

# CLASSICAL SCALE INVARIANCE AS A SOURCE OF MASSES, DARK MATTER AND GRAVITATIONAL WAVES

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*Bogumiła Świeżewska*  
*University of Warsaw*

*in collaboration with*  
*Maciej Kierkla and Alexandros Karam,*

*based on*  
*arXiv:22xx.xxxx*

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*Workshop on Multi-Higgs Models, 31.08.2022*

# IN MEMORY OF PROFESSOR MARIA KRAWCZYK

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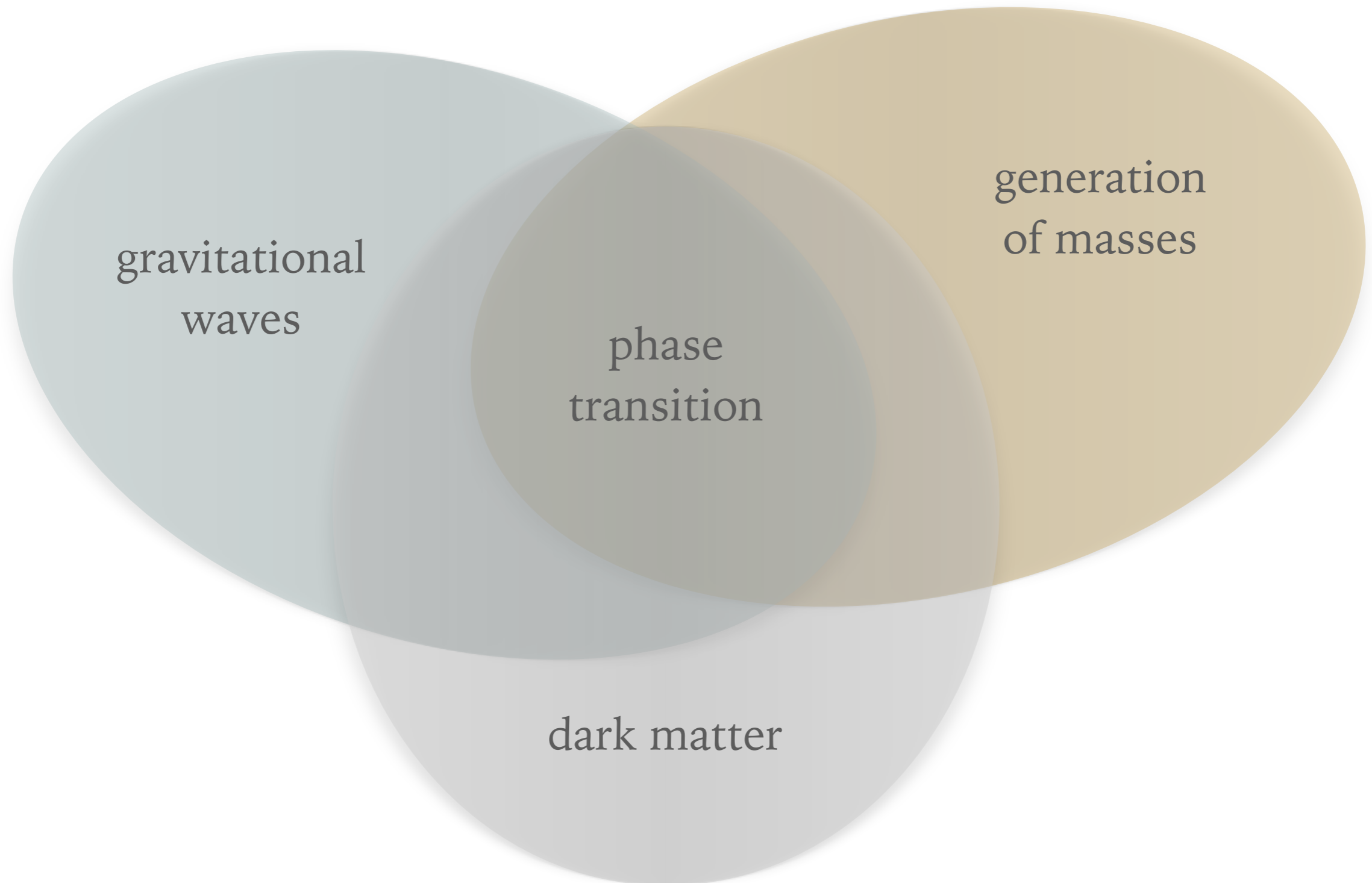


# MOTIVATION

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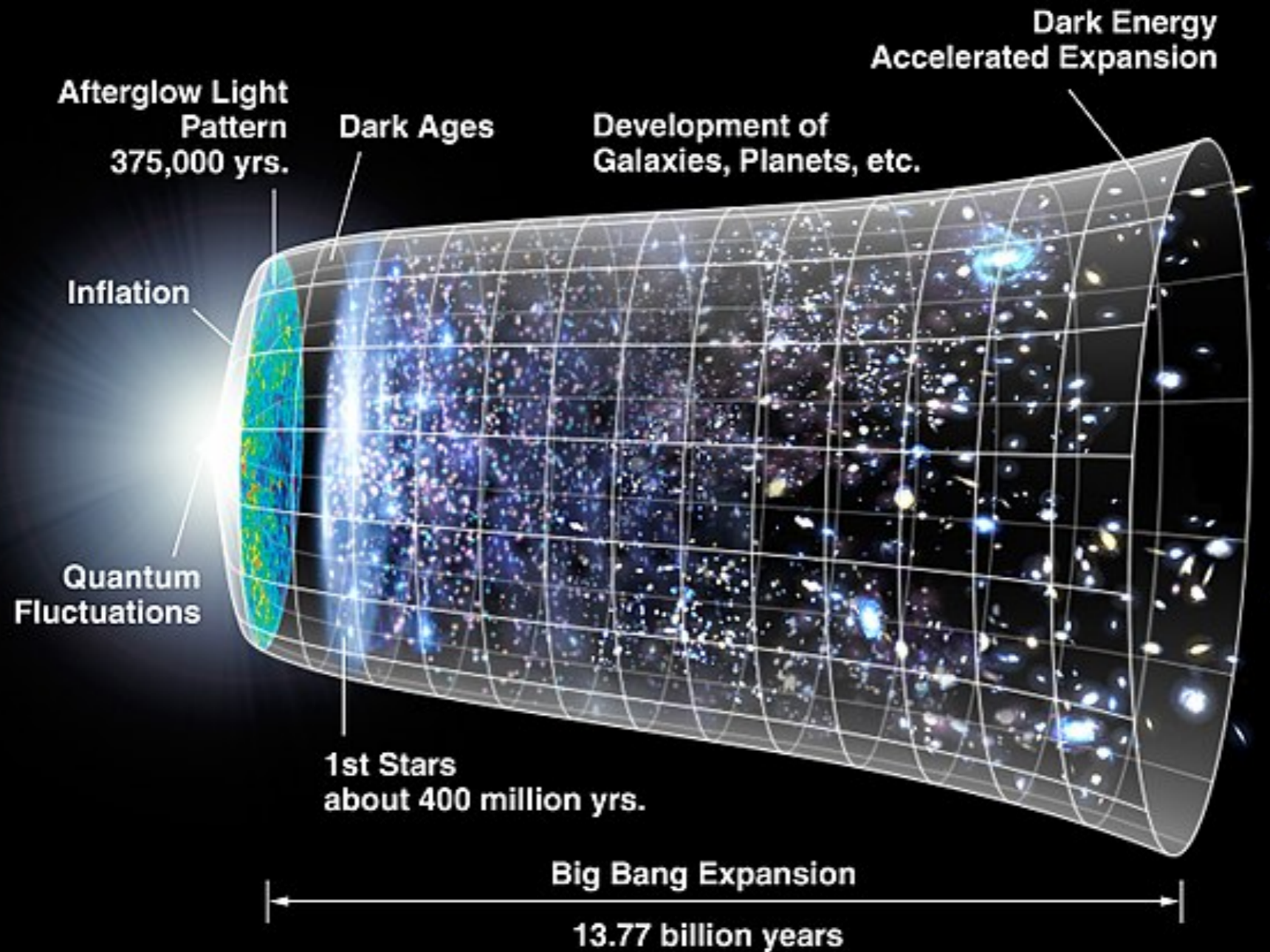
# PT - A LINK BETWEEN DIFFERENT OBSERVABLES

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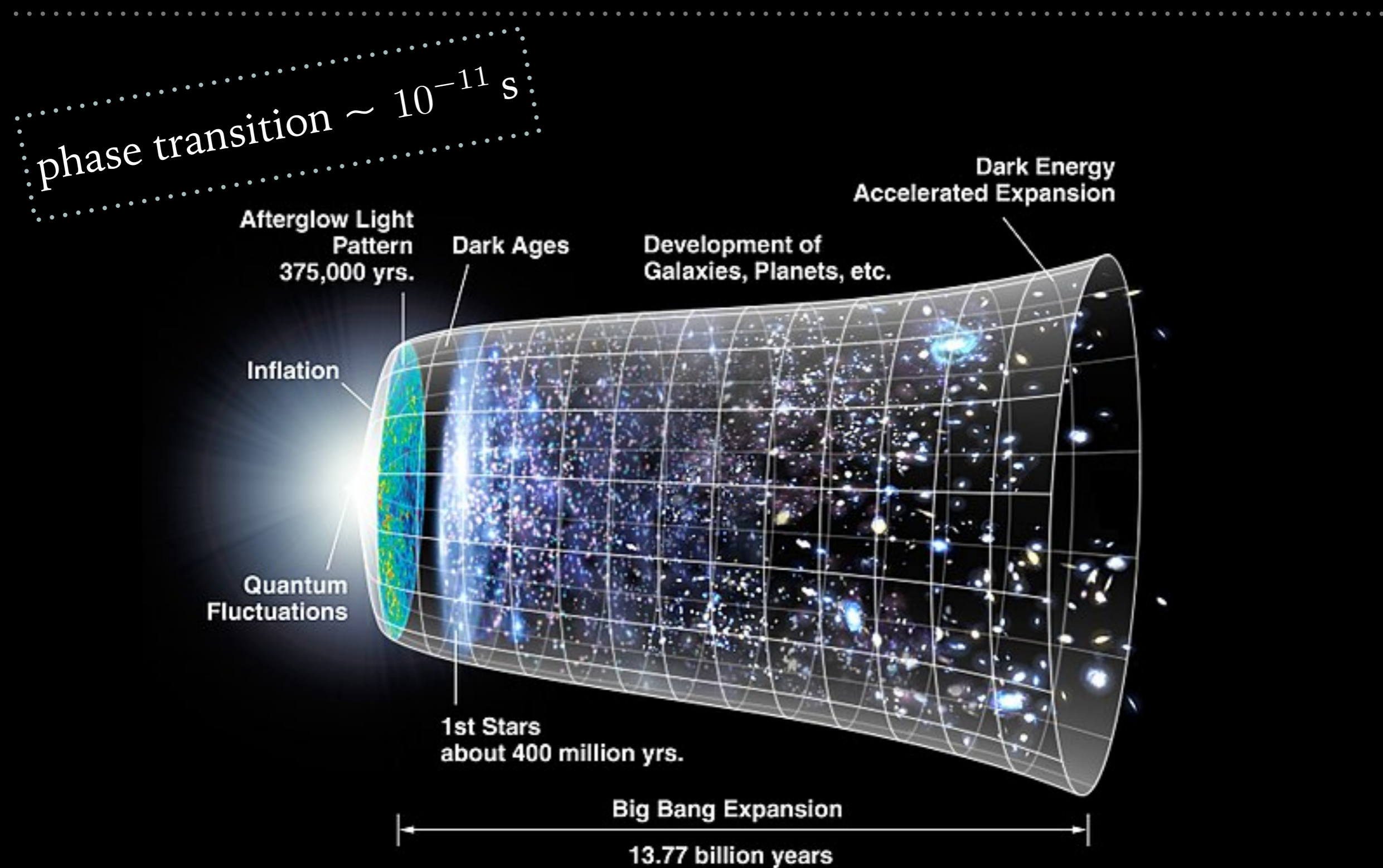


# OBSERVING CHILDHOOD OF THE UNIVERSE?

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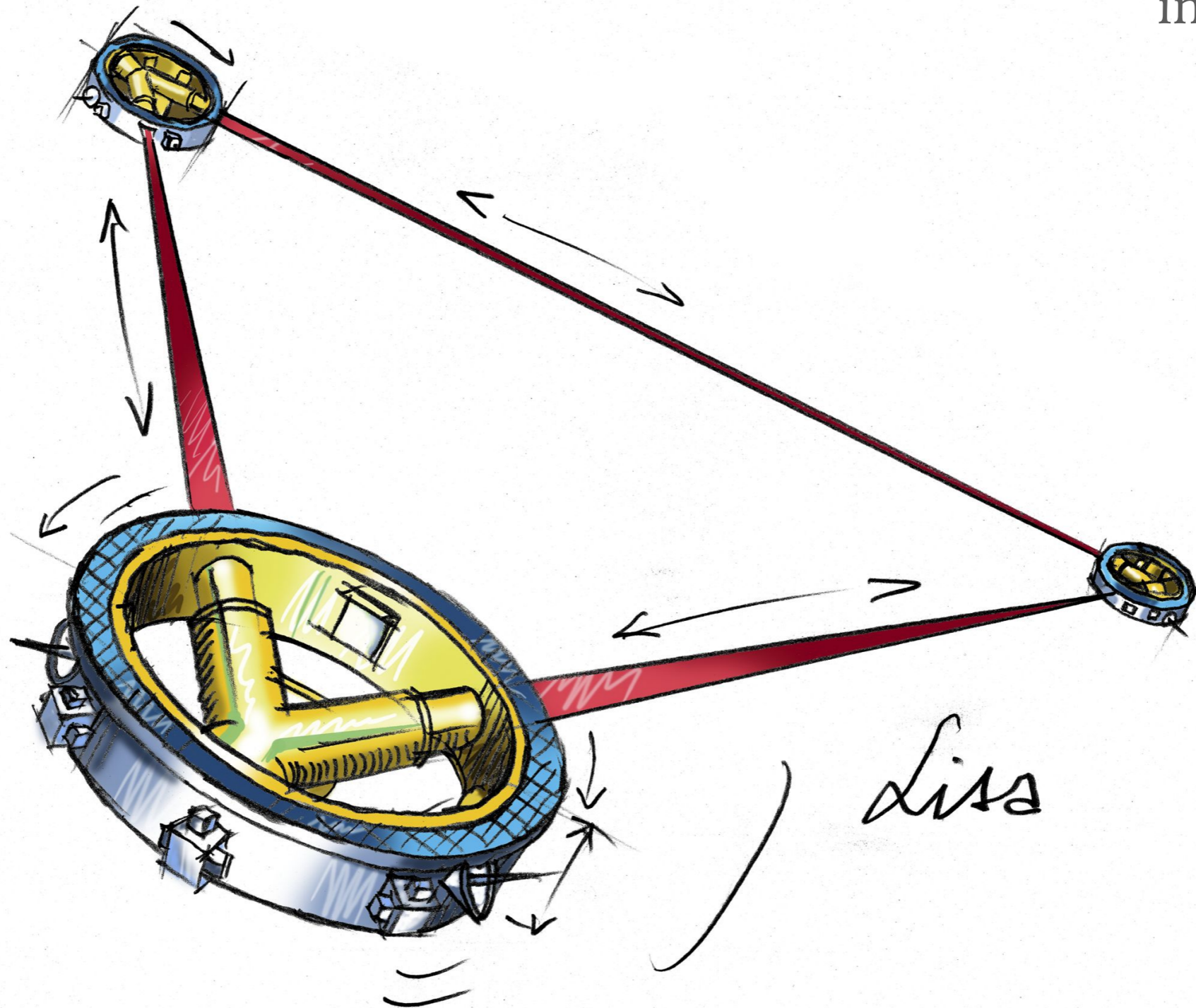


# OBSERVING CHILDHOOD OF THE UNIVERSE?



# LISA IS COMING!

in the 2030's



[Image credit: ESA-C. Vijoux]

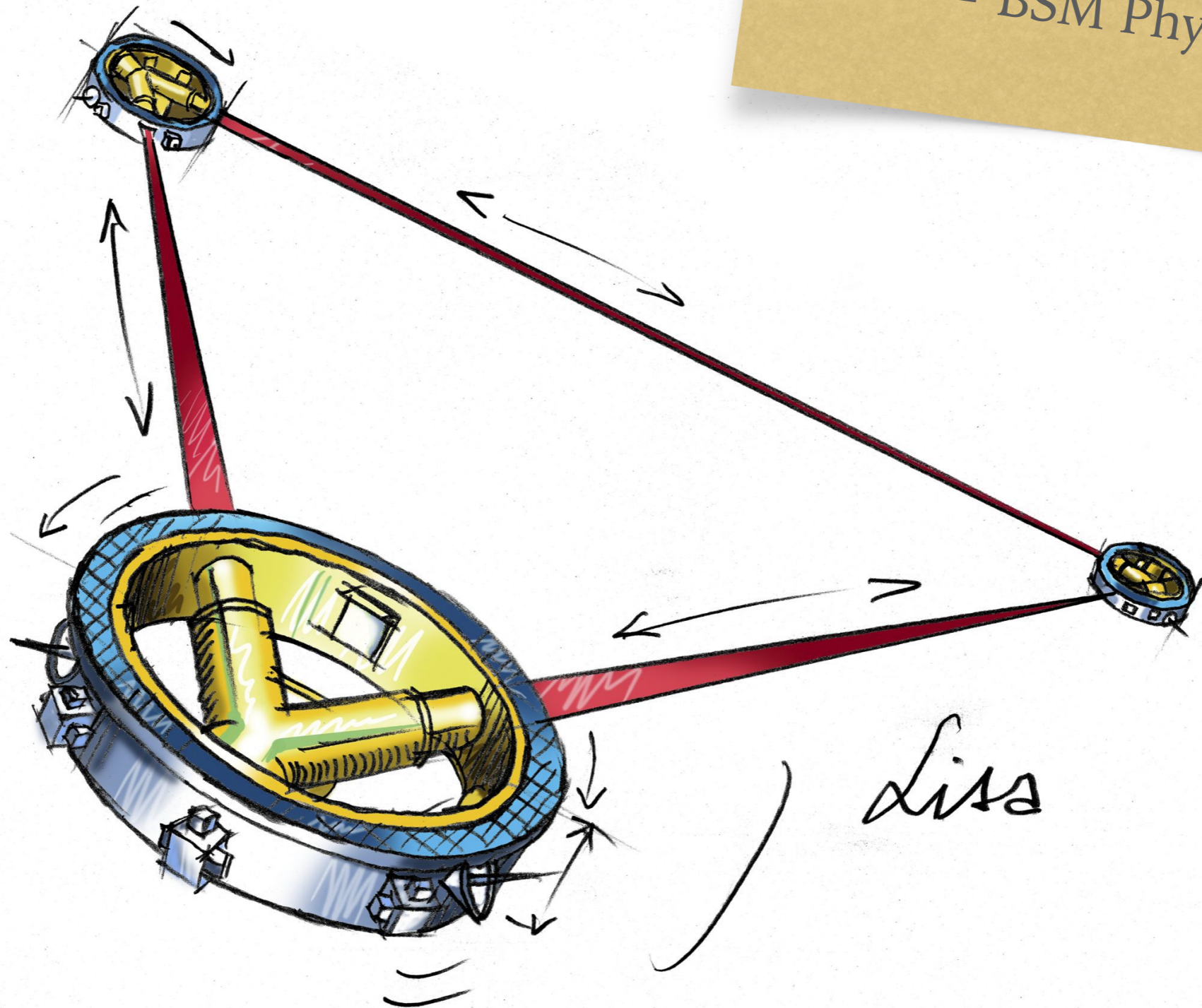
Bogumiła Świeżewska

Classical scale invariance: DM and RG

# LISA IS COMING!

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First-order phase transition  
= BSM Physics!



