## Phenomenology of Flavoured Trinification

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### The SM is a tremendously successful theory that explains "boringly" well all its predictions!

However, it fails to...

- Explain neutrino masses
- Explain dark matter
- Explain CP violation and matter/anti-matter assymetry
- Explain the observed flavour structure

### Top-down approach: the story of Trinification

The trinification gauge group (Glashow, '84)

$$[SU(3)_{L} \times SU(3)_{R} \times SU(3)_{C}] \rtimes \mathbb{Z}_{3}^{(LRC)}$$

$$\downarrow$$

$$SU(3)_{C} \times SU(2)_{L} \times SU(2)_{R} \times U(1)_{L+R}$$

$$\downarrow$$

$$SU(3)_{C} \times SU(2)_{L} \times U(1)_{Y}$$

- Subgroup of  $E_6 \supset [SU(3)]^3$
- SM fields sit in chiral superfields that are bi-fundamental representation of the gauge group:  $\mathbf{L} \sim (\mathbf{3}, \mathbf{\bar{3}}, \mathbf{1})$ ,  $\mathbf{Q}_{\mathrm{L}} \sim (\mathbf{\bar{3}}, \mathbf{1}, \mathbf{3})$ , and  $\mathbf{Q}_{\mathrm{R}} \sim (\mathbf{1}, \mathbf{3}, \mathbf{\bar{3}})$ :

• Each family can be arranged into an  $E_6$  27-plet:

$$\mathbf{27}^{i} = (\mathbf{3}, \mathbf{\bar{3}}, \mathbf{1})^{i} \otimes (\mathbf{1}, \mathbf{3}, \mathbf{\bar{3}})^{i} \otimes (\mathbf{\bar{3}}, \mathbf{1}, \mathbf{3})^{i}$$

#### Why Trinification

#### **Positives:**

- The model accommodates any quark and lepton masses and mixings (Sayre et al 2016)
- Naturally light neutrinos via radiative see-saw with split-SUSY (Cauet et al 2011)
- Gauge symmetry preserve baryon number, i.e. no gauge-mediated proton decay (Achiman&Stech'78; Glashow&Kang'84)
- Motivated as a low-energy version of E8xE8 heterotic string theory (Gross et al 1985)
  - GUT scale fermion masses through  $L \cdot L' \cdot L''$  type operators
    - Higher dimensional operators needed (Cauet et al. 2011)

#### **Negatives:**

- Considerable amount of particles and many couplings involved
  - Realistic calculations cumbersome
- Unmotivated Hierarchy between the trinification and the EW breaking scales (common to most GUTs)

Trinification-based models were left as the least developed GUT scenarios

#### "Flavoured" T-GUT approach

#### Build a SUSY GUT-scale framework in the top-down approach that:

- > Features all the basic advantages of the trinification GUTs and resolves their major issues;
- > Addresses the μ-problem of conventional MSSM-based approaches;
- Senerates larger masses and Cabibbo mixing at tree-level;
- > Full CKM and light fermion masses to be radiatively generated;
- > Adopts a seesaw mechanism for light active neutrinos, with no strong PMNS hierarchies;
- > Unifies gauge interactions and reduces parametric freedom in the Yukawa sector (Yukawa unification).

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References:
2004.114550,
2001.06383, 2001.04804,
1711.05199, 1610.03642,
1606.03492
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#### "Flavoured" T-GUT with gauged family symmetry

#### **Consider embedding Trinification into E6:**

#### **Scale hierarchy:**

$$M_{\rm GUT} \gtrsim M_6 \gtrsim M_3$$
  $M_{\rm S} \ll M_3$ 

possible source

for Dark Matter

# $egin{aligned} & \mathbb{Z}_2 ext{-even} & \mathbb{Z}_2 ext{-odd} \ & oldsymbol{\psi}^{\mu\,i} = (\mathbf{27,2})_{(1)} \;, \;\; oldsymbol{\psi}^{\mu\,3} = (\mathbf{27,1})_{(-2)} \ & oldsymbol{\mathcal{H}}_{\mathcal{U}} = (\mathbf{1,2})_{(-1)} \;, \;\; oldsymbol{\mathcal{H}}_{\mathcal{D}} = (\mathbf{1,2})_{(+1)} & oldsymbol{\mathcal{L}}_k = (\mathbf{1,2})_{(-1)} \ & oldsymbol{\mathcal{L}}_k = (\mathbf{1,1})_{(+2)} \ & oldsymbol{\mathcal{E}}_k = (\mathbf{1,1})_{(+2)} \ & oldsymbol{\mathcal{N}}_k = (\mathbf{1,1})_{(0)} \ & oldsymbol{\Psi} = (\mathbf{2430,1})_{(0)} \ & oldsymbol{\Psi} = (\mathbf{2430,1})_{(0)} \ & oldsymbol{\mathcal{L}}_k = (\mathbf{1,1})_{(0)} \ & oldsymb$

