}2})$$

- **Dark matter direct detection:**

$$\sigma(SN \rightarrow SN) = \frac{(\lambda_{12} + \lambda'_{12} + 2\lambda_5)^2}{4\pi} \frac{f_N^2 m_N^2 \mu_{SN}^2}{m_S^2 m_h^4}$$



- Best experimental upper bounds come from the **LZ**, **PandaX-4T** and **XENON1T** experiments.

[LZ Collaboration, arXiv:2207.03764](#), [PandaX-4T Collaboration, PhysRevLett.127.261802](#), [XENON Collaboration, PhysRevLett.121.111302](#)

- **Collider searches:** upper bound for **Higgs to invisible decays** is  **$B(h \rightarrow SS) < 0.11$** . [PDG, Zyla et al., PTEP 2020, 083C01 \(2020\)](#)
- **Model 3 contribution to EW oblique parameter T** (no contributions in Model 5): colored scalars have vanishing contributions (equal mass).  **$T = 0.03 \pm 0.12$** . Constraint applied at the end, requiring T to be within its  $2\sigma$  range.

$$T = \frac{g^2}{64\pi^2 m_W^2 \alpha} [F(m_{\phi_l}^2, m_S^2) + F(m_{\phi_l}^2, m_A^2) - F(m_S^2, m_A^2)] \quad F(A, B) = \begin{cases} \frac{A+B}{2} - \frac{AB}{A-B} \ln \frac{A}{B}, & \text{if } A \neq B. \\ 0, & A = B. \end{cases}$$

[Grimus, Lavoura et al., J. Phys. G: Nucl. Part. Phys. 35 075001 \(2008\)](#)

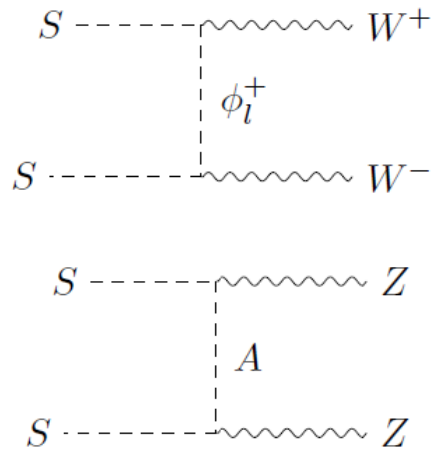
# Results

- **Multiparameter random scan** to find parameter regions that satisfy all relevant flavor constraints, the muon anomalous magnetic moment, the DM constraints and the corrections to the EW oblique parameter T.
- **Final constraints:**
  - $y_s$  and  $y_b$  are real with  $y_s = -y_b/4$ ,  $|y_b| \leq 1$ ,  $1 \leq y_\mu \leq 4\pi$ .
  - Colored scalars mass:  $m_{\phi_l}^{5/3} = m_{\phi_l}^{2/3} = 1.5 \text{ TeV}$ .
  - All particles in the dark sector at least (most) 10 GeV (1 TeV) heavier than S, with  $5 \text{ GeV} \leq m_s \leq 1 \text{ TeV}$ .
  - **LEP constraints:**
    - ❑  $m_S + m_{\phi_l} > m_W$ ,  $m_A + m_{\phi_l} > m_W$ ,  $m_S + m_A > m_Z$ ,  $2m_{\phi_l} > m_Z$ ,  $m_{\phi_l} > 70 \text{ GeV}$ ; [A. Pierce and J. Thaler, JHEP08\(2007\)026](#)
    - ❑  $m_S < 80 \text{ GeV} + m_A < 100 \text{ GeV} + m_A - m_S > 8 \text{ GeV}$  region excluded; [Lundström et al., Physical Review D 79 \(2009\)](#)
    - ❑  $m_\chi > 101.2 \text{ GeV}$ . [Achard et al., Physics Letters B 517, 75 \(2001\)](#)
  - Higgs portal coupling:  $10^{-7} \leq |\lambda_{hs}| \leq 10^{-2}$ .
- Color scheme: **all points satisfy B-physics constraints** within  $2\sigma$ . **Cyan points** excluded when considering **DM relic abundance**, within  $2\sigma$  CL. **Blue points** cannot satisfy **DM searches**. **Green points** not allowed by the **muon ( $g - 2$ )** within its  $3\sigma$  range. **Red points** are the common parameter space which **explain all previous constraints**.