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[Image credit: ESA-C. Vijoux]



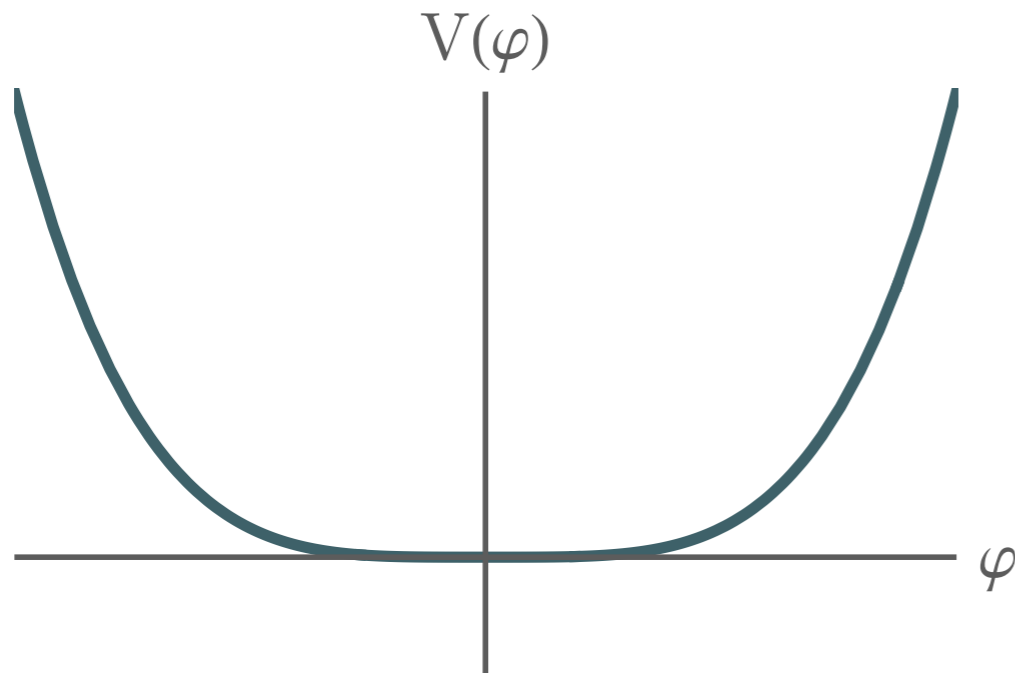
# CLASSICAL CONFORMAL SYMMETRY

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# CLASSICAL CONFORMAL SYMMETRY

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No dimensionful parameters at tree level



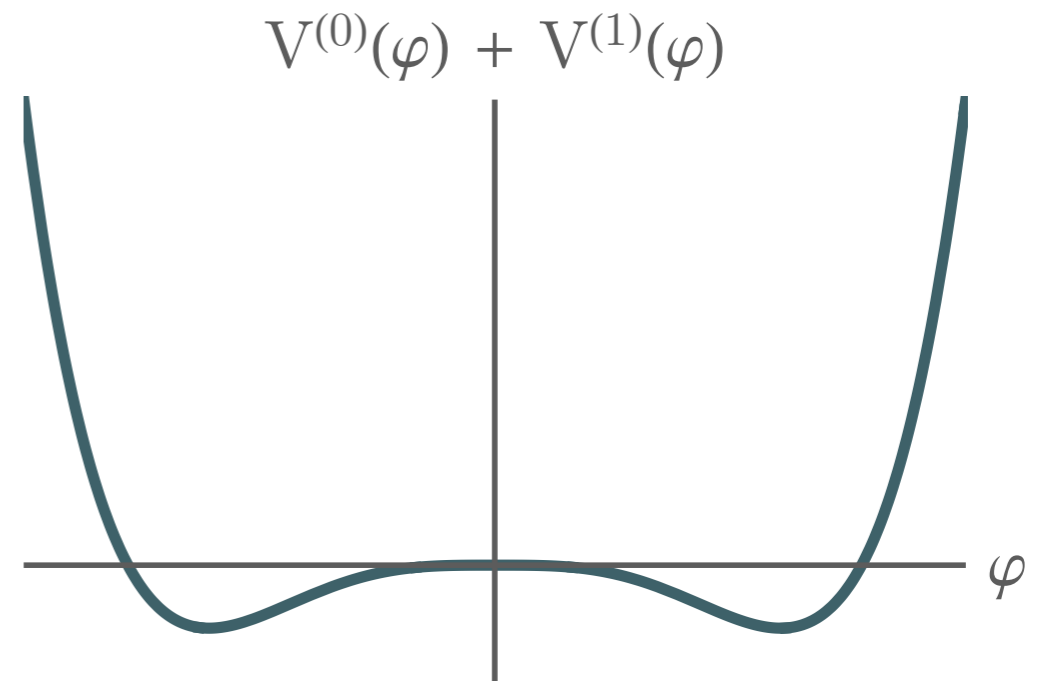
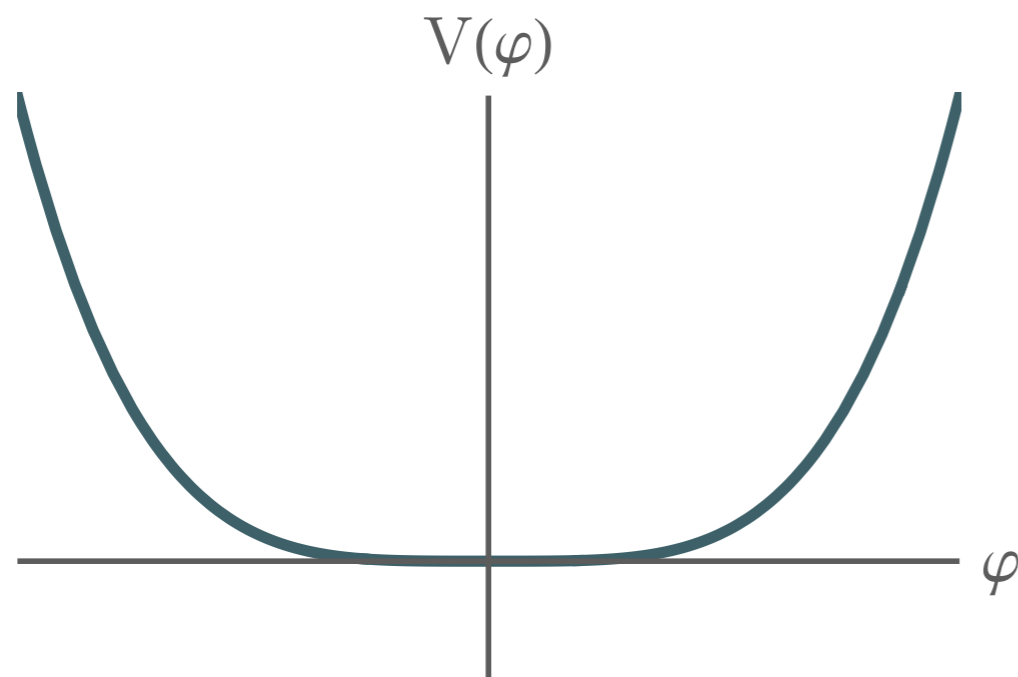
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[S. R. Coleman, E. J. Weinberg, *Phys.Rev. D7* (1973) 1888]

# CLASSICAL CONFORMAL SYMMETRY

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No dimensionful parameters at tree level



Symmetry broken by loop corrections (dimensional transmutation)

[S. R. Coleman, E. J. Weinberg, *Phys.Rev. D7* (1973) 1888]

# WHY CLASSICAL CONFORMAL SYMMETRY?

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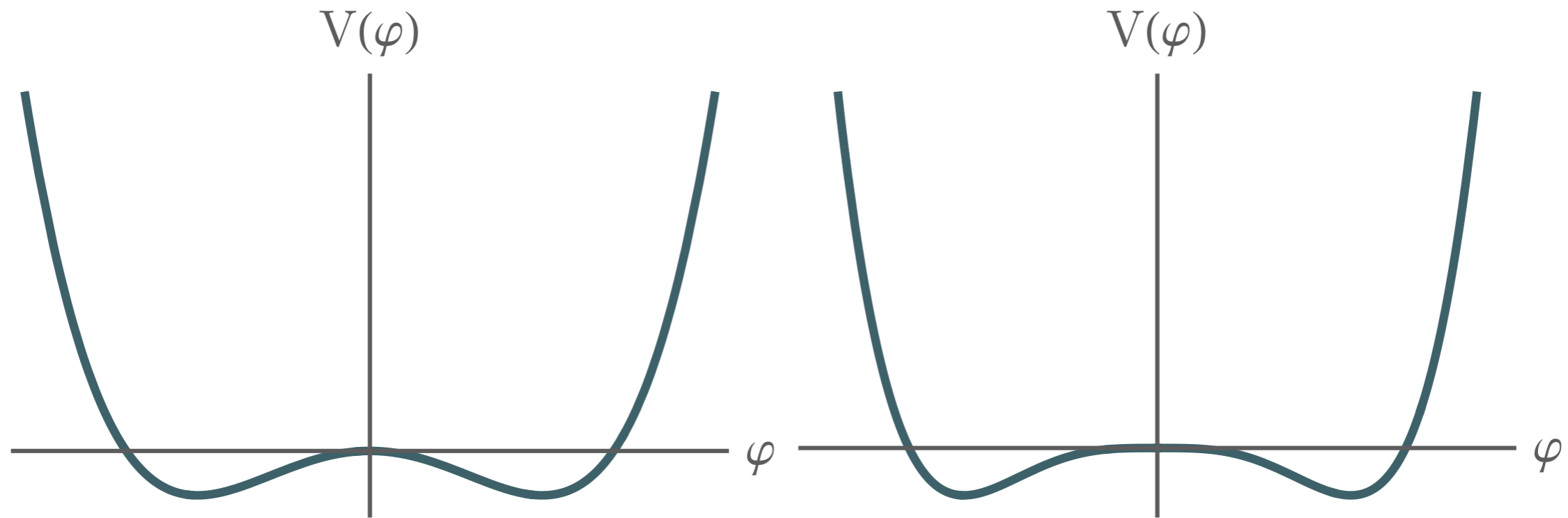
dynamical  
generation of all  
mass scales

predictivity -  
few free  
parameters

Generically strong  
GW signal testable  
with LISA

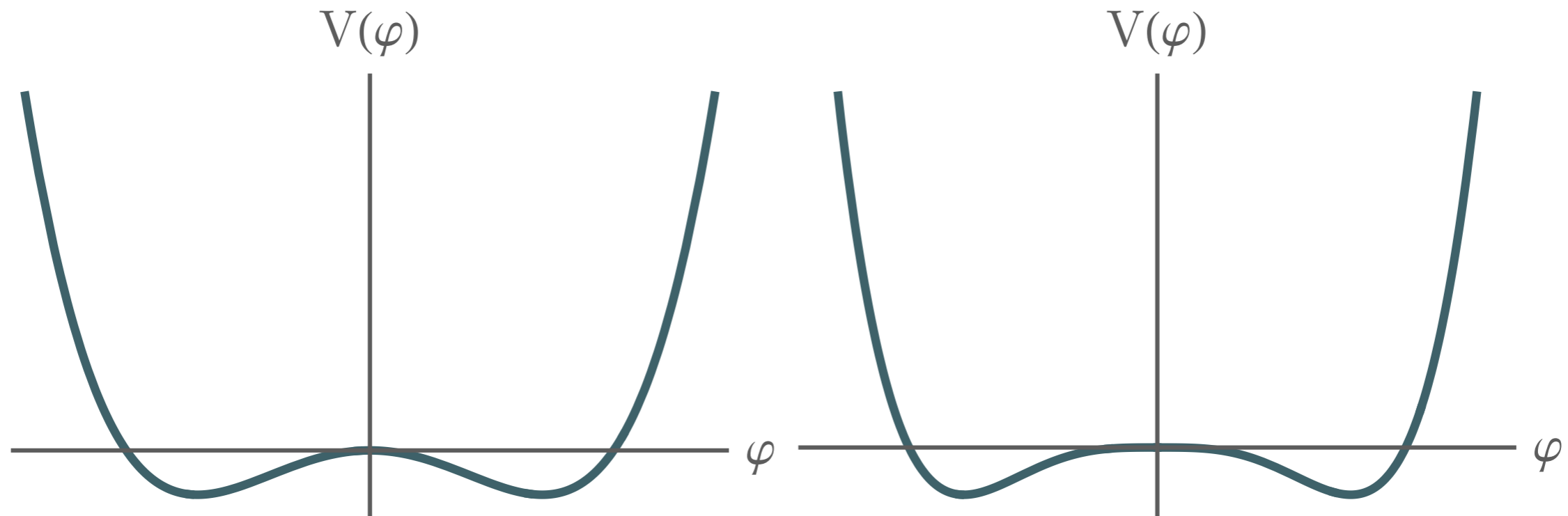
# CONFORMAL VS "NORMAL" POTENTIAL

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# CONFORMAL VS “NORMAL” POTENTIAL

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The thermal barrier can last until low temperatures  
↓  
Potential for supercooling and strong transition

# SU(2)CSM

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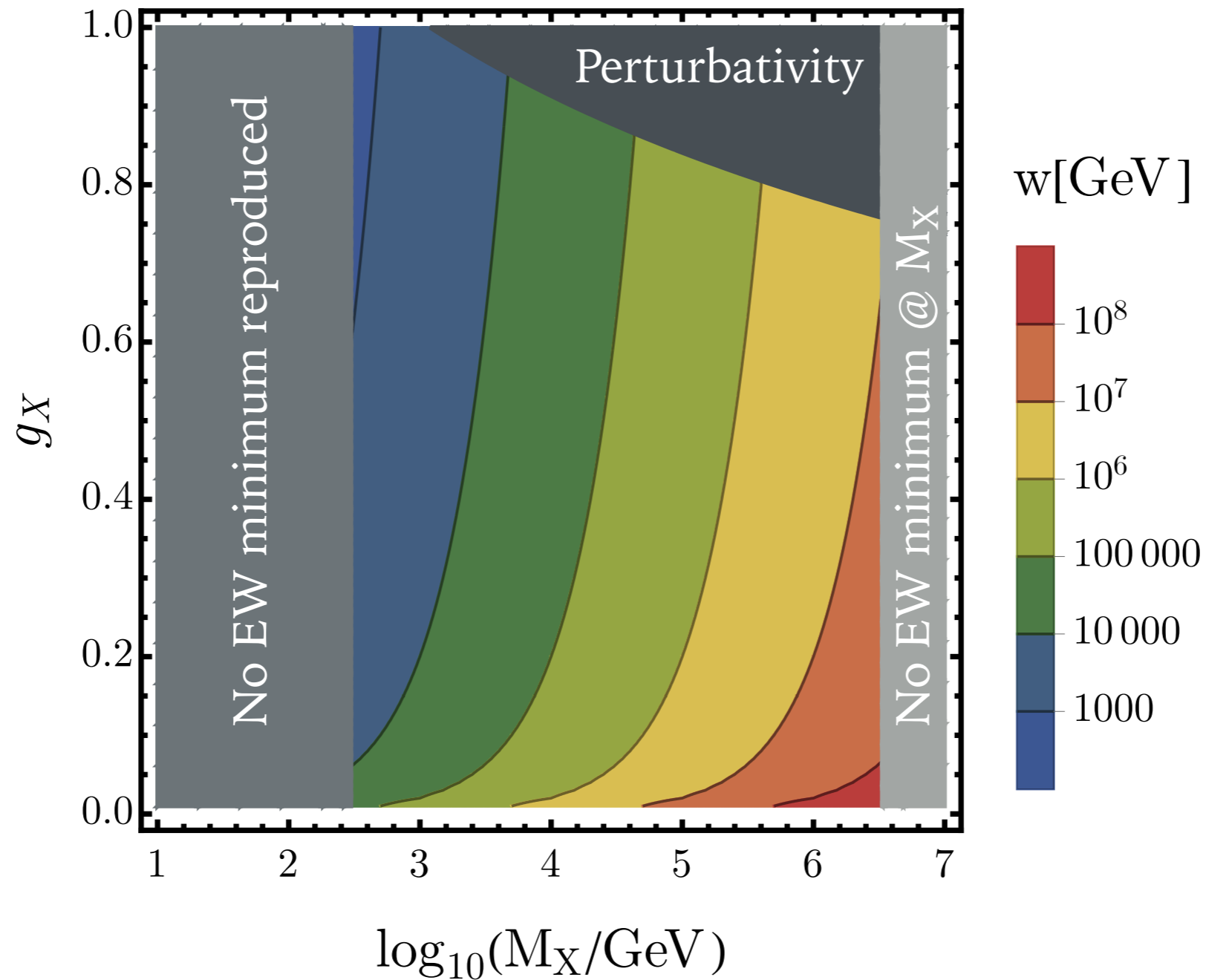


$$V^{(0)}(\Phi, \Psi) = \lambda_1 (\Phi^\dagger \Phi)^2 + \lambda_2 (\Phi^\dagger \Phi) (\Psi^\dagger \Psi) + \lambda_3 (\Psi^\dagger \Psi)^2,$$

[See also: T.Hambye, A.Strumia, PRD88 (2013) 055022, C.Carone, R.Ramos, PRD88 (2013) 055020, V.V.Khoze, C.McCabe, G.Ro, JHEP 08 (2014) 026, T. Hambye, A.Strumia, D.Teresi, JHEP 1808 (2018) 188, I.Baldes, C. Garcia-Cely, JHEP 05 (2019) 190, T.Prokopec, J.Rezacek, BS, JCAP02(2019)009, D. Marfaria, P. Tseng, JHEP 02 (2021) 022]

# RADIATIVE SYMMETRY BREAKING IN SU(2)CSM

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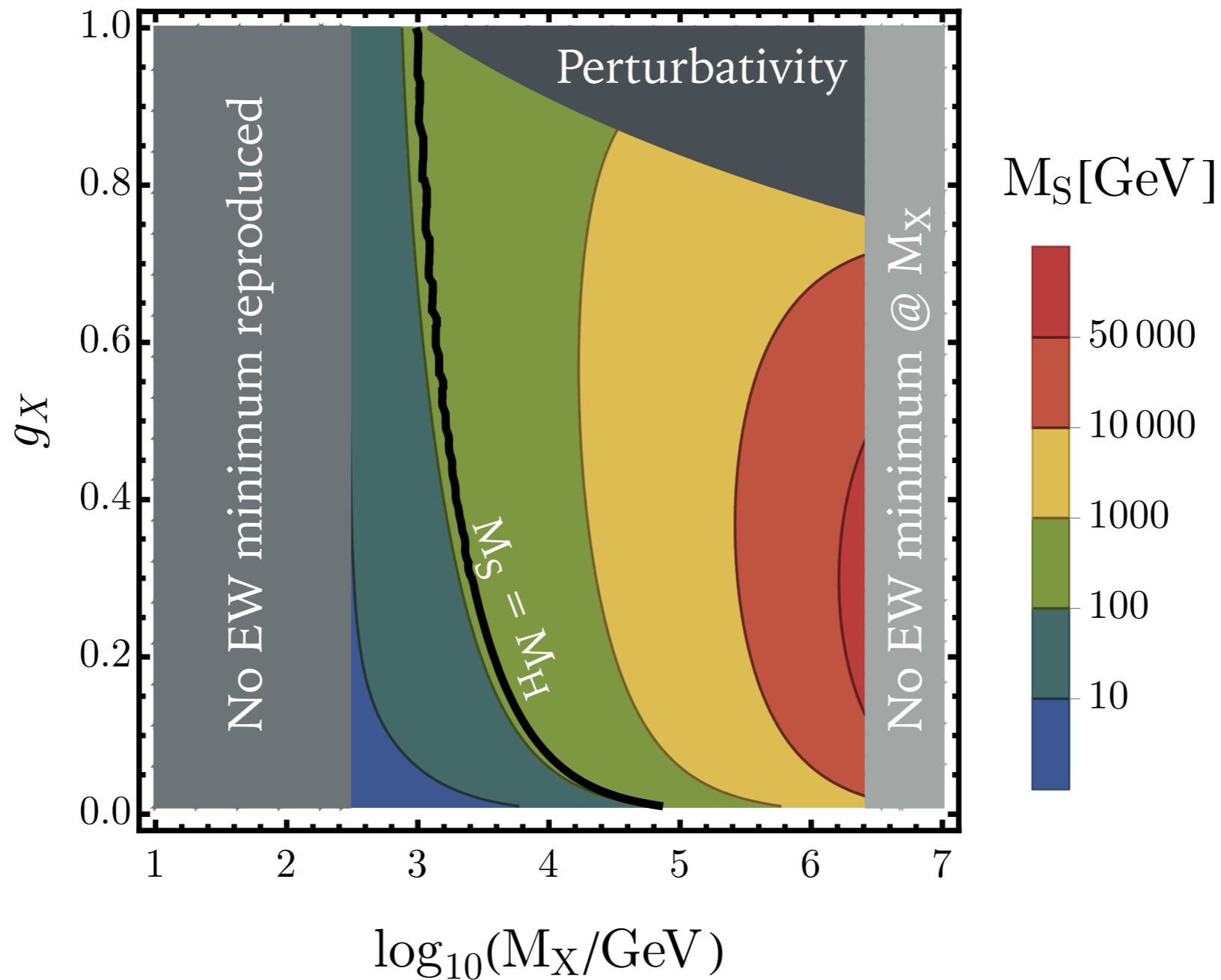
[See also: L. Chataignier, T. Prokopec, M.G. Schmidt, BS, JHEP 08 (2018) 083]

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# RADIATIVE SYMMETRY BREAKING IN SU(2)CSM

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[See also: L. Chataignier, T. Prokopec, M.G. Schmidt, BS, JHEP 08 (2018) 083]

