

# Temperature Evolution in the Early Universe and Freeze-in at stronger coupling

**Catarina M. Cosme**

in collaboration with  
Francesco Costa and Oleg Lebedev

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**Multi Higgs Workshop, Instituto Superior Técnico, Lisboa, Portugal, 26 August 2026**

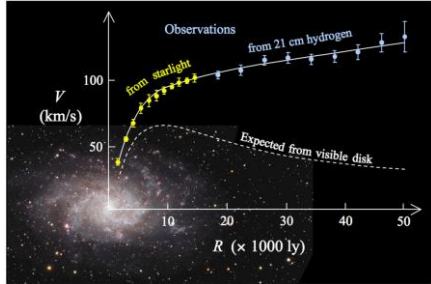


# Outline

- **Introduction**
  - Evidence for the existence of Dark Matter
  - Dark matter production mechanisms
- **The model – Freeze-in at stronger coupling**
- **Phenomenology**
  - Detection prospects
- **Temperature evolution and its consequences**
- **Conclusions**

# Introduction - Dark Matter (DM)

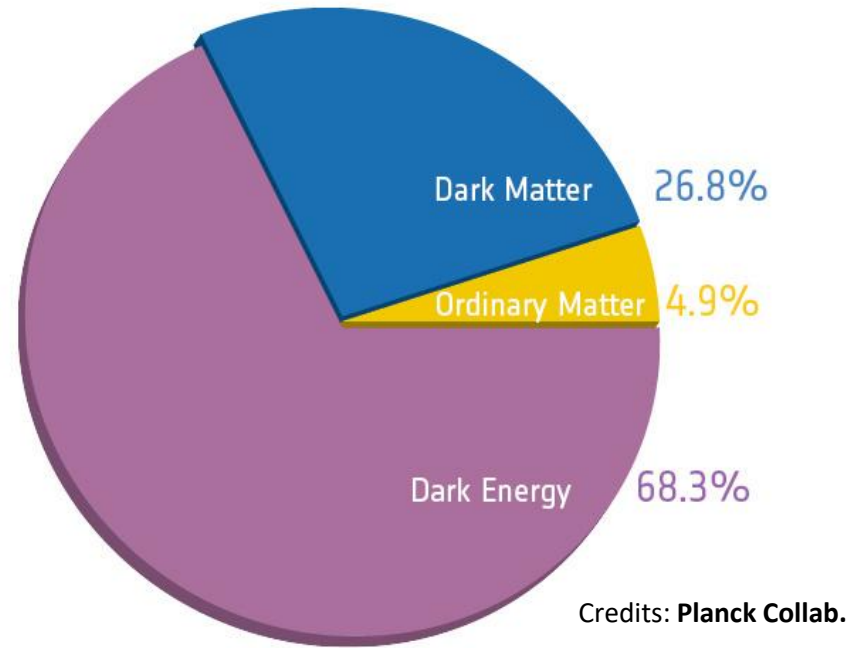
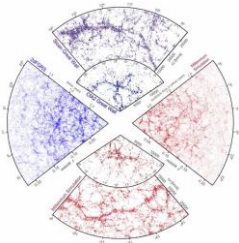
## Galaxy Rotation Curves