#### **Anomaly-free content:**

Massless sector dim-3 superpotential with universal Yukawa coupling:

$$W_{27} = \frac{1}{2} \lambda_{27} d_{\mu\nu\lambda} \varepsilon_{ij} \psi^{\mu i} \psi^{\nu j} \psi^{\lambda 3} = 0$$

 $d_{\mu\nu\lambda}$  – completely symmetric  $\epsilon_{ij}$  – totally anti-symmetric

$$(\mathbf{27},\mathbf{2})_{(1)} \equiv \psi^{\mu i}$$
,  $(\mathbf{27},\mathbf{1})_{(-2)} \equiv \psi^{\mu 3}$   $\mu = 1, \dots, 27$   $i = 1, 2$ 

#### Effects from higher dimensional operators become dominant!

$$W_{\boldsymbol{\psi}} = \frac{\varepsilon_{ij} \boldsymbol{\psi}^{\mu i} \boldsymbol{\psi}^{\nu j} \boldsymbol{\psi}^{\lambda 3}}{2M_{\text{GUT}}} \left[ \tilde{\lambda}_{1} \boldsymbol{\Sigma}^{\alpha}_{\mu} d_{\alpha\nu\lambda} + \tilde{\lambda}_{2} \boldsymbol{\Sigma}^{\alpha}_{\nu} d_{\alpha\mu\lambda} + \tilde{\lambda}_{4} \boldsymbol{\Sigma'}^{\alpha}_{\mu} d_{\alpha\nu\lambda} + \tilde{\lambda}_{5} \boldsymbol{\Sigma'}^{\alpha}_{\nu} d_{\alpha\mu\lambda} \right]$$

#### **E6 and Trinification breaking**

$$\mathcal{L}_{5D} = -\frac{\xi}{M_{CLIT}} \left[ \frac{1}{4C} \operatorname{Tr}(\mathbf{\textit{F}}_{\mu\nu} \cdot \tilde{\Phi}_{E_6} \cdot \mathbf{\textit{F}}^{\mu\nu}) \right] \qquad \qquad \tilde{\Phi}_{E_6} \in (78 \otimes 78)_{\text{sym}} = \mathbf{1} \oplus \mathbf{650} \oplus \mathbf{2430}$$

 $\Sigma$ ,  $\Sigma'$  and  $\Psi$  allow quadratic and cubic superpotential interactions

$$W_{\rm E_6} \supset M_{\Sigma} {\rm Tr} \Sigma^2 + M_{\Sigma'} {\rm Tr} \Sigma'^2 + M_{\Psi} {\rm Tr} \Psi^2 + \lambda_{\Sigma} {\rm Tr} \Sigma^3 + \lambda_{\Sigma'} {\rm Tr} \Sigma'^3 + \lambda_{\Psi} {\rm Tr} \Psi^3 + {\rm crossed terms}$$

and can develop VEVs obeying the relation

$$v_{\rm E_6}^2 = v_{\Sigma}^2 + v_{\Sigma'}^2 + v_{\Psi}^2 \equiv (k_{\Sigma}^2 + k_{\Sigma'}^2 + k_{\Psi}^2) v_{\rm E_6}^2$$
,  $k_{\Sigma}^2 + k_{\Sigma'}^2 + k_{\Psi}^2 = 1$ 

$$k_\Psi \propto rac{\langle 2430
angle}{M_6}$$
 ,  $k_\Sigma \propto rac{\langle 650
angle}{M_6}$  ,  $k_{\Sigma'} \propto rac{\langle 650'
angle}{M_6}$ 