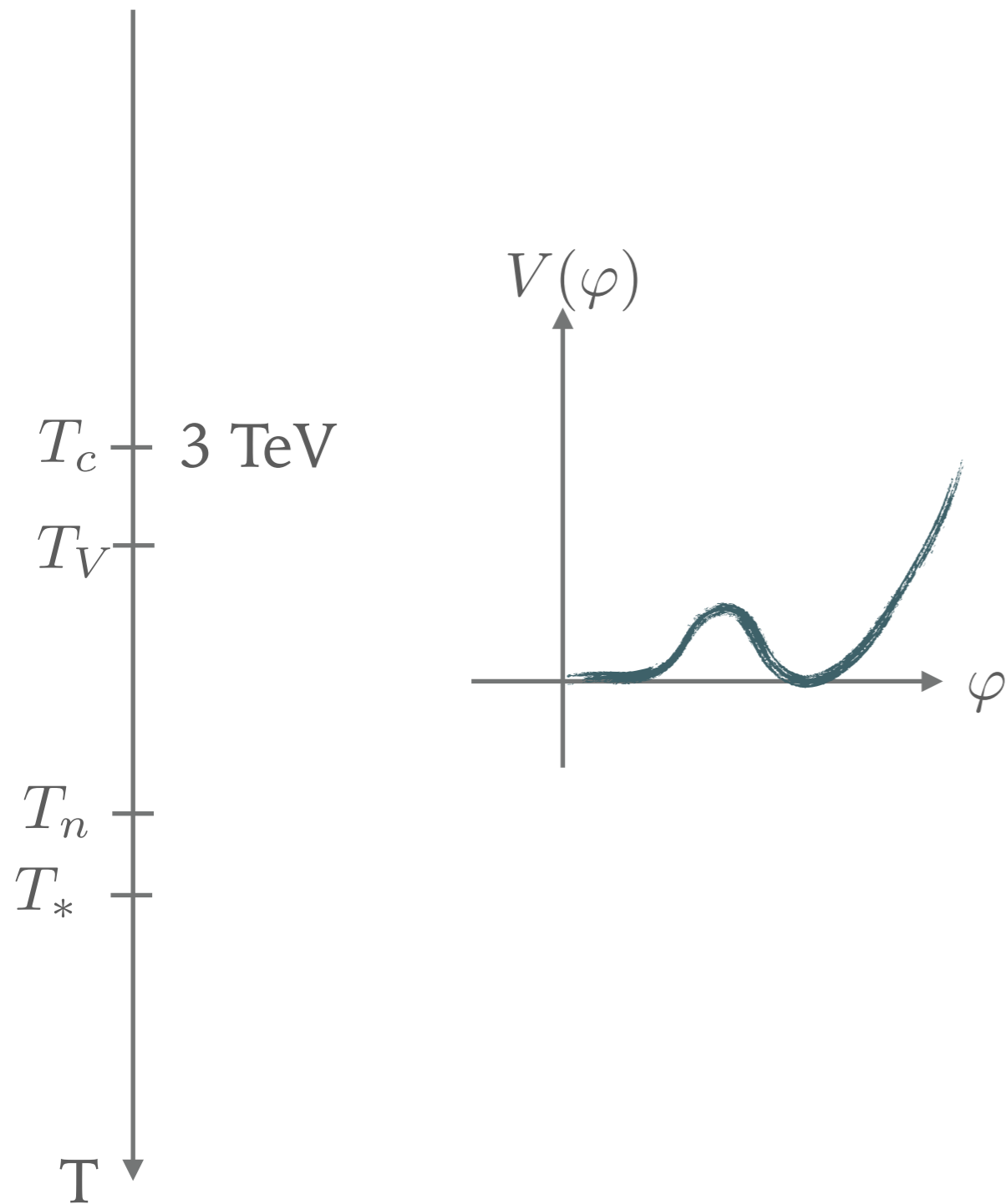
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# PHASE TRANSITION AND GRAVITATIONAL WAVES