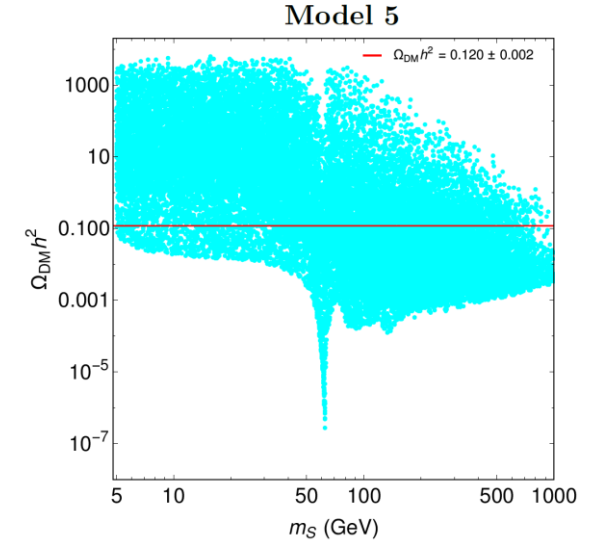
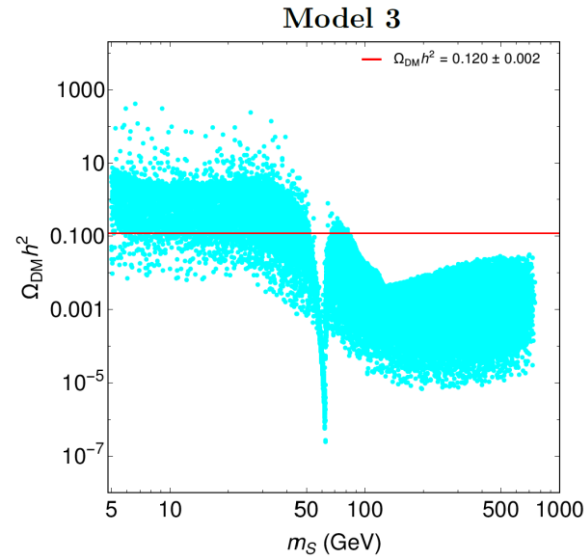


# Results

- In both models, there are regions of the parameter space satisfying all the constraints, but differences exist. The main one is related to the **DM's relic density** distribution, which forces  **$m_S < 80$  GeV for Model 3**. This occurs because in **Model 3**, the scalar fields are **SU(2) doublets** and can couple to gauge bosons, unlike for **Model 5** where they are **singlets**.



**Model 3 only!**



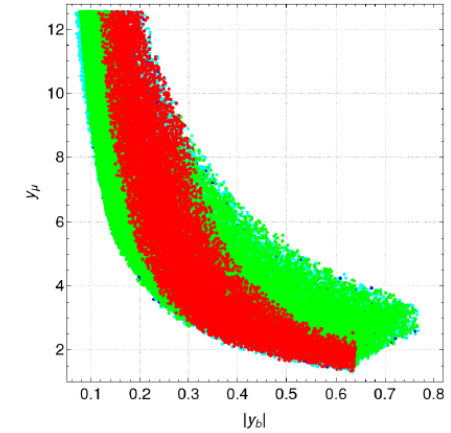
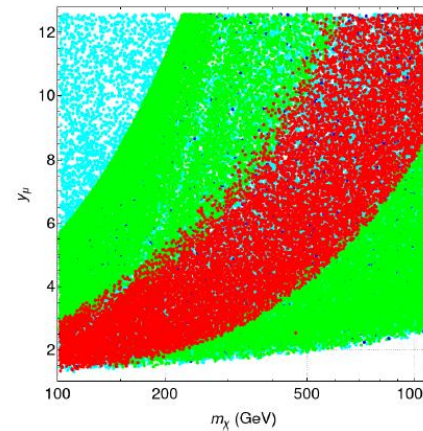
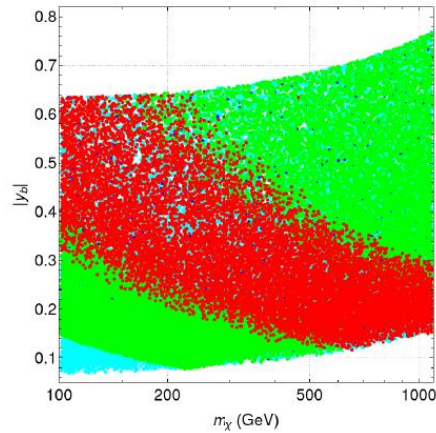
- Some fine-tuning is necessary to keep the **Higgs portal coupling** small enough in Model 3 to verify the direct detection constraints.

$$\lambda_{hS} = \lambda_{12} + \lambda'_{12} + 2\lambda_5 = \lambda_{12} + 2(m_S^2 - m_{\phi_l}^2)/v^2$$

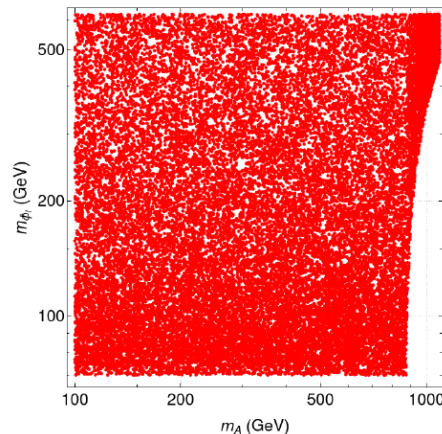
$$\lambda_{12} \approx -2(m_S^2 - m_{\phi_l}^2)/v^2$$

# Results

- **Sizeable Yukawa couplings** with similar limits as the ones in Model 5, as expected since the flavor physics is the same, with  $y_\mu > 1.3$  and  $0.11 < y_b < 0.65$  when all constraints are taken into account.  $m_\chi < 1076$  GeV (maximum allowed value).