$$\alpha_{3C}^{-1}(1+\zeta\delta_{C})^{-1} = \alpha_{3L}^{-1}(1+\zeta\delta_{L})^{-1} = \alpha_{3R}^{-1}(1+\zeta\delta_{R})^{-1}, \qquad \zeta \sim 1$$

$$\alpha_{3A}^{-1} = \frac{4\pi}{g_{A}^{2}}, \qquad \delta_{C} = -\frac{1}{\sqrt{2}}k_{\Sigma} - \frac{1}{\sqrt{26}}k_{\Psi}, \qquad \delta_{L,R} = \frac{1}{2\sqrt{2}}k_{\Sigma} \pm \frac{3}{2\sqrt{2}}k_{\Sigma'} - \frac{1}{\sqrt{26}}k_{\Psi}$$

Chakrabortty, Raychaudhuri Phys.Lett. B673 (2009) 57-62

#### Below E6 breaking scale:

$$W_{78} = \sum_{A=L,R,C} \left[ \frac{1}{2} \mu_{78} \text{Tr} \Delta_A^2 + \frac{1}{3!} \mathcal{Y}_{78} \text{Tr} \Delta_A^3 \right] + \mu_{78} \text{Tr} (\Xi \Xi') + \sum_{A=L,R,C} \mathcal{Y}_{78} \text{Tr} (\Xi \Xi' \Delta_A)$$

$$SU(3)_L \times SU(3)_R \stackrel{v_{L,R}}{\to} SU(2)_L \times SU(2)_R \times U(1)_L \times U(1)_R$$

$$v_{\rm L} = v_{\rm R} \equiv M_3$$

 $SU(3)_L SU(3)_R SU(3)_C SU(2)_F U(1)_F$ 

#### **Trinification EFT: Yukawa sector**

 $E_6$  27-plet contains three trinification  $SU(3)_L \times SU(3)_R \times SU(3)_C$  bi-triplets:

$$\mathbf{27}\supset\left(\mathbf{3},\overline{\mathbf{3}},\mathbf{1}\right)\oplus\left(\overline{\mathbf{3}},\mathbf{1},\mathbf{3}\right)\oplus\left(\mathbf{1},\mathbf{3},\overline{\mathbf{3}}\right)\equiv\boldsymbol{L}\oplus\boldsymbol{Q}_{\mathrm{L}}\oplus\boldsymbol{Q}_{\mathrm{R}}$$

After  $\langle \Sigma \rangle$  and  $\langle \Sigma' \rangle$  VEVs the massless superpotential reduces to

#### **Accidental symmetries**

$$\begin{array}{c|cccc} & U(1)_{W} & U(1)_{B} \\ \hline \boldsymbol{L} & +1 & 0 \\ \boldsymbol{Q}_{L} & -1/2 & +1/3 \\ \boldsymbol{Q}_{R} & -1/2 & -1/3 \\ \end{array}$$

$$W_{\text{eff}} = \varepsilon_{ij} (\mathcal{Y}_1 \mathbf{L}^i \cdot \mathbf{Q}_{\text{L}}^3 \cdot \mathbf{Q}_{\text{R}}^j - \mathcal{Y}_2 \mathbf{L}^i \cdot \mathbf{Q}_{\text{L}}^j \cdot \mathbf{Q}_{\text{R}}^3 + \mathcal{Y}_2 \mathbf{L}^3 \cdot \mathbf{Q}_{\text{L}}^i \cdot \mathbf{Q}_{\text{R}}^j)$$

$$\mathcal{Y}_{1} = \zeta \frac{k_{\Sigma'}}{\sqrt{6}} \tilde{\lambda}_{45}, \quad \mathcal{Y}_{2} = \zeta \frac{k_{\Sigma}}{2\sqrt{2}} (\tilde{\lambda}_{21} - \tilde{\lambda}_{45})$$

$$\tilde{\lambda}_{ij} \equiv \tilde{\lambda}_{i} - \tilde{\lambda}_{j} \qquad \zeta \simeq M_{6}/M_{3F}$$

$$\zeta \sim 1 \qquad k_{\Sigma} \simeq -k_{\Sigma'} \qquad \tilde{\lambda}_{21} \simeq \tilde{\lambda}_{45}$$

$$\tilde{\lambda}_{ij} \equiv \tilde{\lambda}_i - \tilde{\lambda}_j \qquad \zeta \simeq M_6/M_{3F}$$