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# TEMPERATURE EVOLUTION

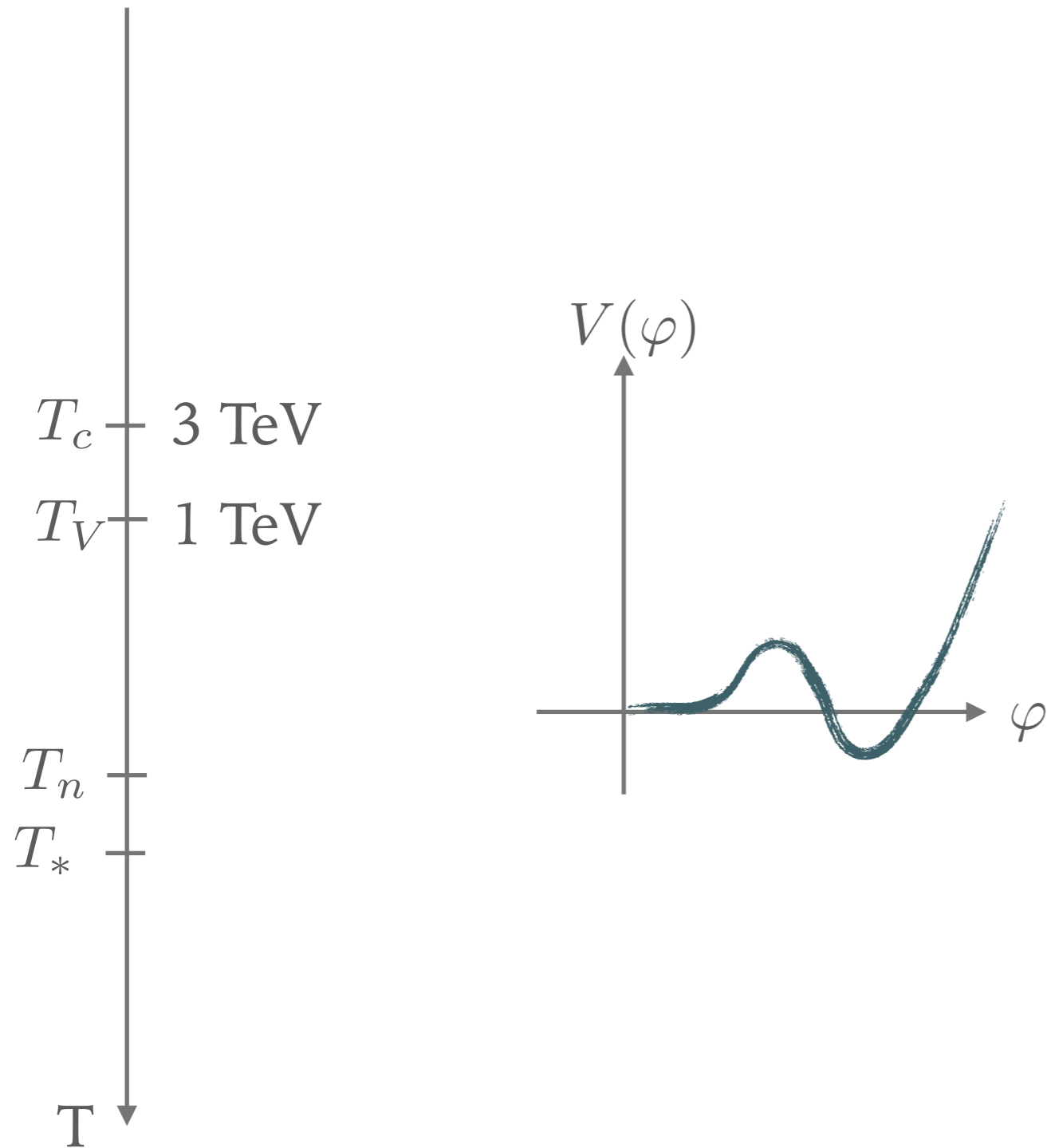
$$M_X = 9 \text{ TeV}, g_X = 0.9$$



critical temperature:  
two degenerate  
minima

# TEMPERATURE EVOLUTION

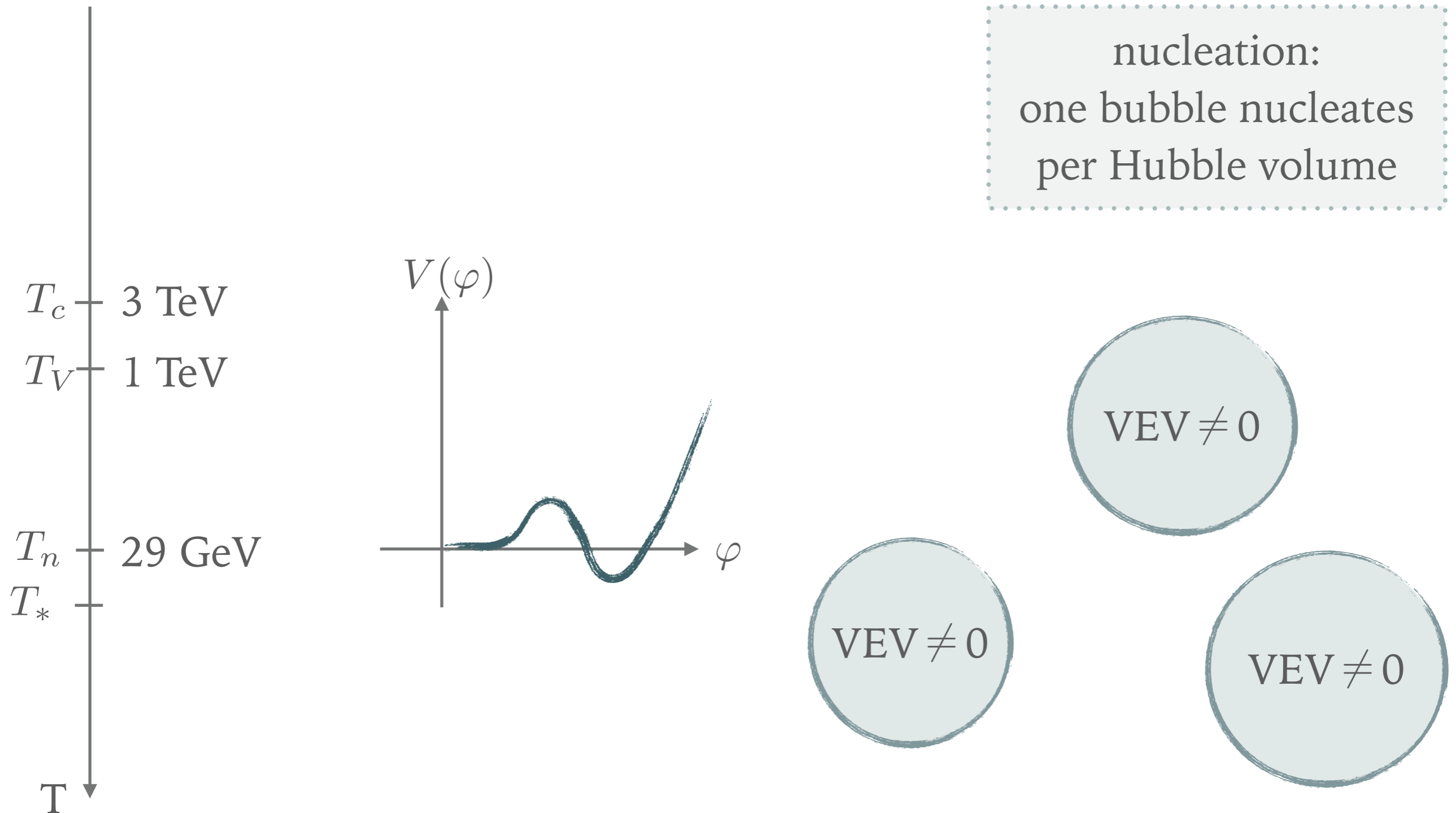
$$M_X = 9 \text{ TeV}, g_X = 0.9$$



vacuum domination  
begins

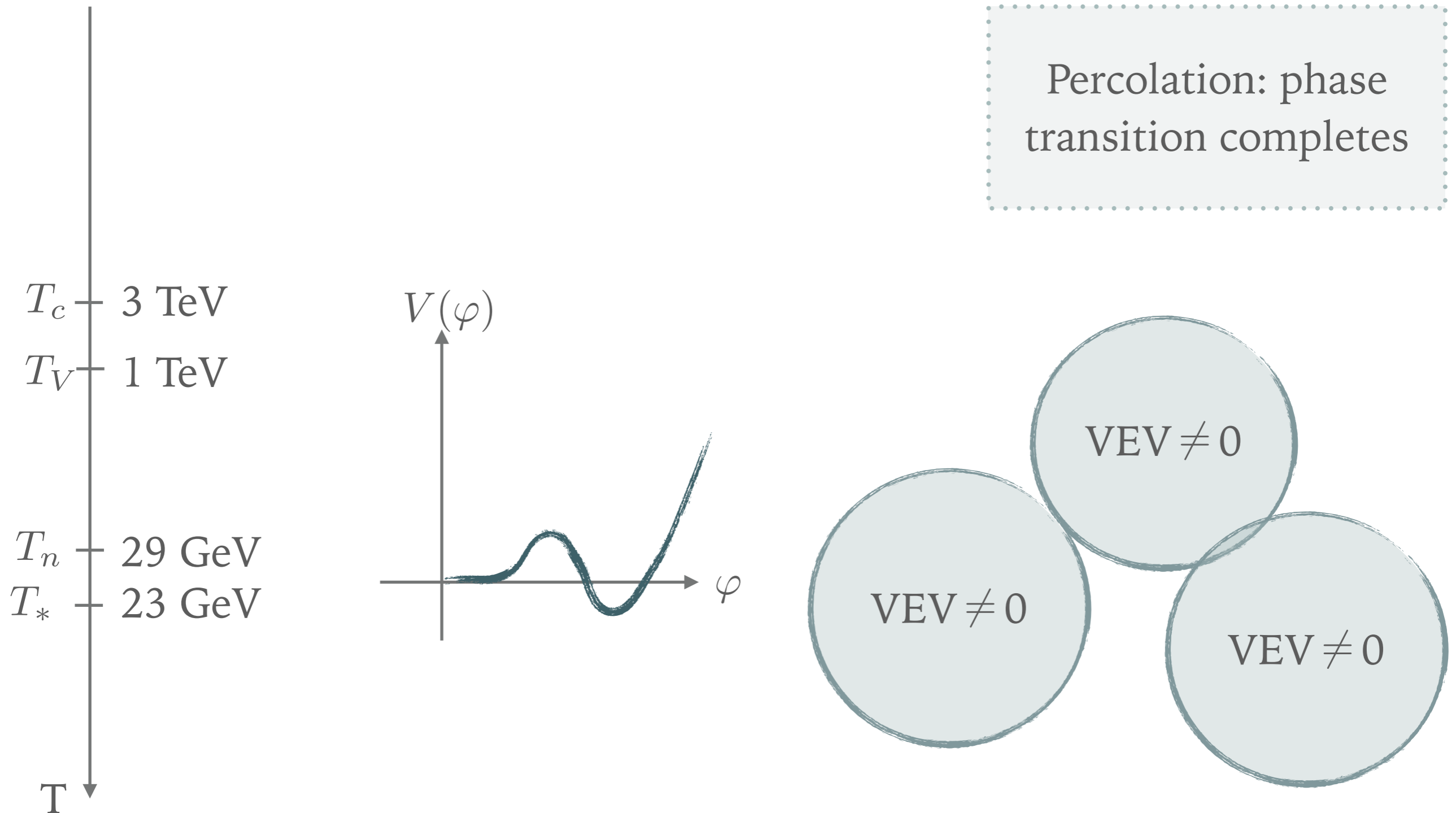
# TEMPERATURE EVOLUTION

$$M_X = 9 \text{ TeV}, g_X = 0.9$$



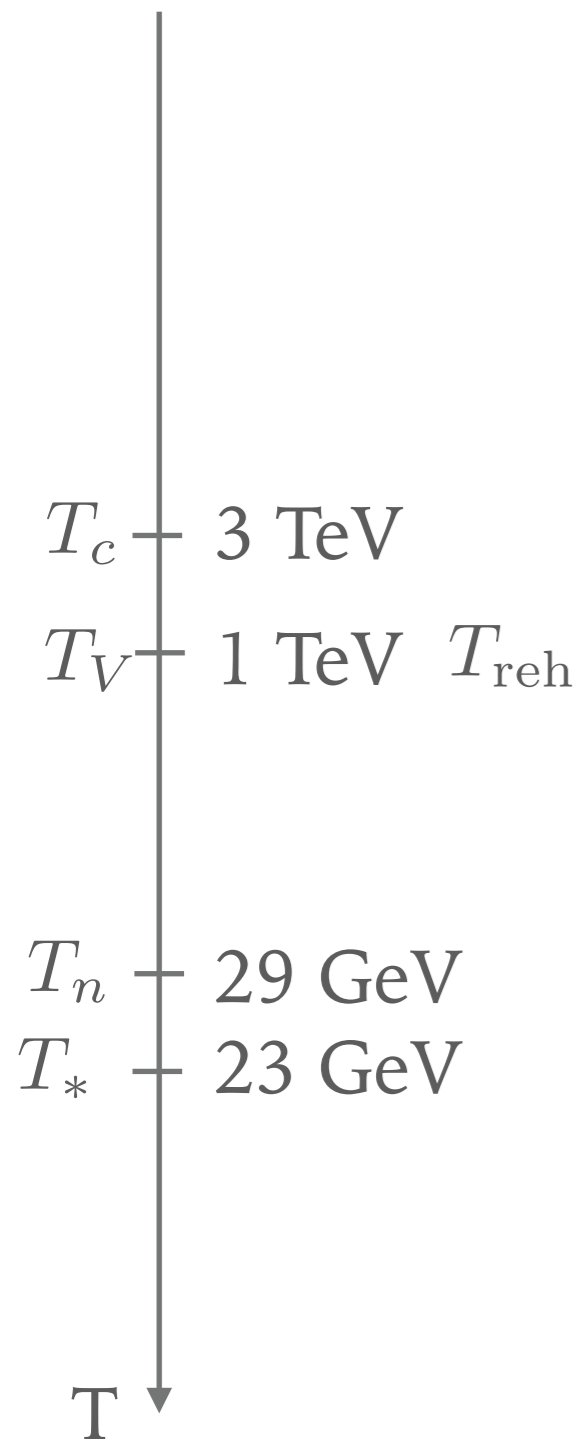
# TEMPERATURE EVOLUTION

$$M_X = 9 \text{ TeV}, g_X = 0.9$$



# TEMPERATURE EVOLUTION

$$M_X = 9 \text{ TeV}, g_X = 0.9$$

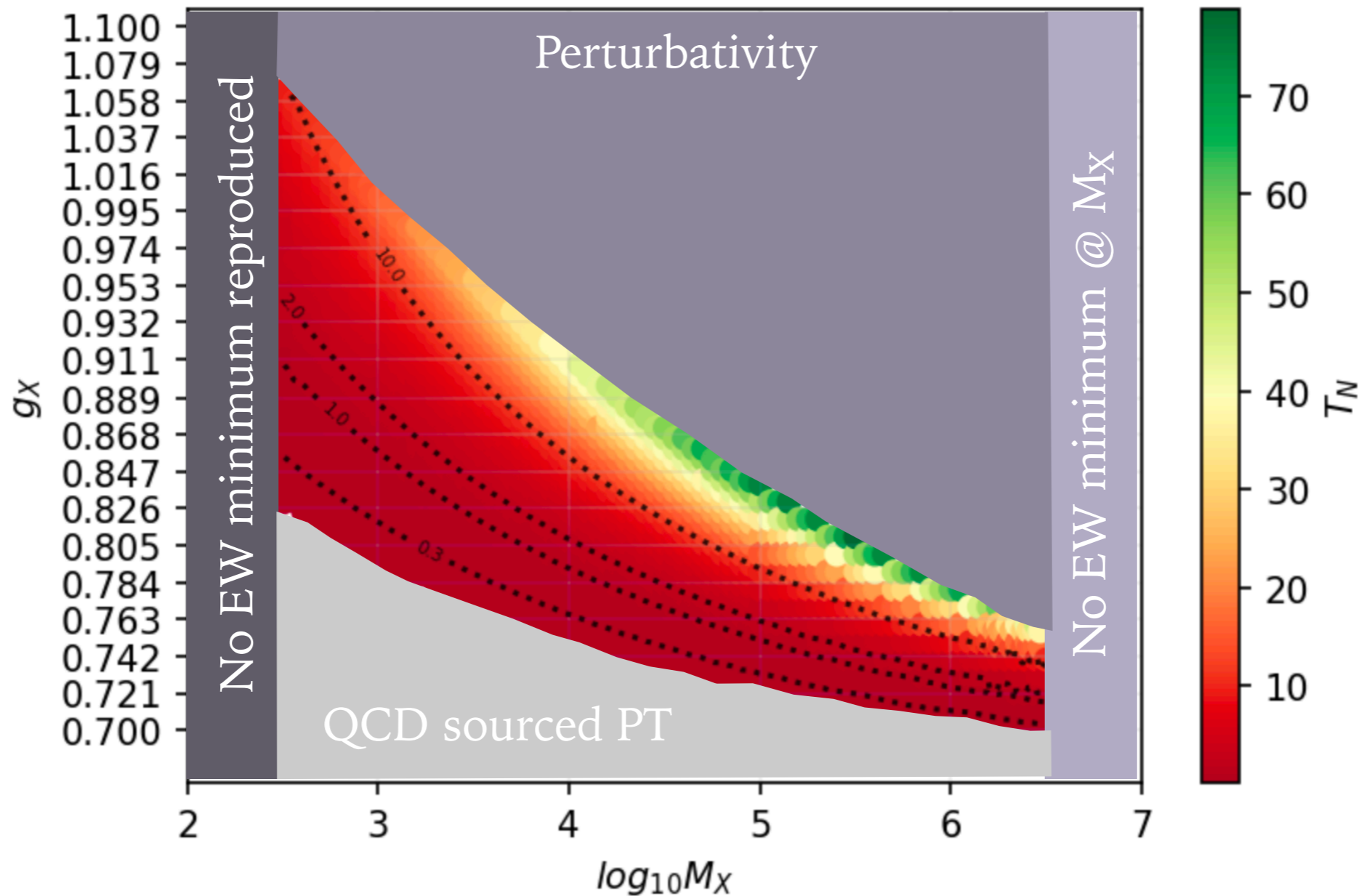


reheating

$$\alpha = \frac{\Delta V}{\text{energy of radiation}} \approx 4 \cdot 10^6$$

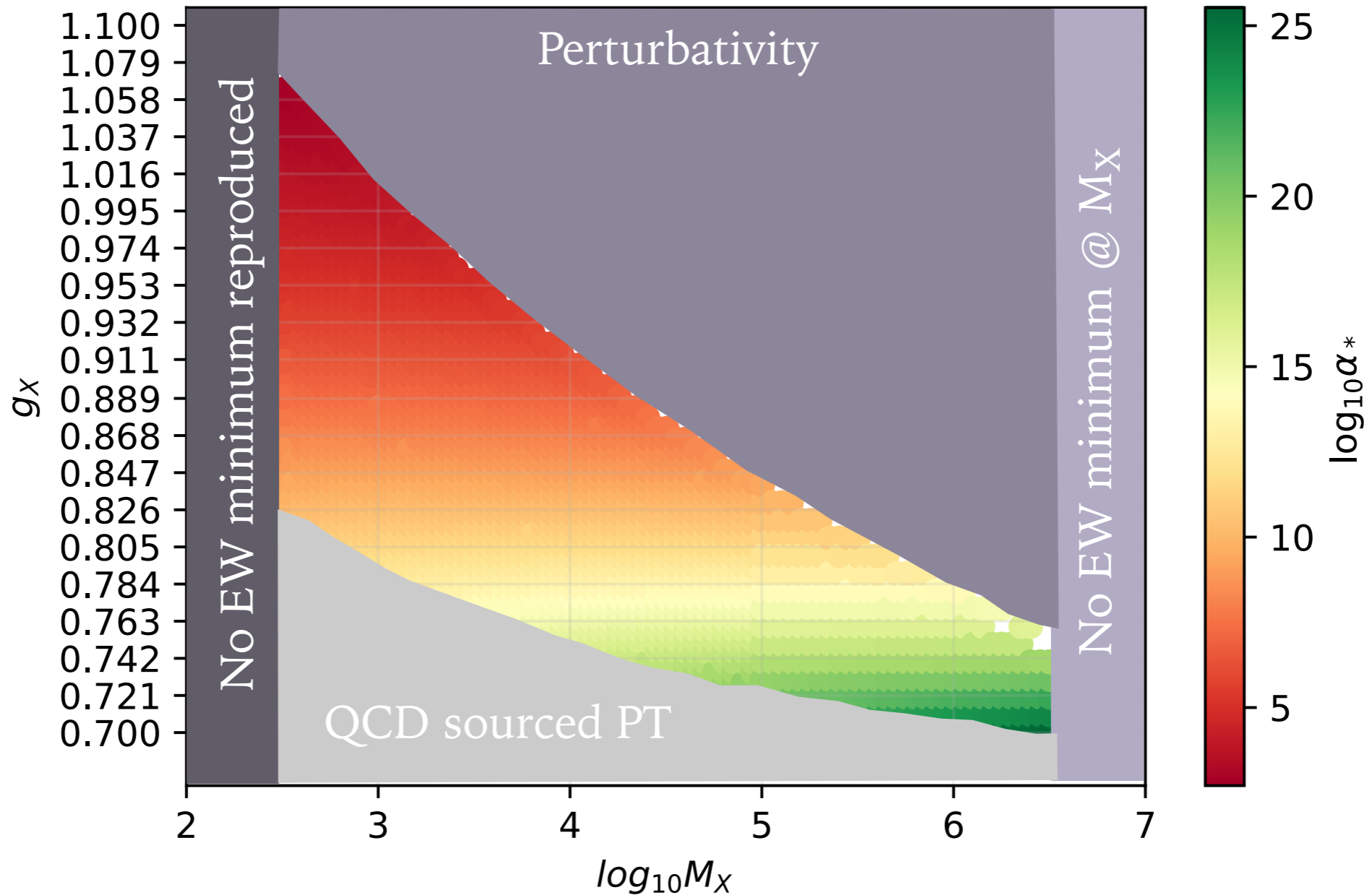
# SCANNING THE PARAMETER SPACE

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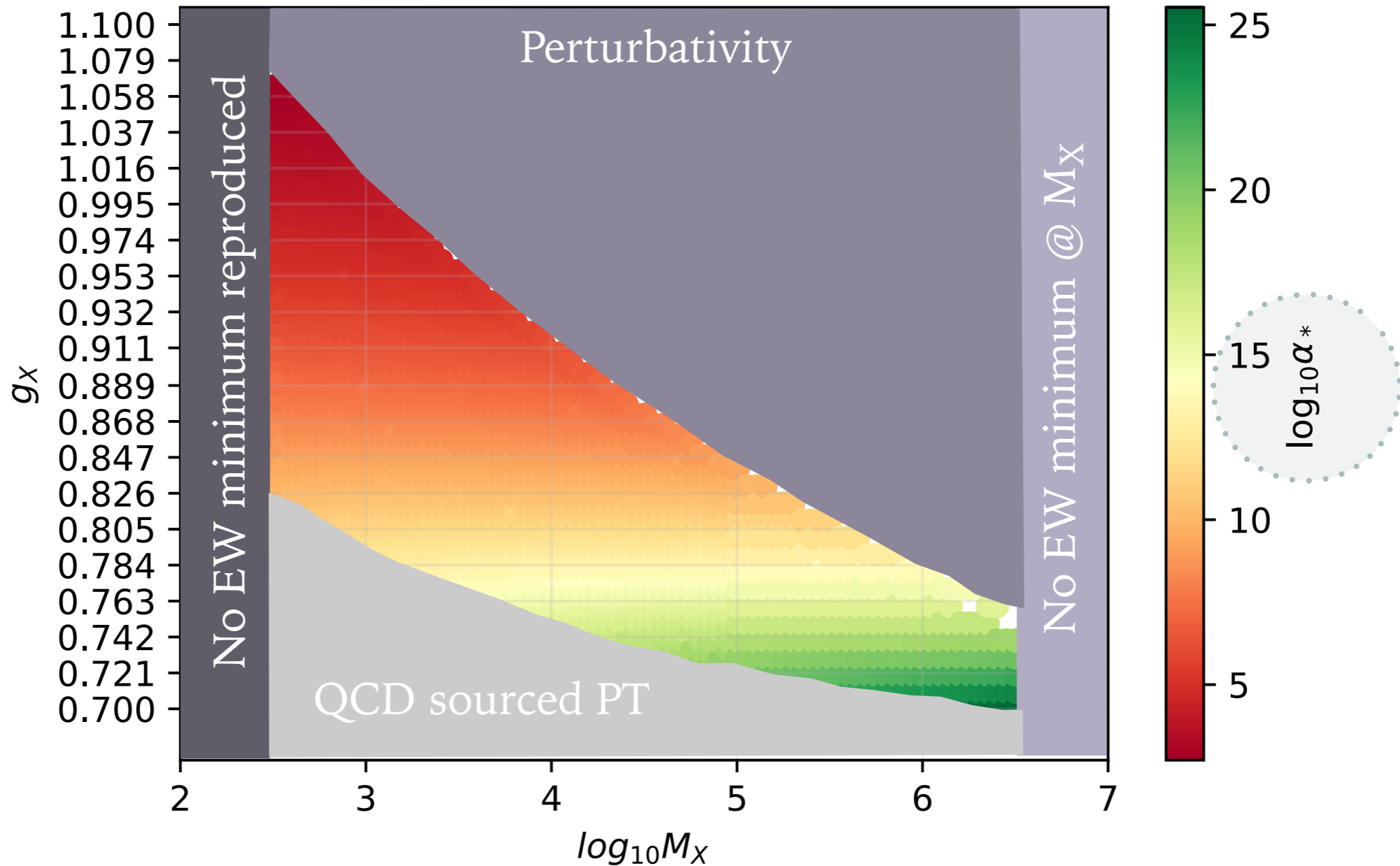




# SCANNING THE PARAMETER SPACE

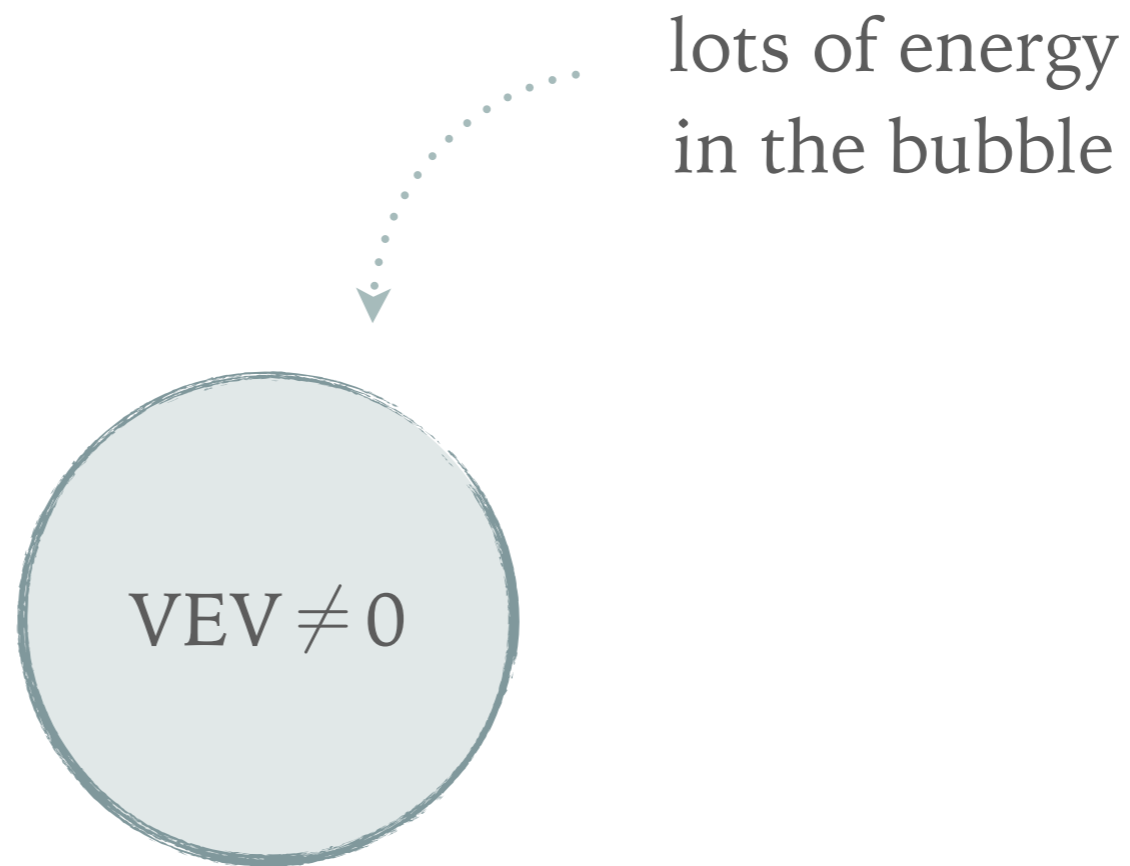


# SCANNING THE PARAMETER SPACE



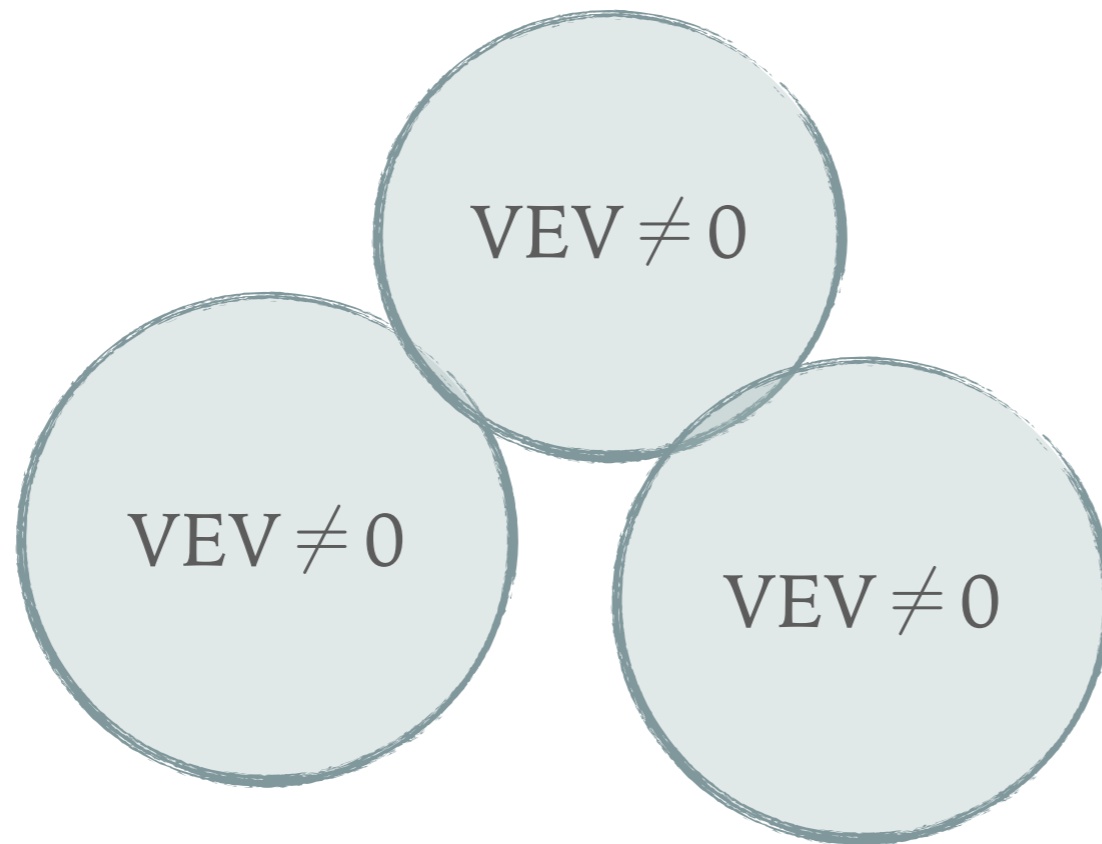
# SOURCES OF GRAVITATIONAL WAVES

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# SOURCES OF GRAVITATIONAL WAVES

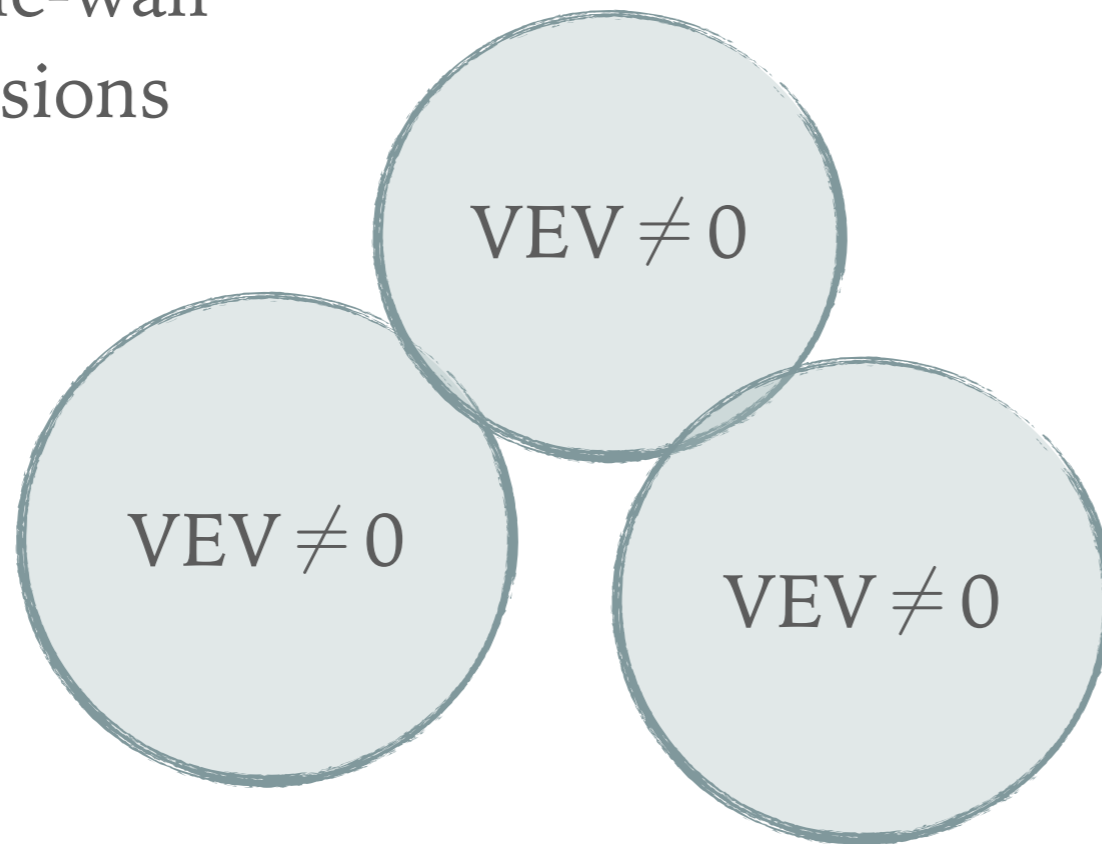
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# SOURCES OF GRAVITATIONAL WAVES