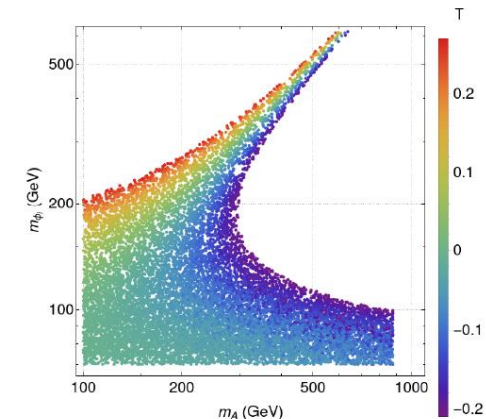


- **Corrections from EW oblique parameters:** upper limit for  $m_A$  slightly lower (1070 GeV to **870 GeV**), and for heavier masses ( $m_{\phi_l} > 200$  GeV and  $m_A > 300$  GeV), a significant part of the previously allowed parameter space is now excluded.



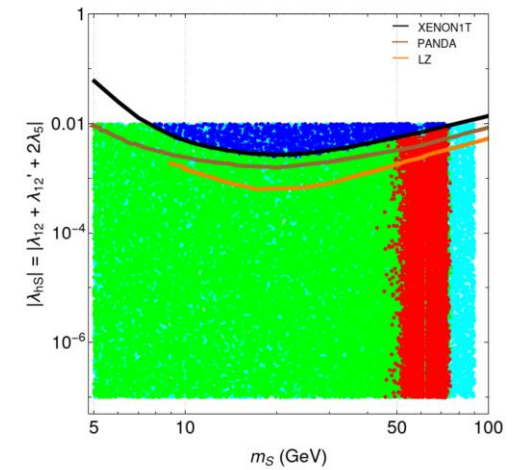
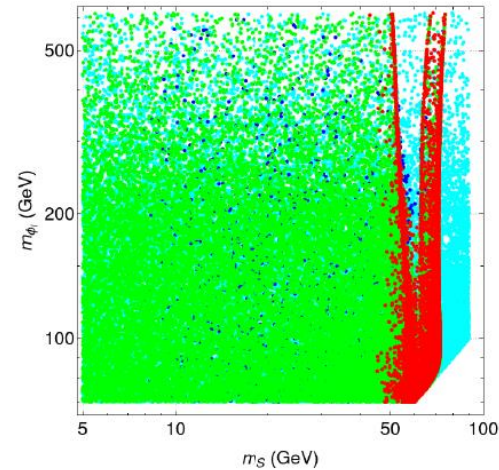
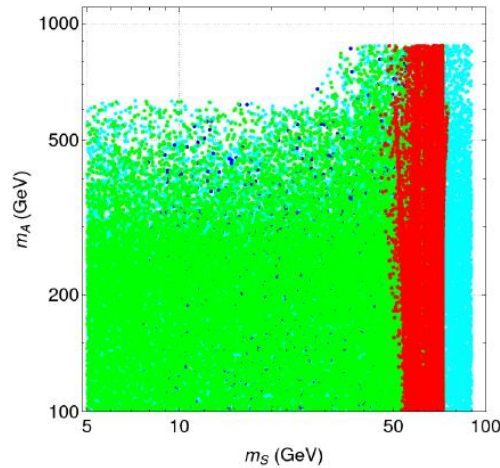
$$T \propto (m_{\phi_l} - m_A)(m_{\phi_l} - m_S)$$

EW constraints



# Results

- For the **DM mass**, we have  **$42 \text{ GeV} < m_s < 76 \text{ GeV}$**  (in **Model 5**,  **$30 \text{ GeV} < m_s < 350 \text{ GeV}$** ), thus, the DM mass is limited in a very narrow range in Model 3, while for Model 5 its range is much broader. For the remaining parameters we observe  **$|\lambda_{hs}| \leq 0.008$** , and  **$m_{\phi_l} < 621 \text{ GeV}$** . The constraint on  $m_{\phi_l}$  keeps  $\lambda_{12} < 4\pi$ .



# Conclusions

- A model with a new dark sector which provides a **DM candidate** and is able to solve some discrepancies in **B meson decays** and the **muon (g-2)** was explored (Model 3) and compared to a previously studied model (Model 5).
- **Both models have regions satisfying all the constraints.** The **contributions to the flavor observables and the muon (g-2) do not change** since the vertices contributing to the loop processes are the same.
- However, there are **differences** in the allowed parameter space **related to DM physics**. The main one is due to the **DM relic density constraint**, which sets an **upper limit of 80 GeV for the DM mass** in **Model 3**. In Model 5, the DM mass range is much broader. This occurs because of the **different SU(2) representations** of the models.

THE END.  
THANK YOU!

# Direct Detection vs Collider Searches