$$\zeta \sim 1$$

$$k_{\Sigma} \simeq -k_{\Sigma}$$

$$\tilde{\lambda}_{21} \simeq \tilde{\lambda}_{45}$$

Compressed hierarchy + steep E6 RG evolution suggest:

$$\mathcal{Y}_2 \ll \mathcal{Y}_1 \sim 1$$

#### tree-level quark hierarchies are secured!

$$\frac{\mathcal{Y}_1}{\mathcal{Y}_2} = \frac{m_{\mathrm{t}}}{m_{\mathrm{c}}} \approx \frac{m_{\mathrm{b}}}{m_{\mathrm{s}}} \approx \frac{m_{\mathrm{B}}}{m_{\mathrm{D,S}}} \sim \mathcal{O}(100)$$

- SUSY unifies Higgs and Leptons in L
- Only two universal Yukawa couplings at trinification scale
- Only two quark generations acquire tree-level masses

### Quark spectrum: more details

#### The most generic VeV setting:

$$\left\langle \tilde{L}^{1} \right\rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} u_{1} & 0 & 0 \\ 0 & d_{1} & e_{1} \\ 0 & \omega & s_{1} \end{pmatrix}, \quad \left\langle \tilde{L}^{2} \right\rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} u_{2} & 0 & 0 \\ 0 & d_{2} & e_{2} \\ 0 & s_{2} & f \end{pmatrix}, \quad \left\langle \tilde{L}^{3} \right\rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} u_{3} & 0 & 0 \\ 0 & d_{3} & e_{3} \\ 0 & s_{3} & p \end{pmatrix}$$

#### **Up-quark sector:**

$$M_{\rm u} = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & u_3 \mathcal{Y}_2 & u_2 \mathcal{Y}_2 \\ -u_3 \mathcal{Y}_2 & 0 & -u_1 \mathcal{Y}_2 \\ -u_2 \mathcal{Y}_1 & u_1 \mathcal{Y}_1 & 0 \end{pmatrix} \qquad m_{\rm u} = 0 \qquad m_{\rm c}^2 = \frac{1}{2} \mathcal{Y}_2^2 \left( u_1^2 + u_2^2 + u_3^2 \right) \qquad m_{\rm t}^2 = \frac{1}{2} \left[ \mathcal{Y}_1^2 \left( u_1^2 + u_2^2 \right) + \mathcal{Y}_2^2 u_3^2 \right]$$

$$m_{\rm u} = 0$$

$$m_{\rm c}^2 = \frac{1}{2} \mathcal{Y}_2^2 \left( u_1^2 + u_2^2 + u_3^2 \right)$$

$$m_{\rm t}^2 = \frac{1}{2} \left[ \mathcal{Y}_1^2 \left( u_1^2 + u_2^2 \right) + \mathcal{Y}_2^2 u_3^2 \right]$$

#### vector-like

quarks!

#### **Down-quark sector (before EWSB):**

#### **Down-quark sector (after EWSB):**

$$M_{\rm d}^{6\times6} = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & d_3\mathcal{Y}_2 & d_2\mathcal{Y}_2 & 0 & 0 & 0\\ -d_3\mathcal{Y}_2 & 0 & -d_1\mathcal{Y}_2 & 0 & 0 & 0\\ -d_2\mathcal{Y}_1 & d_1\mathcal{Y}_2 & 0 & 0 & 0 & 0\\ 0 & s_3\mathcal{Y}_2 & s_2\mathcal{Y}_2 & 0 & p\mathcal{Y}_2 & f\mathcal{Y}_2\\ -s_3\mathcal{Y}_2 & 0 & -\omega\mathcal{Y}_2 & -p\mathcal{Y}_2 & 0 & -s_1\mathcal{Y}_2\\ -s_2\mathcal{Y}_1 & w\mathcal{Y}_1 & 0 & -f\mathcal{Y}_1 & s_1\mathcal{Y}_1 & 0 \end{pmatrix}$$

$$(d_{\mathrm{L}}^{i} \ D_{\mathrm{L}}^{i})^{\top} M_{d} \ (d_{\mathrm{R}}^{i} \ D_{\mathrm{R}}^{i})$$

$$m_{\mathrm{D/S}}^2 \simeq rac{1}{2} (f^2 + p^2) \mathcal{Y}_2^2 \,, \quad m_{\mathrm{S/D}}^2 \simeq rac{\omega^2 (f^2 + p^2 + \omega^2)}{2 (f^2 + \omega^2)} \mathcal{Y}_2^2 \,,$$
 $m_{\mathrm{B}}^2 \simeq rac{1}{2} (f^2 + \omega^2) \mathcal{Y}_1^2 + rac{f^2 p^2}{2 (f^2 + \omega^2)} \mathcal{Y}_2^2 \,.$ 