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bubble-wall  
collisions

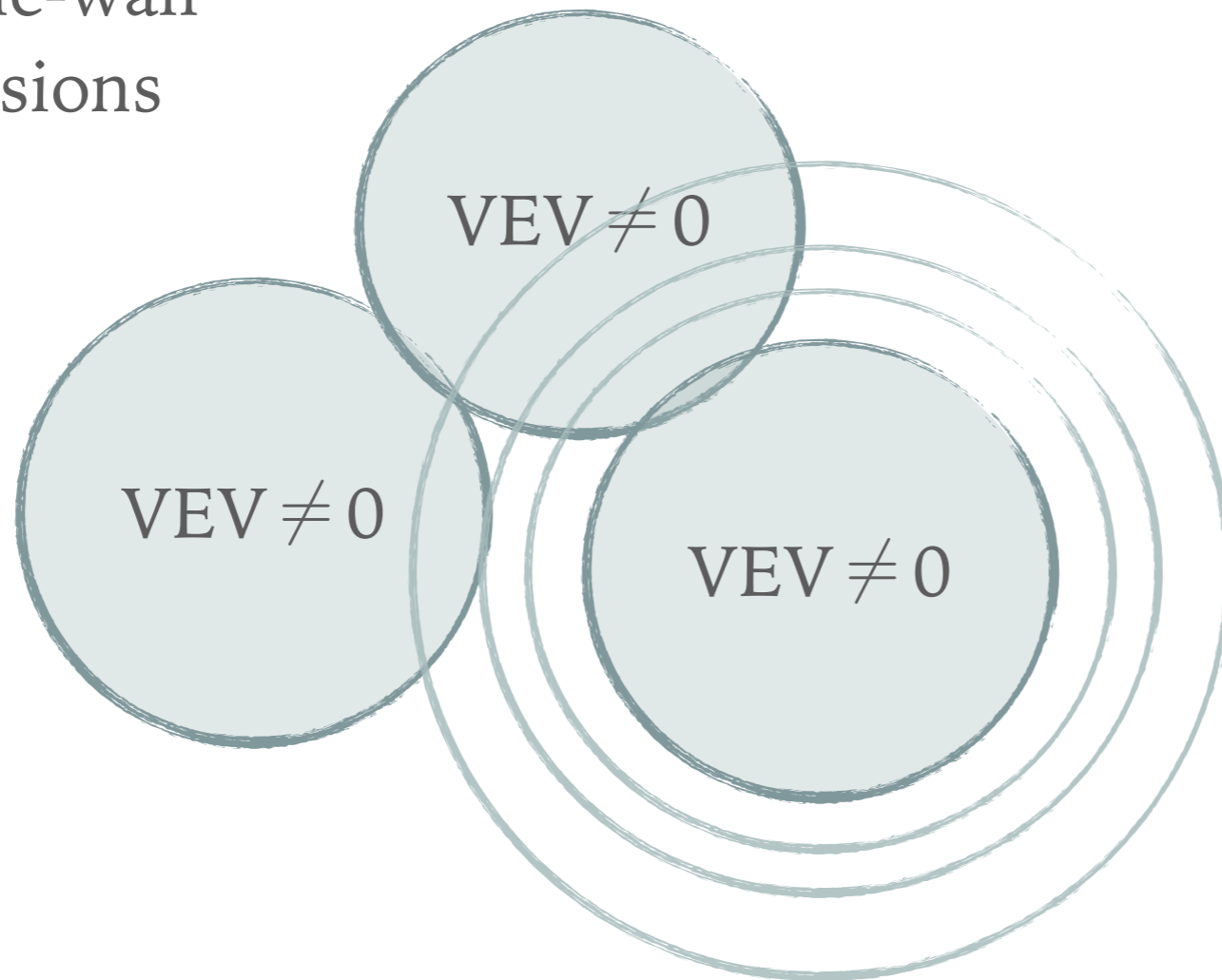


# SOURCES OF GRAVITATIONAL WAVES

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bubble-wall  
collisions

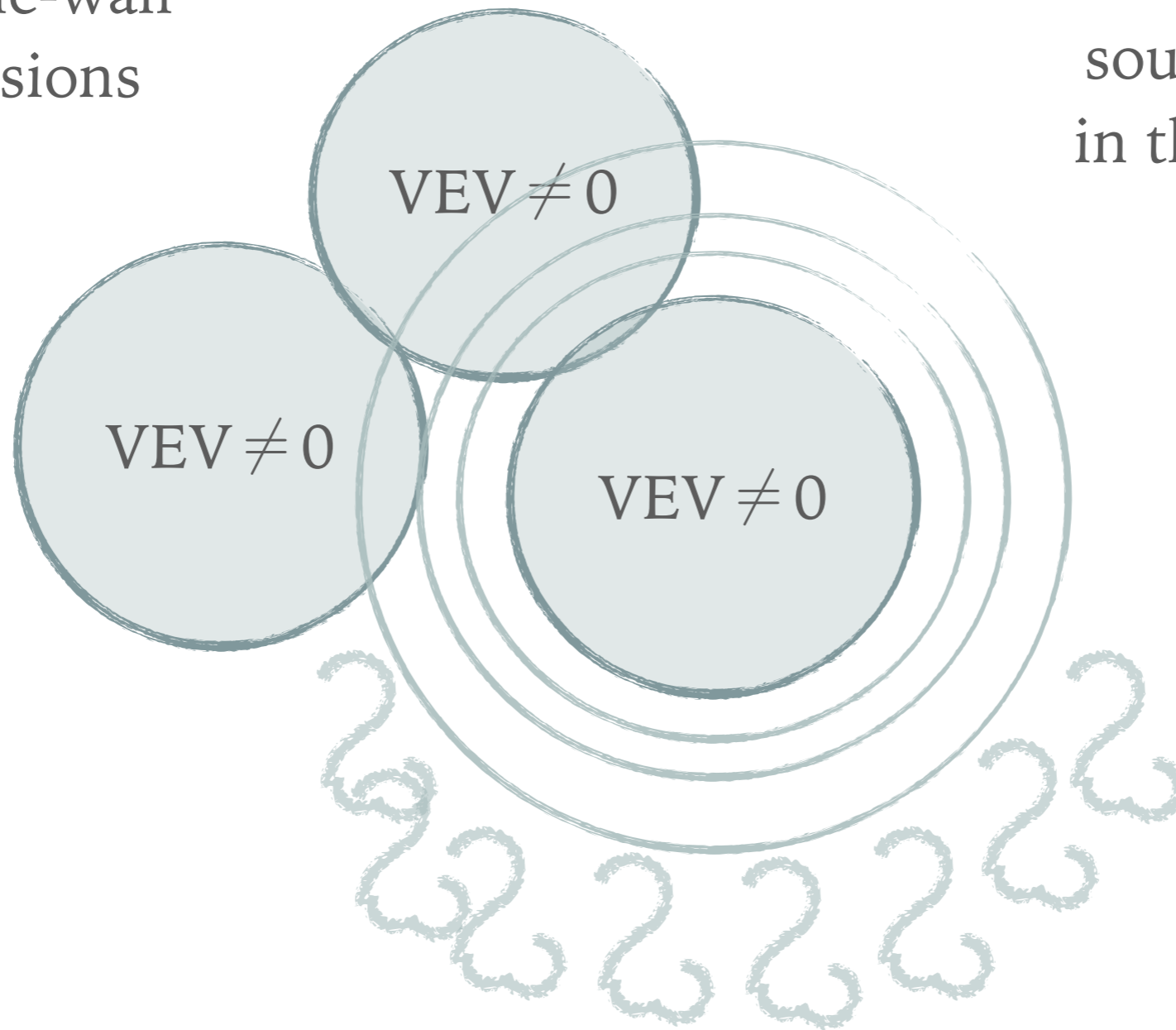
sound waves  
in the plasma



# SOURCES OF GRAVITATIONAL WAVES

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bubble-wall  
collisions

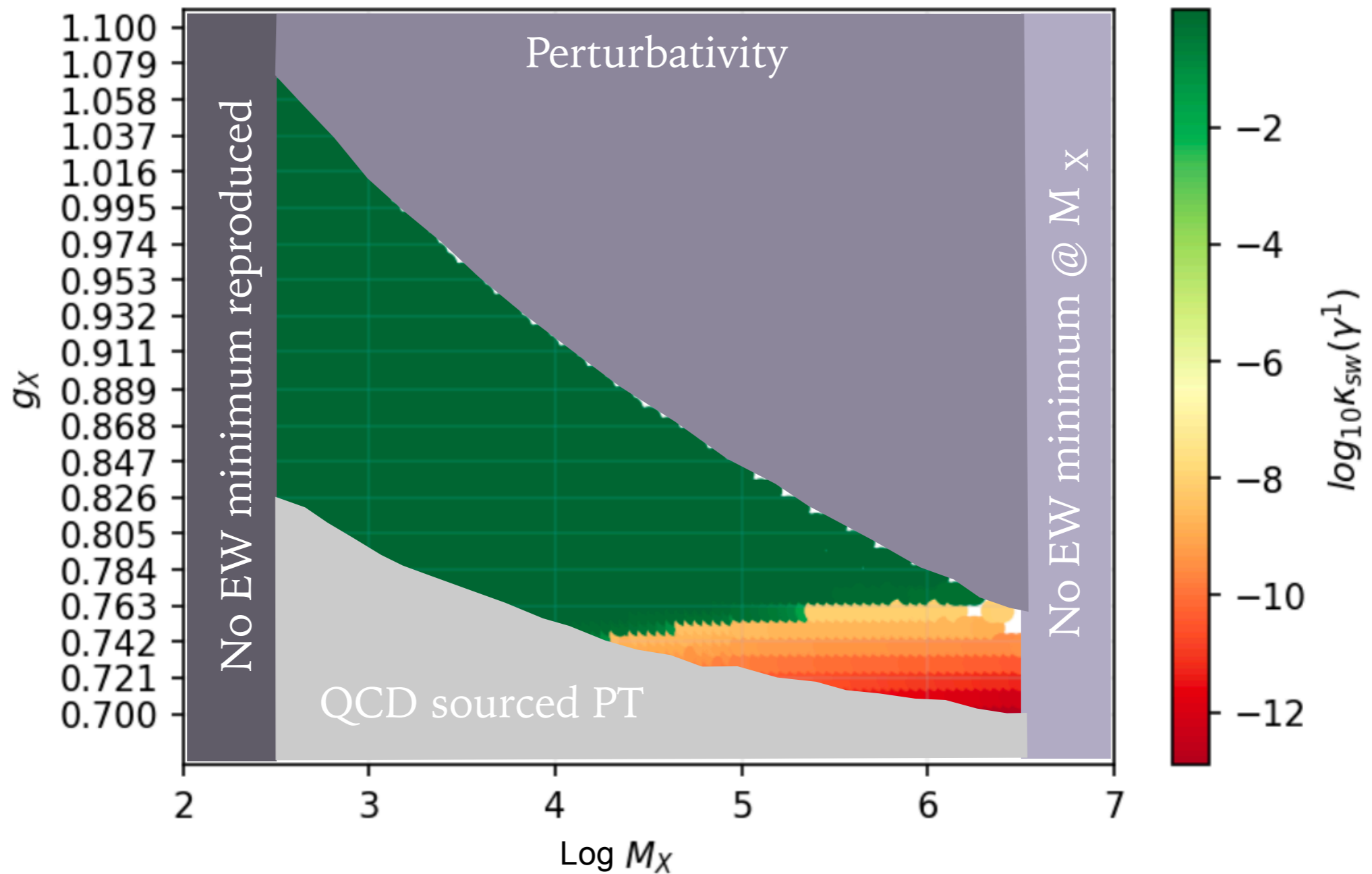


sound waves  
in the plasma

turbulence in  
the plasma

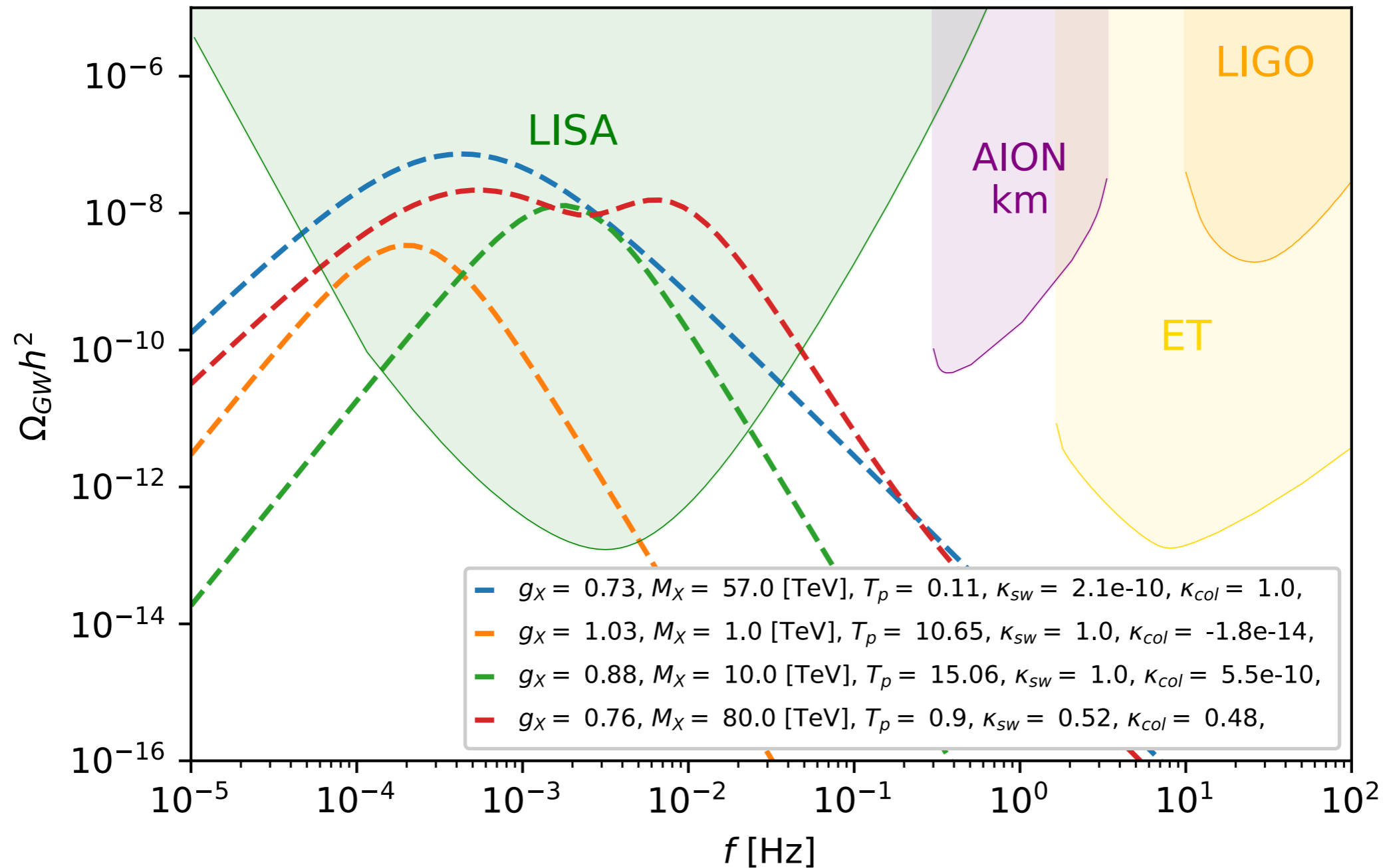
# SOURCES OF GRAVITATIONAL WAVES

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# GRAVITATIONAL WAVE SPECTRA



[sensitivity curves courtesy M. Lewicki]

# DARK MATTER PRODUCTION

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# SU(2)CSM

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$$V^{(0)}(\Phi, \Psi) = \lambda_1 (\Phi^\dagger \Phi)^2 + \lambda_2 (\Phi^\dagger \Phi) (\Psi^\dagger \Psi) + \lambda_3 (\Psi^\dagger \Psi)^2,$$

$$SU(2) \rightarrow \mathbb{Z}_2 \times \mathbb{Z}_2$$

DM stability protected by a symmetry

[See also: T.Hambye, A.Strumia, PRD88 (2013) 055022, C.Carone, R.Ramos, PRD88 (2013) 055020, V.V.Khoze, C.McCabe, G.Ro, JHEP 08 (2014) 026, T. Hambye, A.Strumia, D.Teresi, JHEP 1808 (2018) 188, I.Baldes, C. Garcia-Cely, JHEP 05 (2019) 190, T.Prokopec, J.Rezacek, BS, JCAP02(2019)009, D. Marfaria, P. Tseng, JHEP 02 (2021) 022]

# NON-STANDARD DM PRODUCTION

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supercooling

PT and reheating

hot Universe,  
massless particles

cool Universe,  
diluted massless  
particles

reheated Universe,  
diluted massive  
particles

# NEW PRODUCTION MECHANISM

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Standard freezeout  
With nonstandard  
initial condition

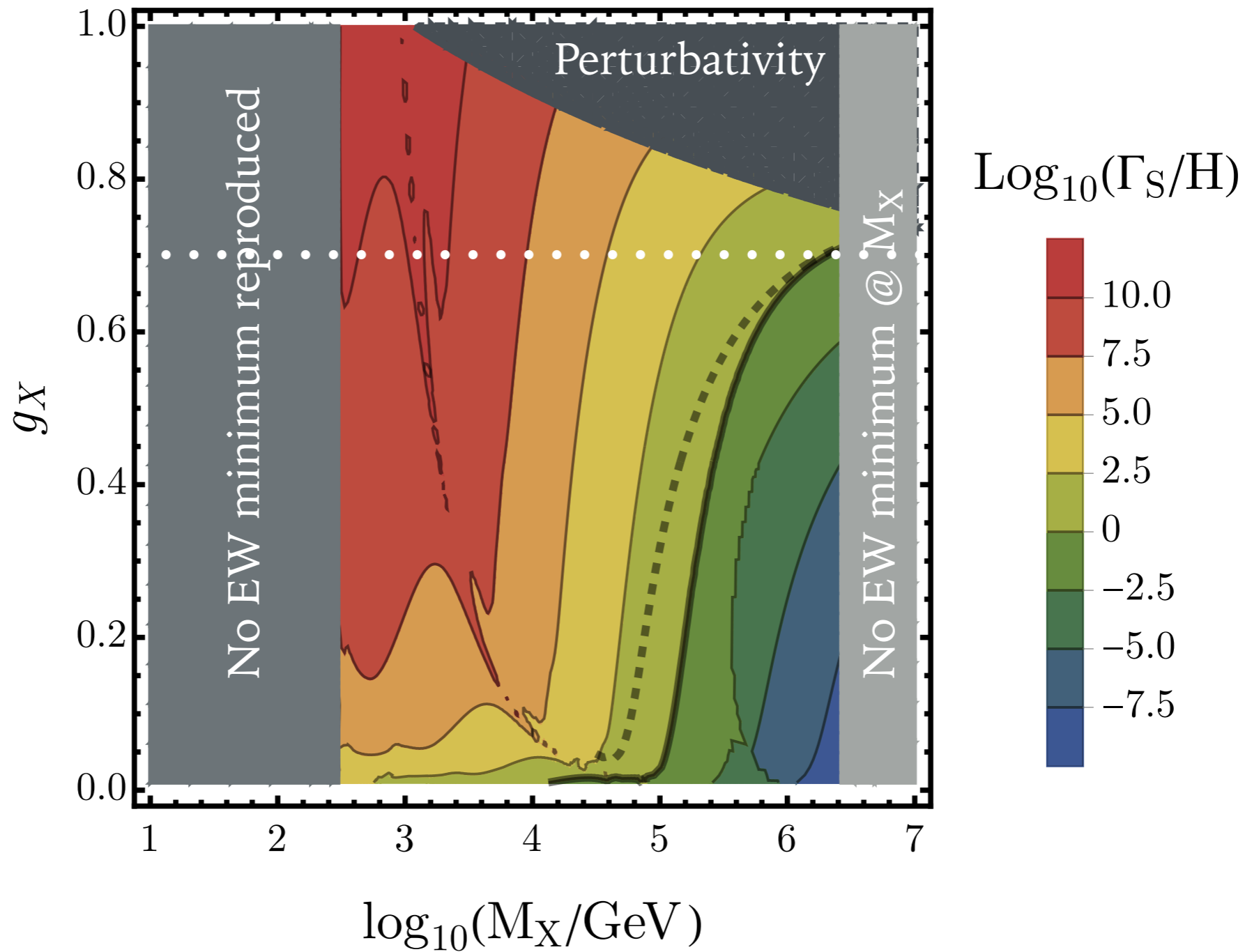
$$T_{\text{dec}} < T_{\text{reh}}$$

Supercool DM  
DM diluted by  
thermal inflation

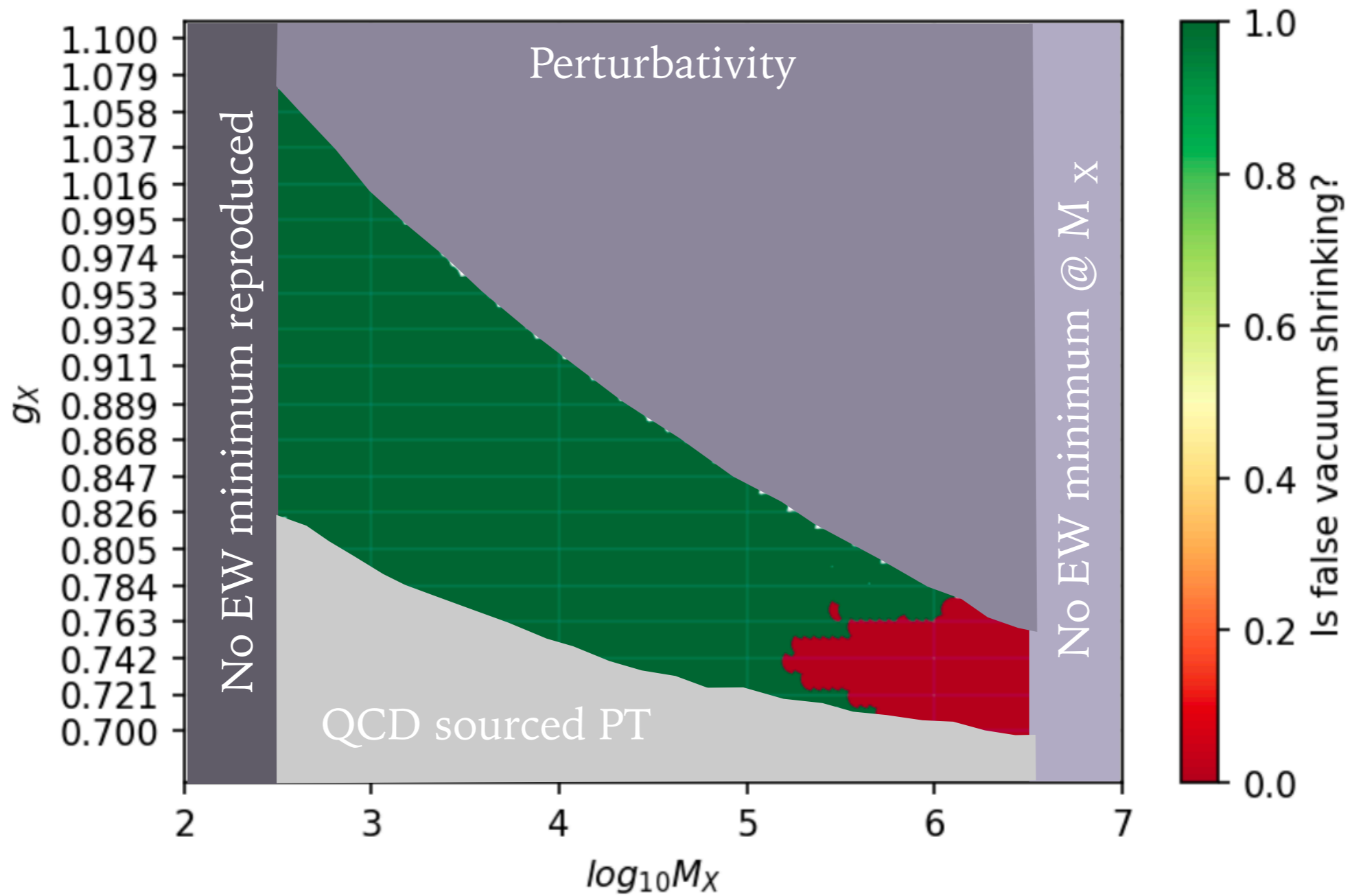
$$T_{\text{dec}} > T_{\text{reh}}$$

[T.Hambye, A.Strumia, PRD88 (2013) 055022, C.Carone, R.Ramos, PRD88 (2013) 055020, V.V.Khoze, C.McCabe, G.Ro, JHEP 08 (2014) 026, T. Hambye, A.Strumia, D.Teresi, JHEP 1808 (2018) 188, I.Baldes, C. Garcia-Cely, JHEP 05 (2019) 190, D. Marfaria, P. Tseng, JHEP 02 (2021) 022]