Scenarios | 
$$\omega$$
 [TeV] |  $f$  [TeV] |  $p$  [TeV] |  $m_{\rm D}$  [TeV]  $m_{\rm S}$  [TeV] |  $m_{\rm B}$  [TeV] |  $\omega \sim f \sim p$  |  $100 - 1000 \ 100 - 1000 \ 100 - 1000$  |  $1 - 10 \ 1 - 10 \ 100 - 1000$  |  $\omega \sim f \ll p$  |  $10 - 100 \ 100 - 1000$  |  $100 - 1000$  |  $1 - 10 \ 100 - 1000$  |  $1 - 10 \ 100 - 1000$  |  $1 - 10 \ 1000$  |  $1 - 10 \ 1000$  |  $1 - 10 \ 1000$  |  $1 - 10 \ 1000$  |  $1 - 10 \ 1000$  |  $1 - 10 \ 1000$  |  $1 - 10 \ 1000$  |  $1 - 10 \ 1000$  |  $1 - 10 \ 1000$  |  $1 - 10 \ 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |  $1 - 1000$  |

light up-type quarks!

$$m_{\rm d} = 0, \qquad m_{\rm s}^2 = \frac{(d_3 f - d_2 p)^2}{2(f^2 + p^2 + \omega^2)} \mathcal{Y}_2^2, \qquad m_{\rm b}^2 = \frac{1}{2} (d_2^2 \mathcal{Y}_1^2 + d_3^2 \mathcal{Y}_2^2)$$

### **Quark mixing**

$$d_1 = 0$$
**CKM mixing:**

$$V_{\text{CKM}} \equiv L_{\text{u}} L_{\text{d}}^{\dagger} = \begin{pmatrix} \frac{d_2 u_2 \mathcal{Y}_1^2 + d_3 u_3 \mathcal{Y}_2^2}{\sqrt{\mathcal{A}\mathcal{B}}} & -\frac{u_1 \mathcal{Y}_1}{\sqrt{\mathcal{A}}} & \frac{(d_2 u_3 - d_3 u_2) \mathcal{Y}_1 \mathcal{Y}_2}{\sqrt{\mathcal{A}\mathcal{B}}} \\ -\frac{d_2 u_1 \mathcal{Y}_1}{\sqrt{\mathcal{B}\mathcal{C}}} & -\frac{u_2}{\sqrt{\mathcal{C}}} & \frac{d_3 u_1 \mathcal{Y}_2}{\sqrt{\mathcal{B}\mathcal{C}}} \\ \frac{(\mathcal{C}d_3 - d_2 u_2 u_3) \mathcal{Y}_1 \mathcal{Y}_2}{\sqrt{\mathcal{A}\mathcal{B}\mathcal{C}}} & \frac{u_1 u_3 \mathcal{Y}_2}{\sqrt{\mathcal{A}\mathcal{C}}} & \frac{\mathcal{C}d_2 \mathcal{Y}_1^2 + d_3 u_2 u_3 \mathcal{Y}_2^2}{\sqrt{\mathcal{A}\mathcal{B}\mathcal{C}}} \end{pmatrix}$$

$$\mathcal{A} = \mathcal{C}\mathcal{Y}_1^2 + u_3^2\mathcal{Y}_2^2$$
,  $\mathcal{B} = d_2^2\mathcal{Y}_1^2 + d_3^2\mathcal{Y}_2^2$ ,  $\mathcal{C} = u_1^2 + u_2^2$ .

For consistency with the up-quark spectrum, we require

$$\mathcal{Y}_2 \ll \mathcal{Y}_1$$

$$V_{tb} \simeq 1 - \left(\frac{\mathcal{Y}_2}{\mathcal{Y}_1}\right)^2 \frac{d_3^2 \mathcal{C} + d_2 u_3 (d_2 u_3 - 2d_3 u_2)}{2d_2^2 \mathcal{C}}$$

#### **Minimal 3HDM limit:**

$$u_3 \to 0$$
  $d_3 \to 0$   $|V_{\text{CKM}}| = \begin{pmatrix} \cos \theta_C & \sin \theta_C & 0 \\ \sin \theta_C & \cos \theta_C & 0 \\ 0 & 0 & 1 \end{pmatrix}$   $\theta_C = \arctan \left(\frac{u_1}{u_2}\right)$ 

Fully compressed  $\omega \sim f \sim p$  scenario

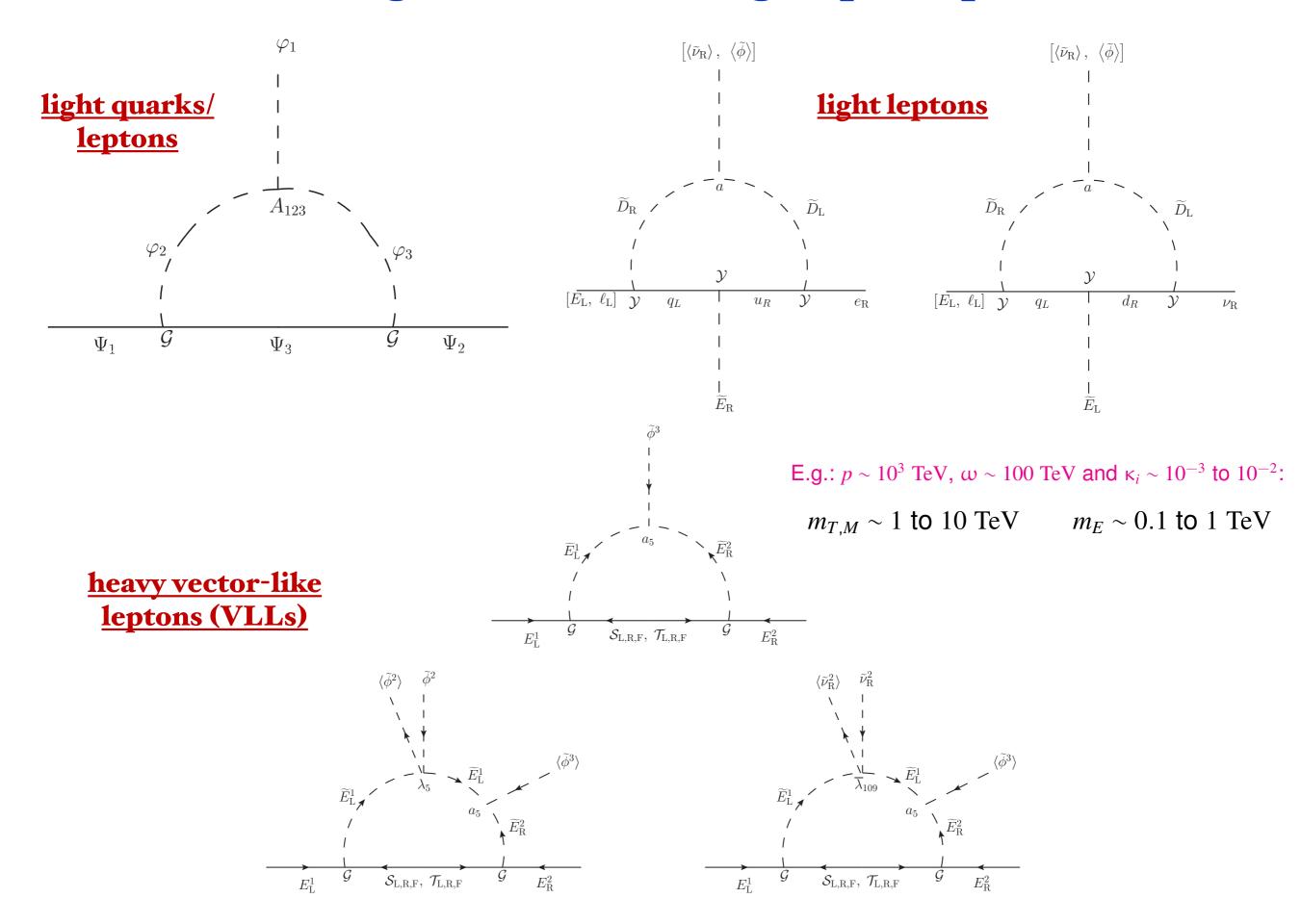
$$p=220~{\rm TeV}\,,~f=210~{\rm TeV}\,,~\omega=200~{\rm TeV}$$