# REHEATING

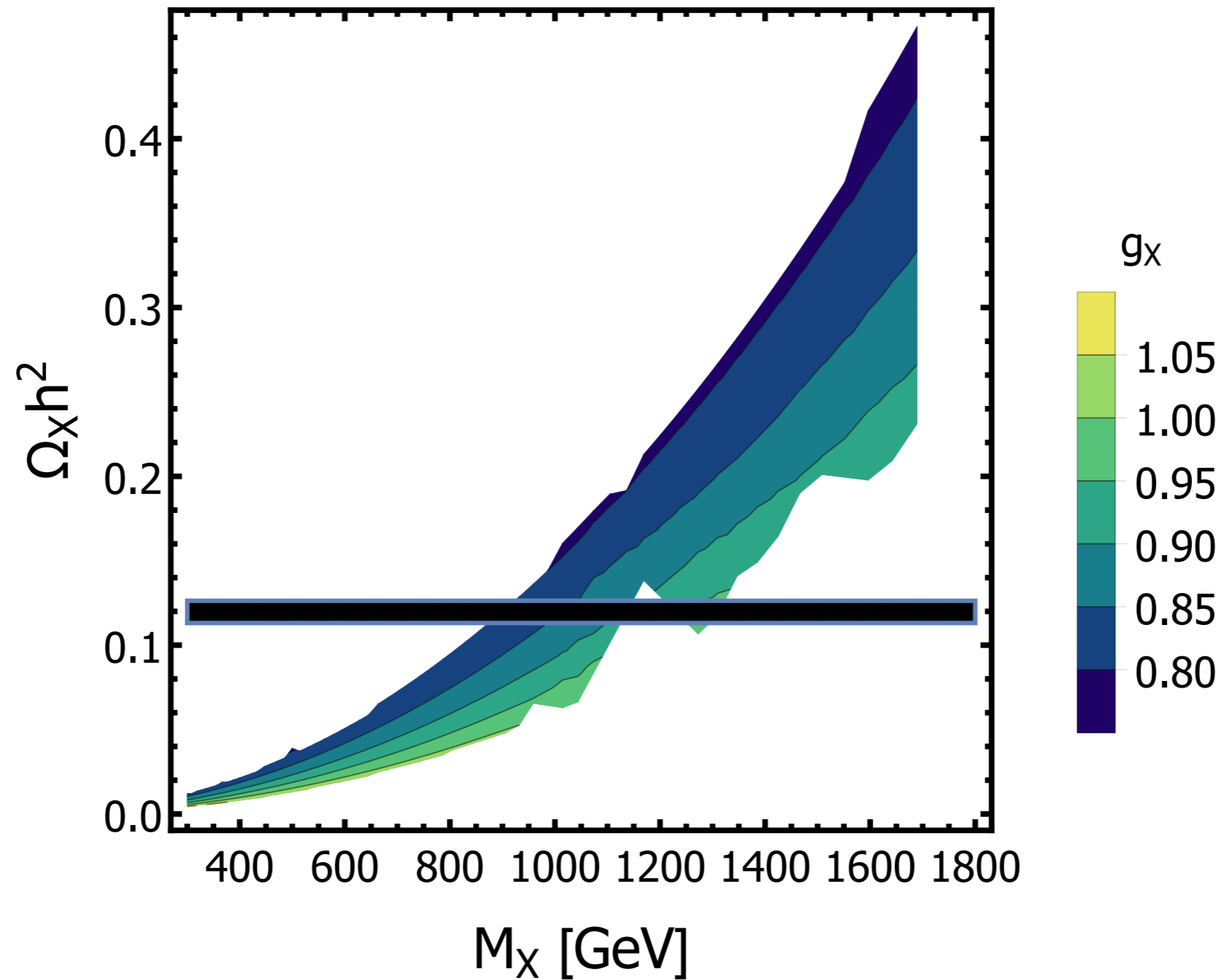


# REHEATING



# DM ABUNDANCE - FREEZEOUT

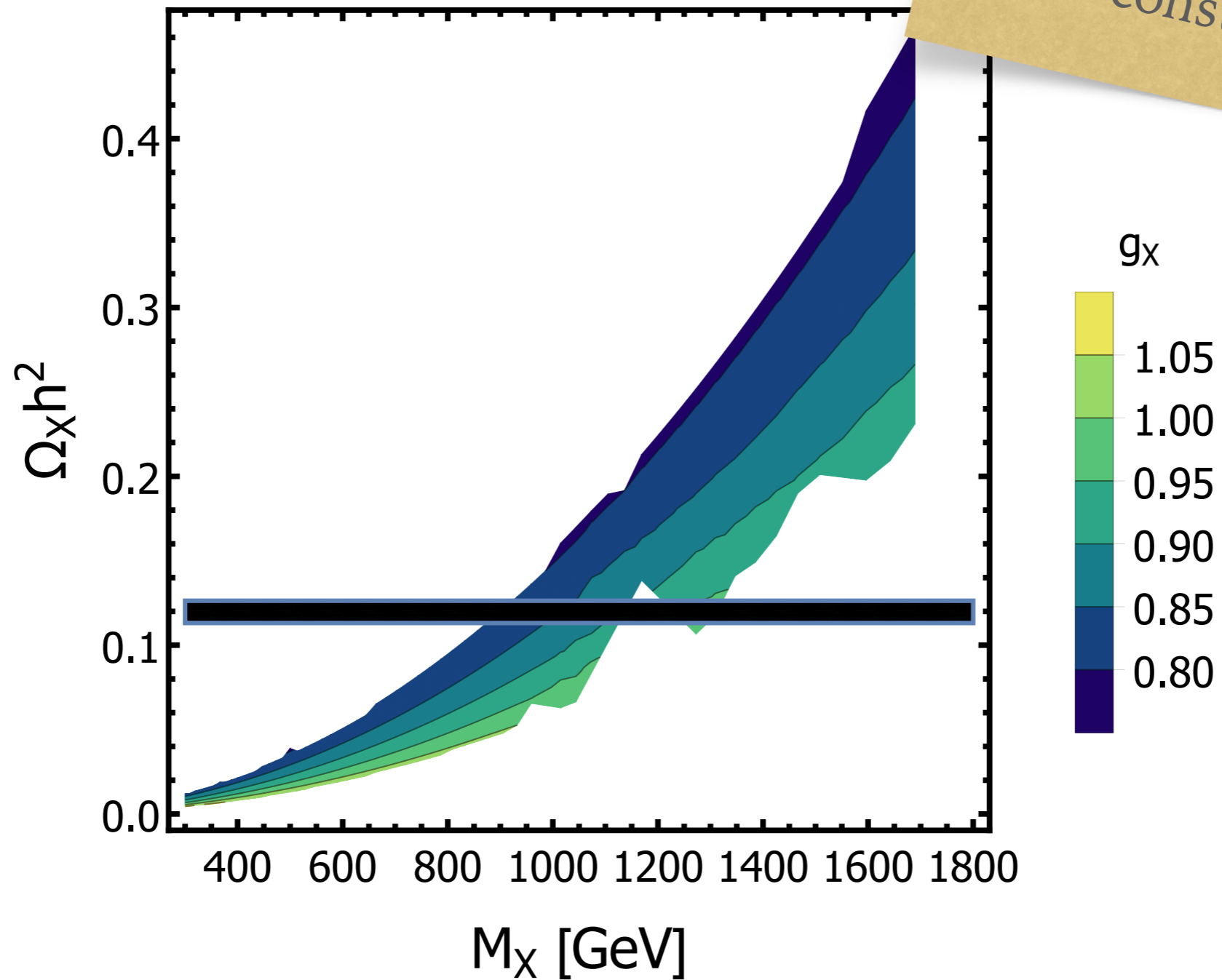
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# DM ABUNDANCE - FREEZEOUT

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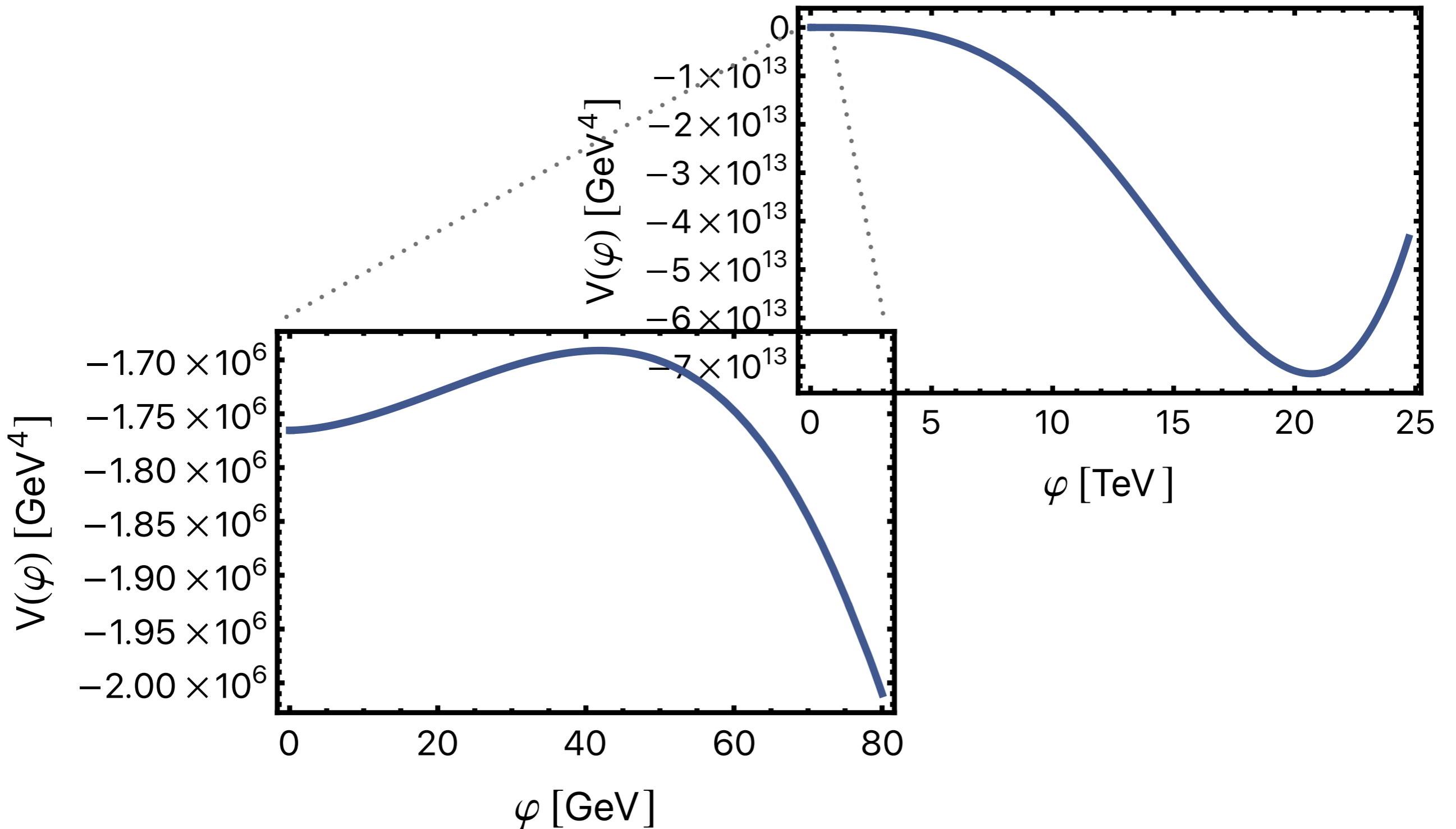
Parameter space for correct DM relic abundance significantly constrained

# SCALE DEPENDENCE OF PT PARAMETERS

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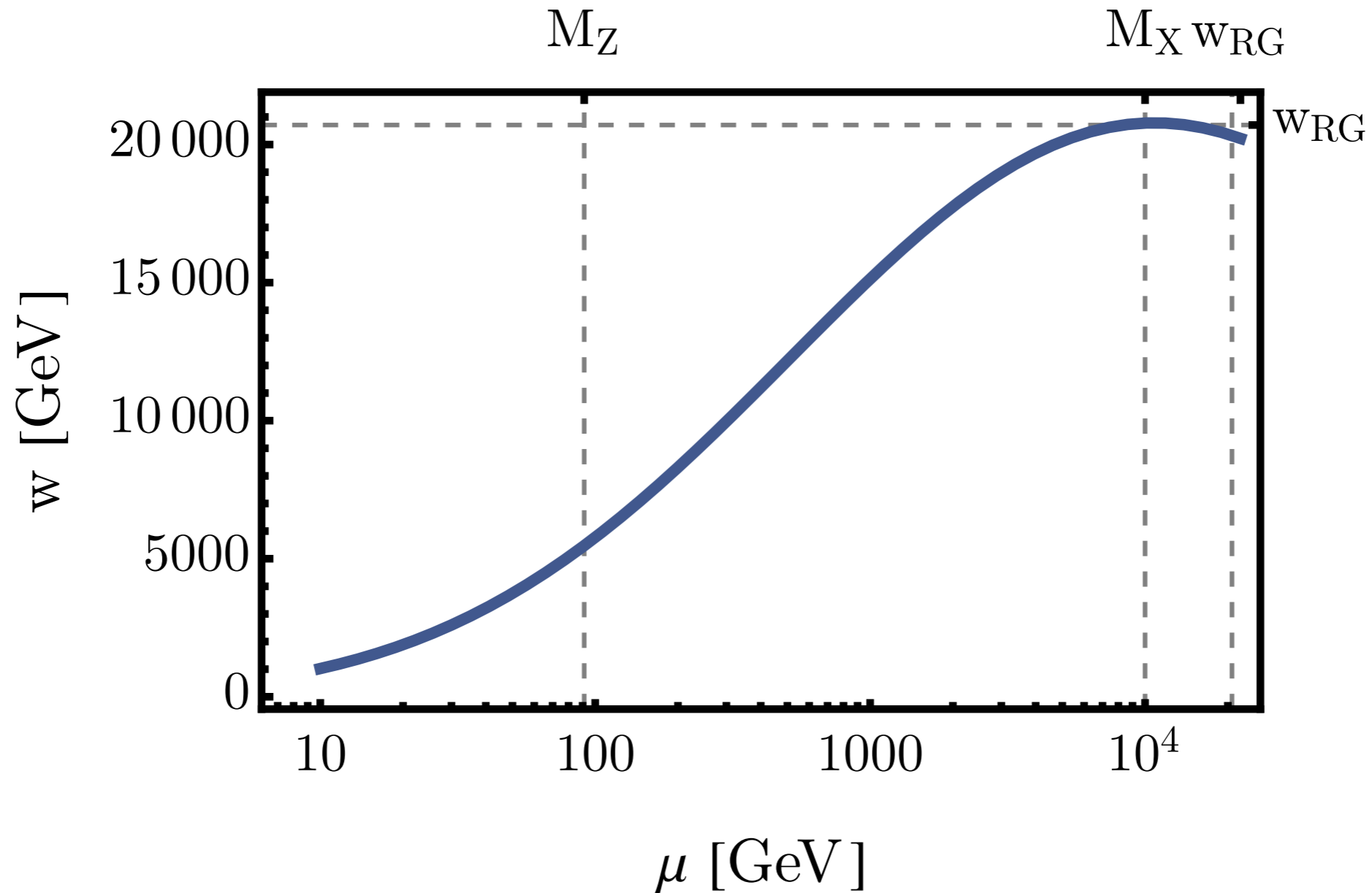
# DIFFERENT SCALES INVOLVED

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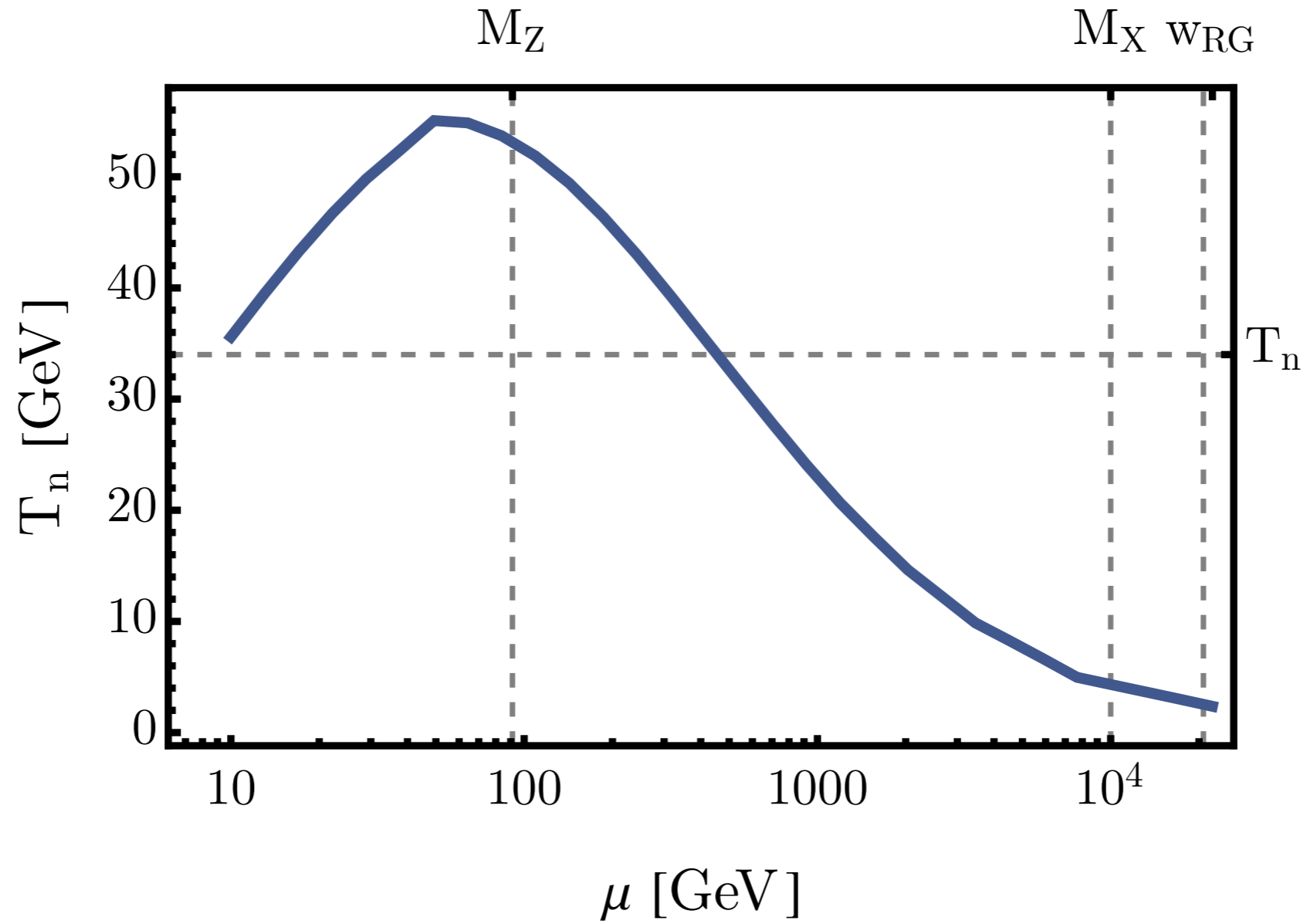
# SCALE DEPENDENCE OF THE VEV

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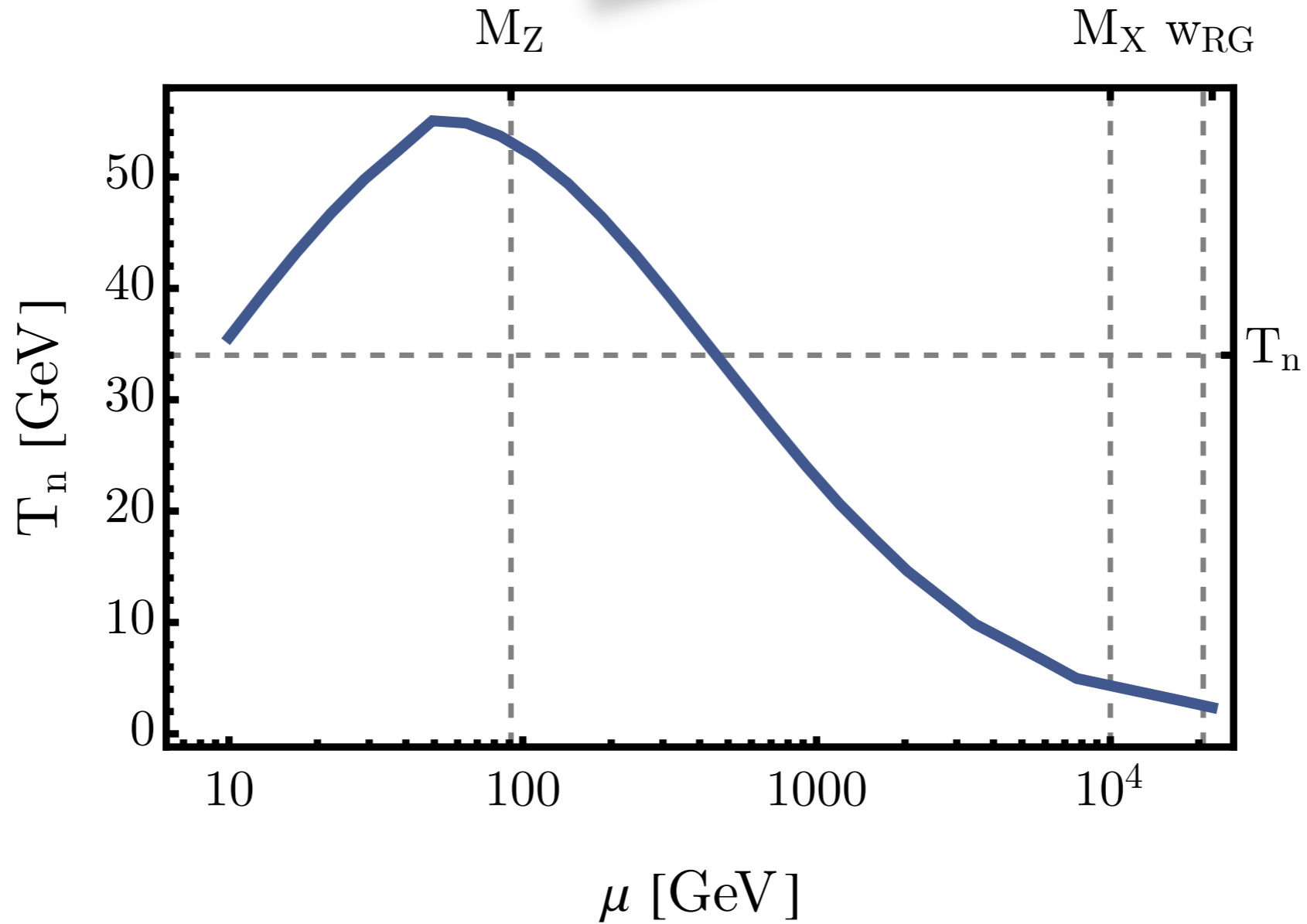
# SCALE DEPENDENCE

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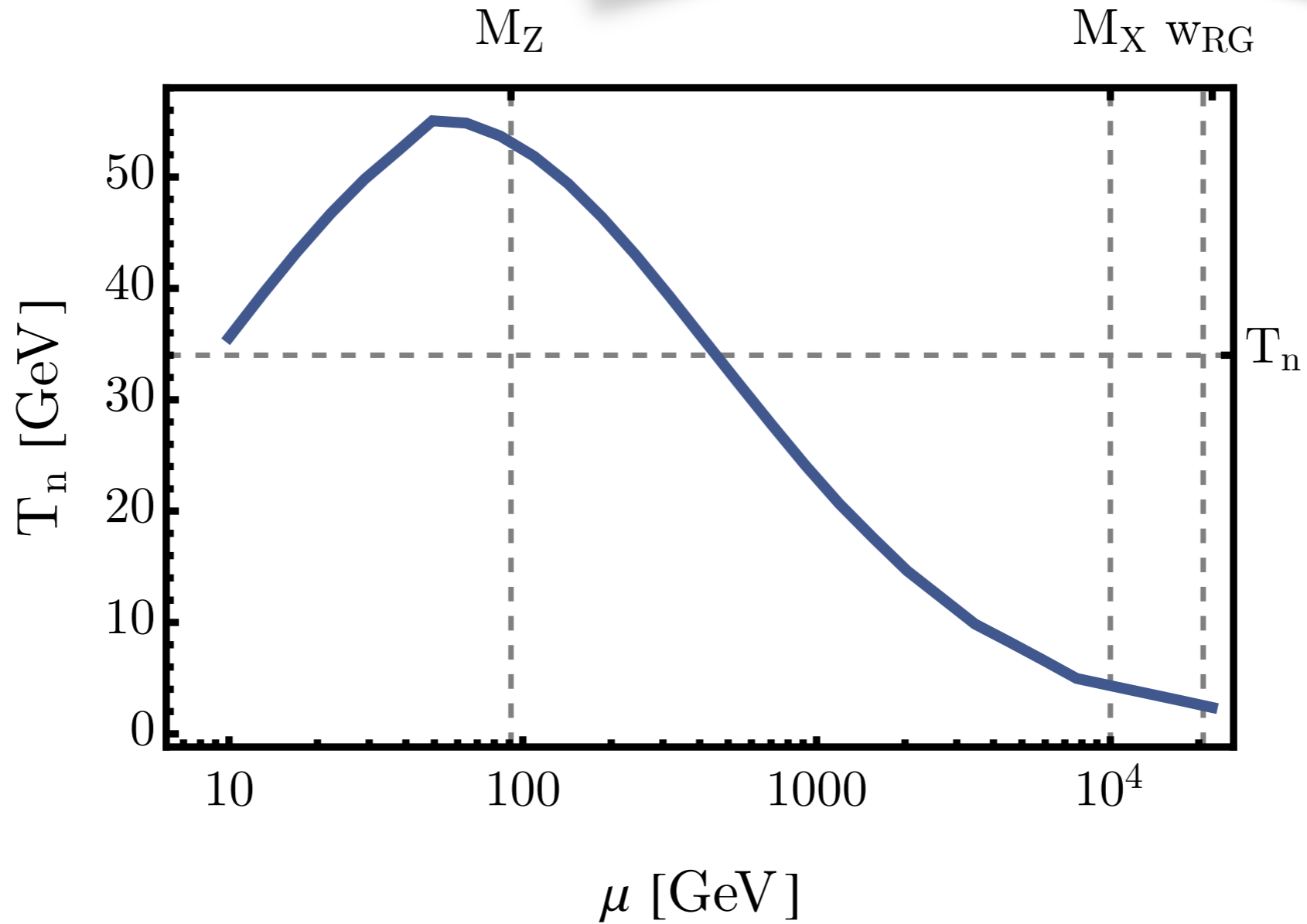
# SCALE DEPENDENCE

Remedy: RG improvement



# SCALE DEPENDENCE

Still to be improved



# SUMMARY

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# SUMMARY

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Phase transition is  
well testable in  
conformal modes

DM parameter space  
highly constrained  
from running of  
couplings

Theoretical  
uncertainties are still  
huge: improvements  
needed before LISA

THANK YOU FOR YOUR ATTENTION

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NATIONAL SCIENCE CENTRE  
POLAND

# DM PRODUCTION MECHANISMS

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## Freeze-in

DM not in thermal equilibrium, produced by decays or annihilations in the visible sector

## Dark freeze-out

DM not in equilibrium with the visible sector, freeze-out within the dark sector

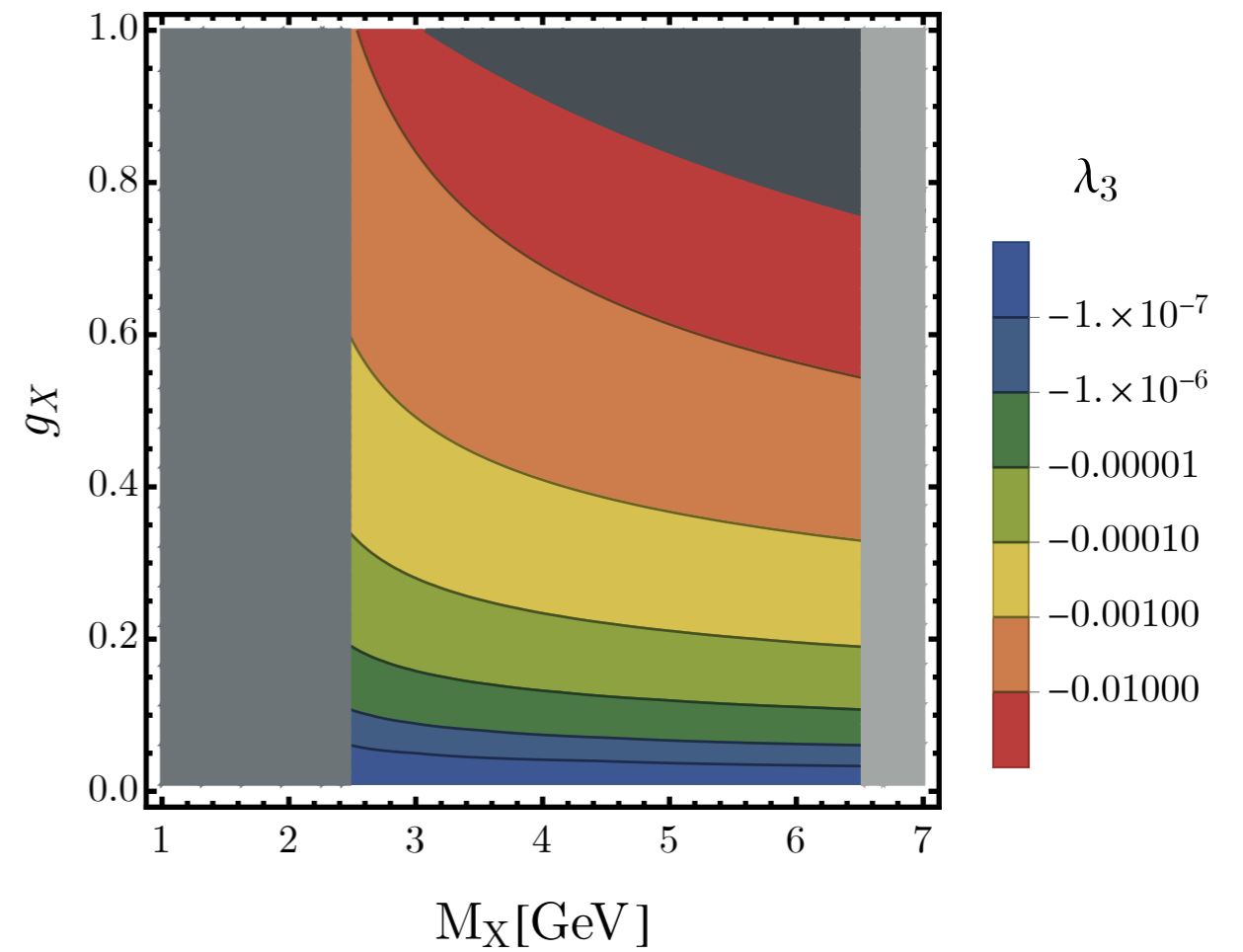
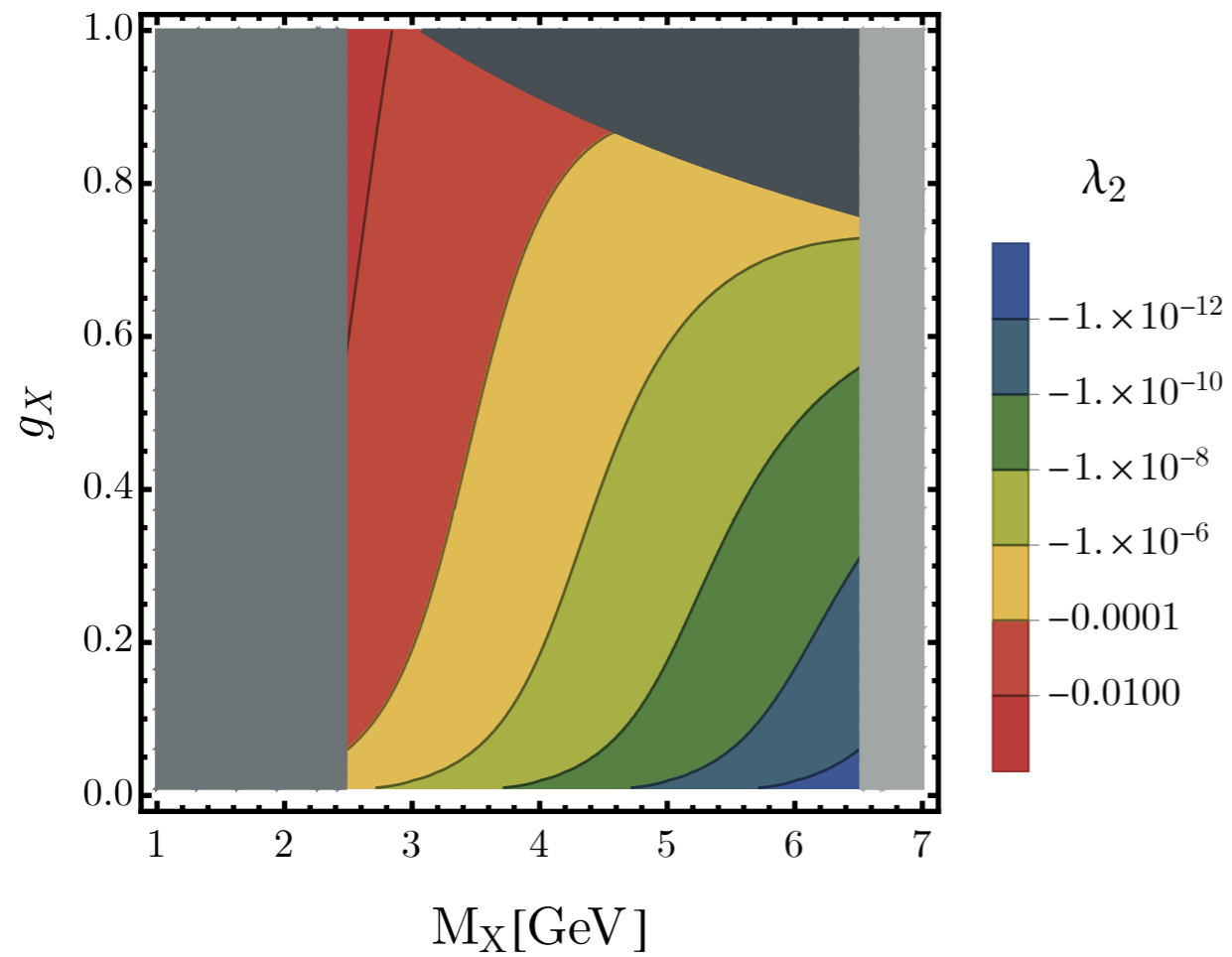
## Reannihilation

DM frozen in the dark sector but produced by the visible sector, final freeze-out when the yield ends

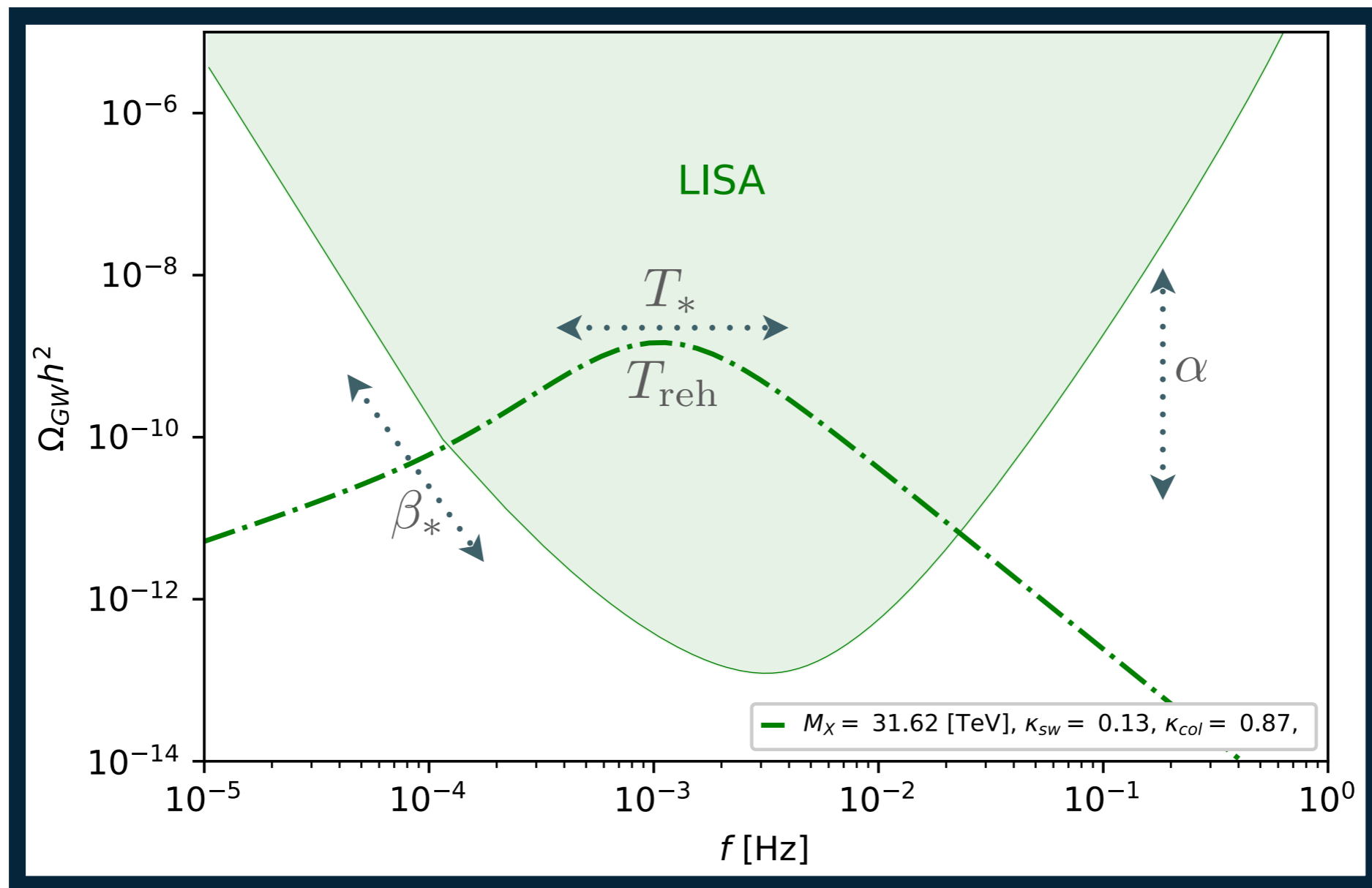
[N. Bernal et al, *Int.J.Mod.Phys.A* 32 (2017) 27, 1730023]

# SCALAR COUPLINGS

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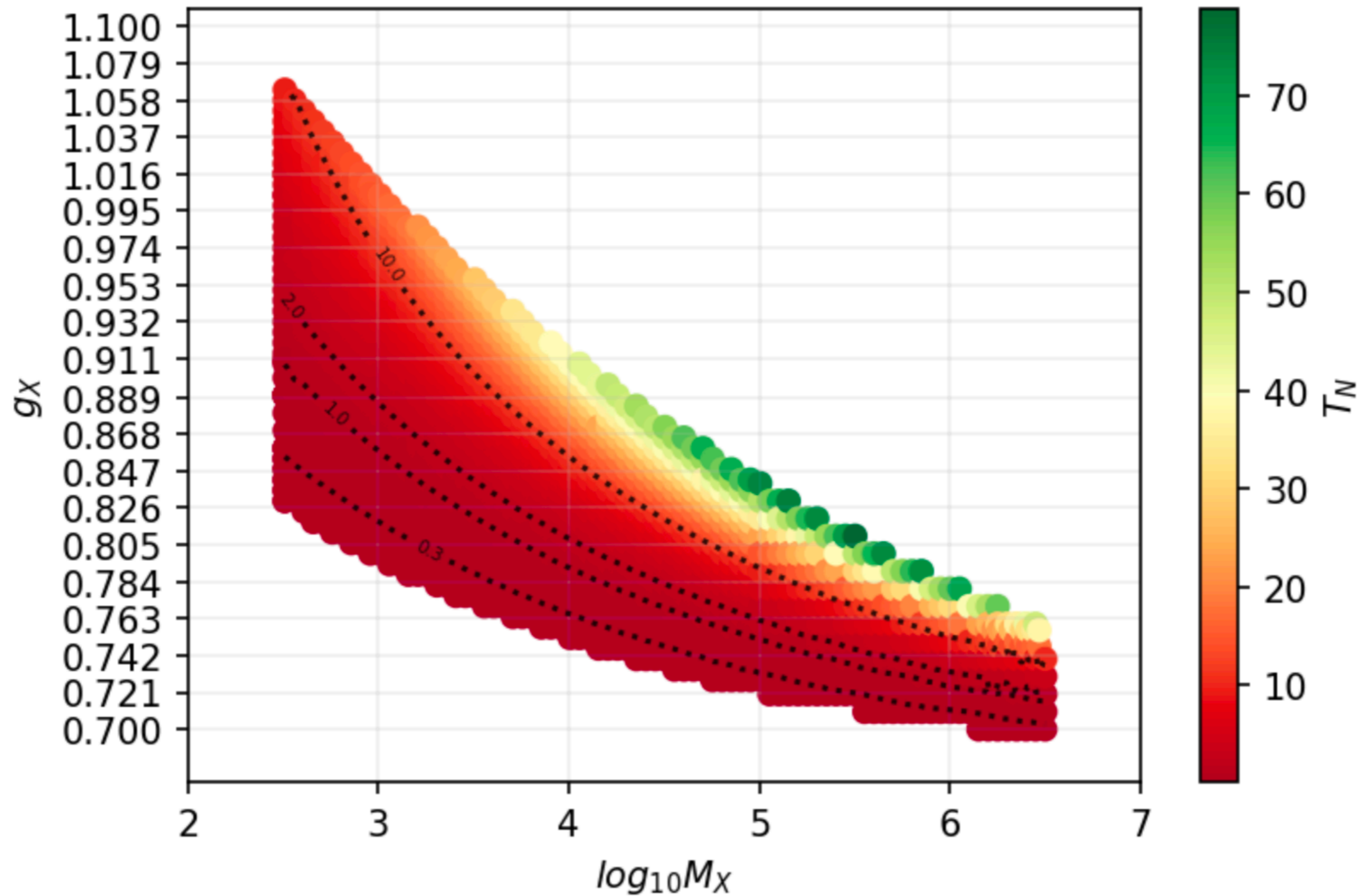