$$m_{\rm s} = 0.017 \,{\rm GeV}\,, \ m_{\rm b} = 4.15 \,{\rm GeV}\,, \ m_{\rm D} = 1.3 \,{\rm TeV}\,, \ m_{\rm S} = 1.5 \,{\rm TeV}\,, \ m_{\rm B} = 211.0 \,{\rm TeV}$$

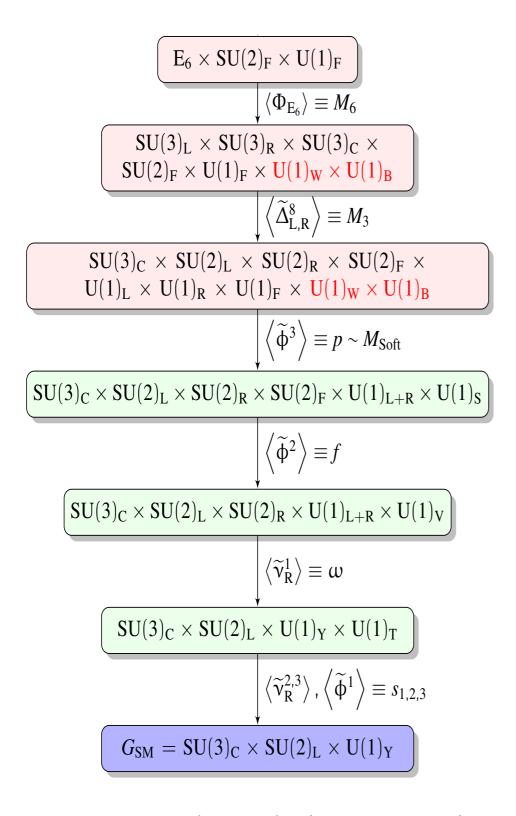
$$|V_{\text{CKM}}| \simeq \begin{pmatrix} 0.97 & 0.24 & 2.31 \times 10^{-5} & 4.36 \times 10^{-6} & 7.29 \times 10^{-7} & \sim 0 \\ 0.24 & 0.97 & 9.23 \times 10^{-5} & 1.74 \times 10^{-5} & 2.92 \times 10^{-6} & \sim 0 \\ 0 & 9.51 \times 10^{-5} & 1 & 5.55 \times 10^{-5} & 1.15 \times 10^{-5} & 6.47 \times 10^{-7} \end{pmatrix}$$

Good opportunity to probe the model at the LHC or future colliders

### Radiative generation of charge lepton spectra



#### **Emergence of SM-like EFT**



#### No proton decay below E6 scale!

$$\mathbb{P}_{B}$$
-parity  $\mathbb{P}_{B} = (-1)^{2W+2S} = (-1)^{3B+2S}$ 

- SUSY theory, broken SUSY, broken flavour
- Between  $M_6$  and  $M_3$ : Steep running due to  $\Psi$ ,  $\Sigma$ ,  $\Sigma'$
- Between  $M_3$  and  $M_{\rm Soft}$ : Trinification running including L,  $Q_{\rm L}$ ,  $Q_{\rm R}$ ,  $\Delta_{\rm L.R.C}$
- Soft scales compressed  $s = \omega = f = p$

#### Low scale $G_{\rm SM}$ theory

- Three Higgs doublets 3HDM
- Two generations of VLQ below the soft scale
- Three generations of VLL below the soft scale

$$M_{\rm S} \lesssim 10^3 \ {
m TeV}, \quad M_{\rm GUT} = 10^{16} - 10^{18} \ {
m GeV} \quad M_{\rm EW} \ll M_{
m S}$$

 $\log_{10}(\mu/{\rm GeV})$ 

### **Concluding remarks**

 We developed a novel Flavoured Trinification GUT framework giving rise to a SM-like EFT, with a realistic flavour structure in charged fermion and neutrino sectors

 The framework offers interesting implications for flavour and collider physics, primarily through vector-like fermions and scalar leptoquarks (LQs)