# GW PARAMETERS



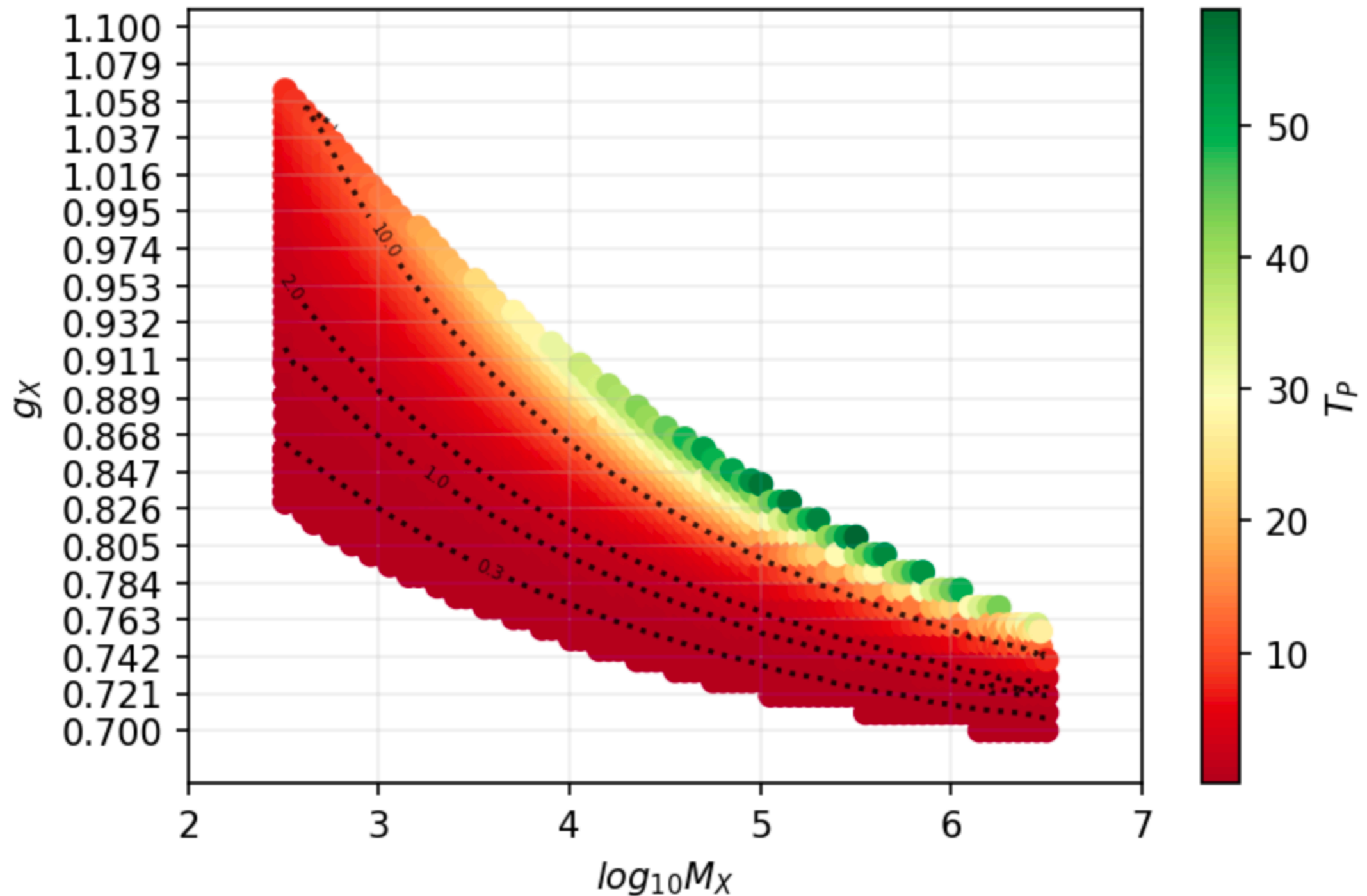
[Inspired by a talk by Pedro Schwaller]

# GW PARAMETERS



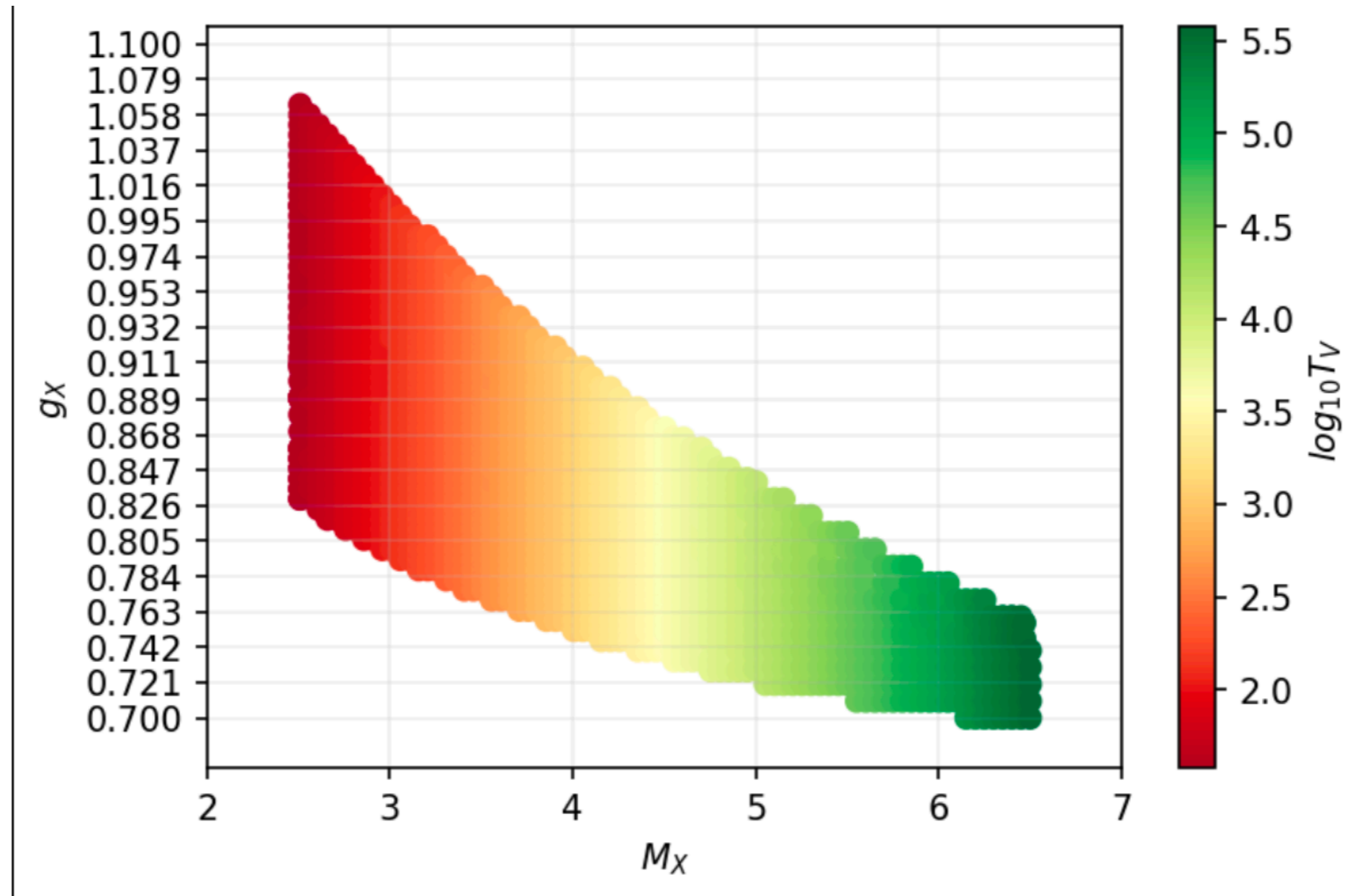
# GW PARAMETERS

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# GW PARAMETERS

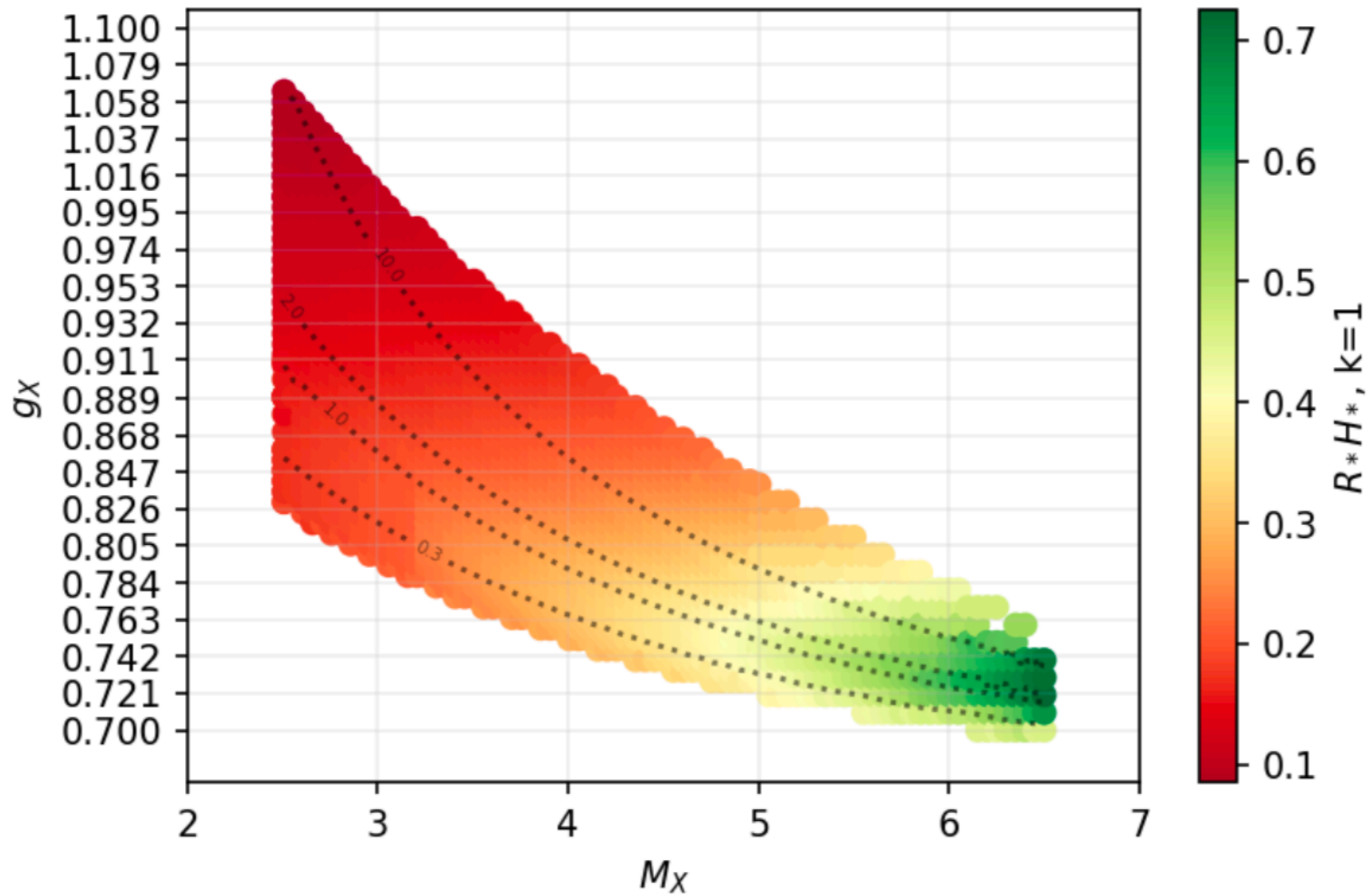
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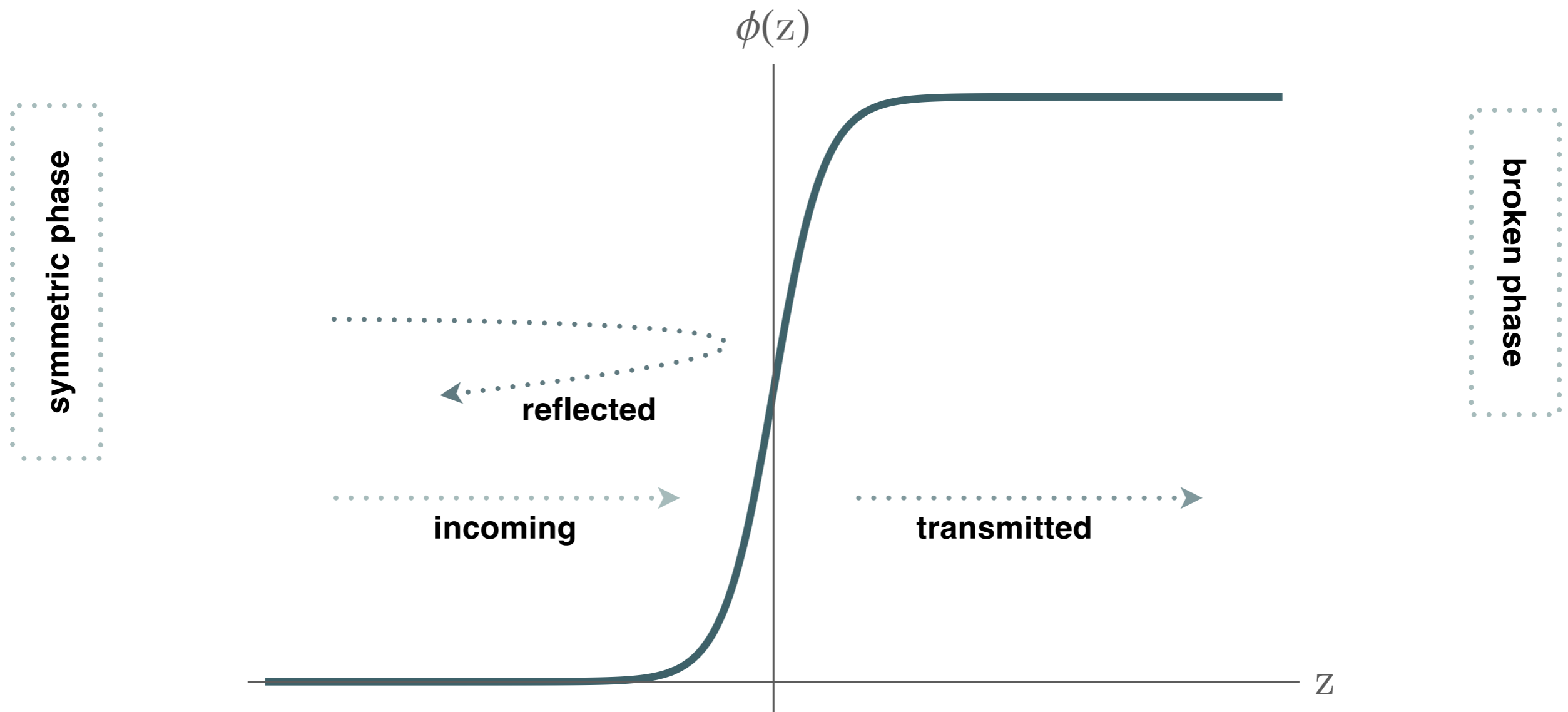
# GW PARAMETERS

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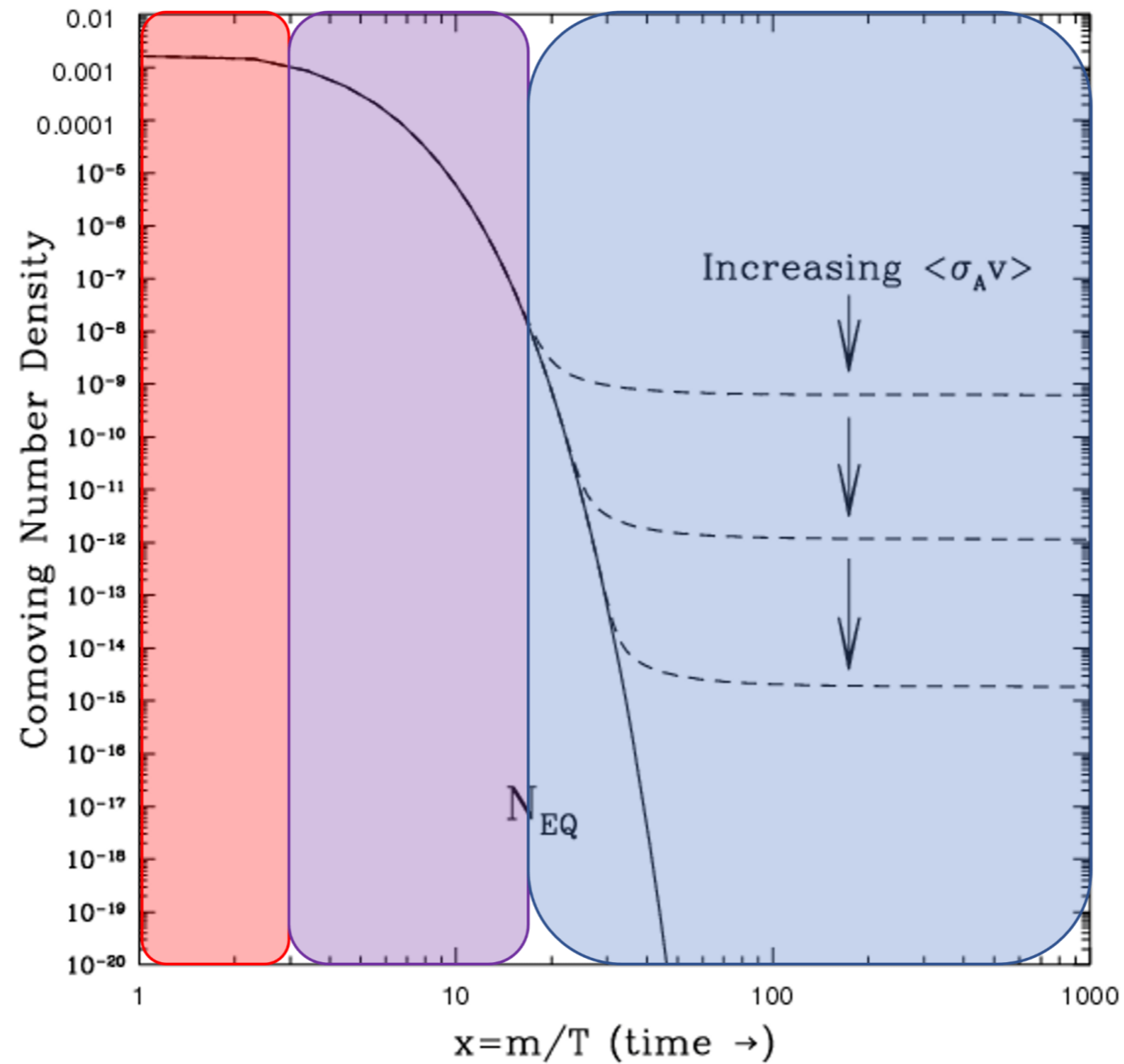
# SOUND WAVES OR BUBBLE COLLISIONS?

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[G.D. Moore, T. Prokopec, PRL 75 (1995), PRD 52 (1995), P.B. Arnold, PRD 48 (1993) 1539, D. Bodeker, G.D. Moore, JCAP 0905 (2009) 009; JCAP 1705 (2017) 025, G.C. Dorsch, S. J. Huber and T. Konstandin, JCAP 12 (2018); 2106.06547, T. Konstandin, G. Nardini and I. Rues, JCAP 09 (2014), J.Kozaczuk, JHEP 10 (2015), S. Höche et al, 2007.10343, Y. Gouttenoire, R. Jinno, F. Sala, 2112.07686]

# STANDARD FREEZE-OUT



[from Colb and Turner, adapted by particle bites.com]