## Merging clusters (Bullet Cluster)



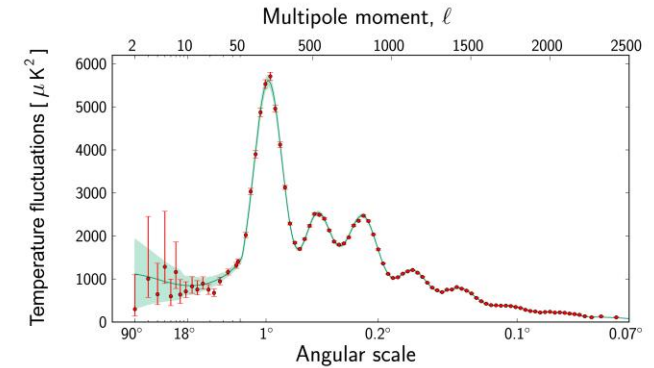
## Structure formation



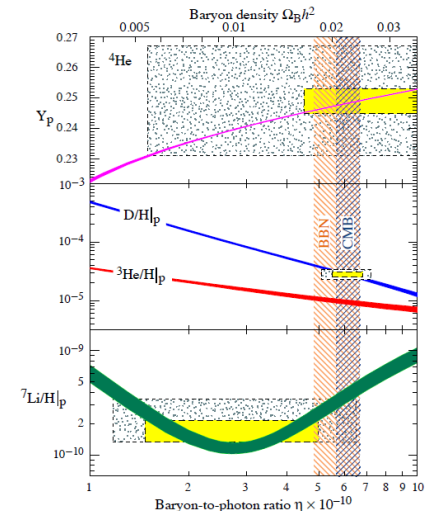
## Properties of a DM candidate

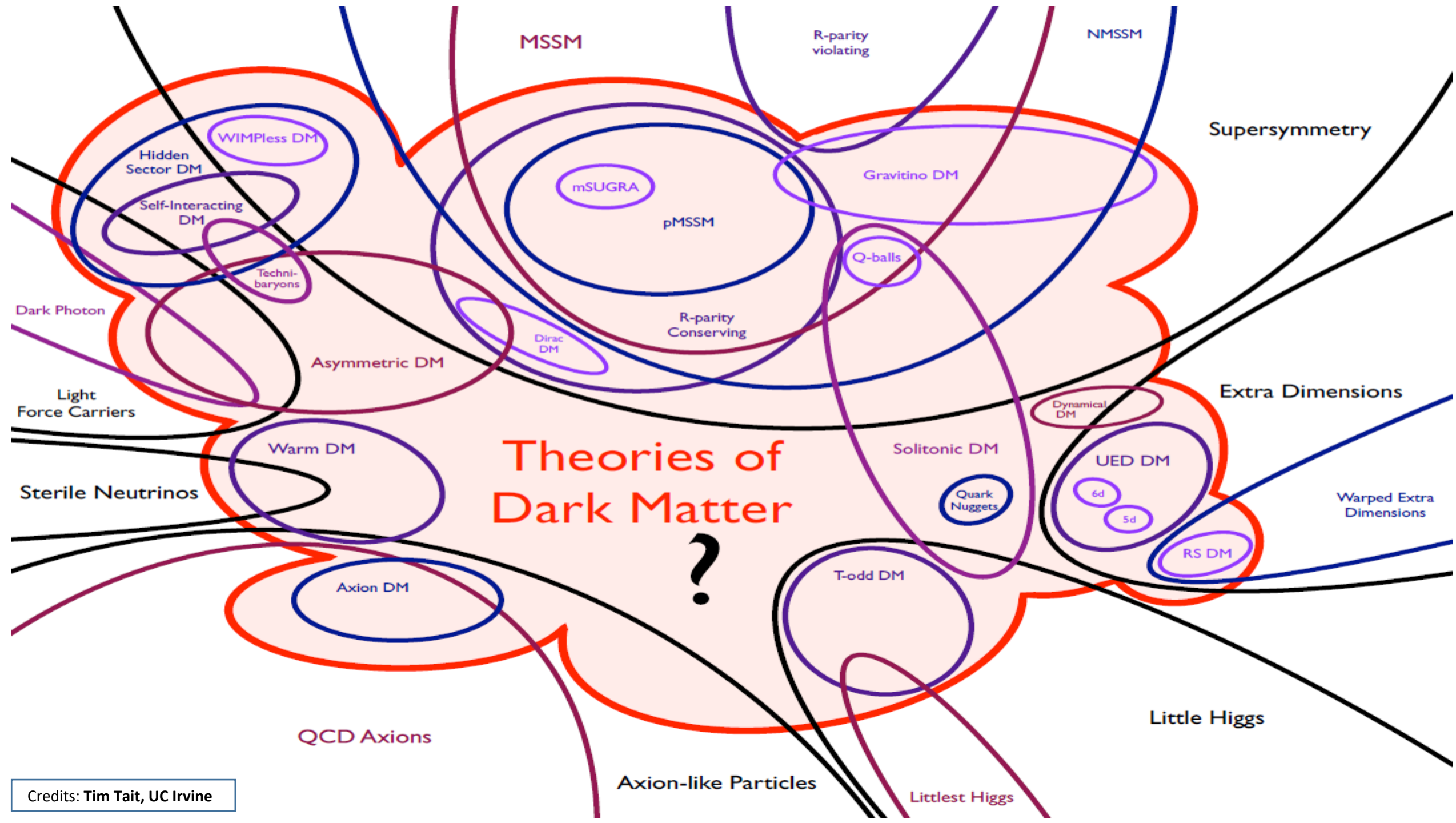
- Stable or very long-lived (lifetime  $\geq$  age of the Universe);
- Cold (non-relativistic);
- Very small interaction with the electromagnetic field;
- It must have the observed abundance.

## Cosmic Microwave Background (CMB)



## Big Bang Nucleosynthesis (BBN)





# Introduction – Dark Matter production mechanisms

**Freeze-out mechanism (Weakly Interacting Massive Particles – WIMPs)**

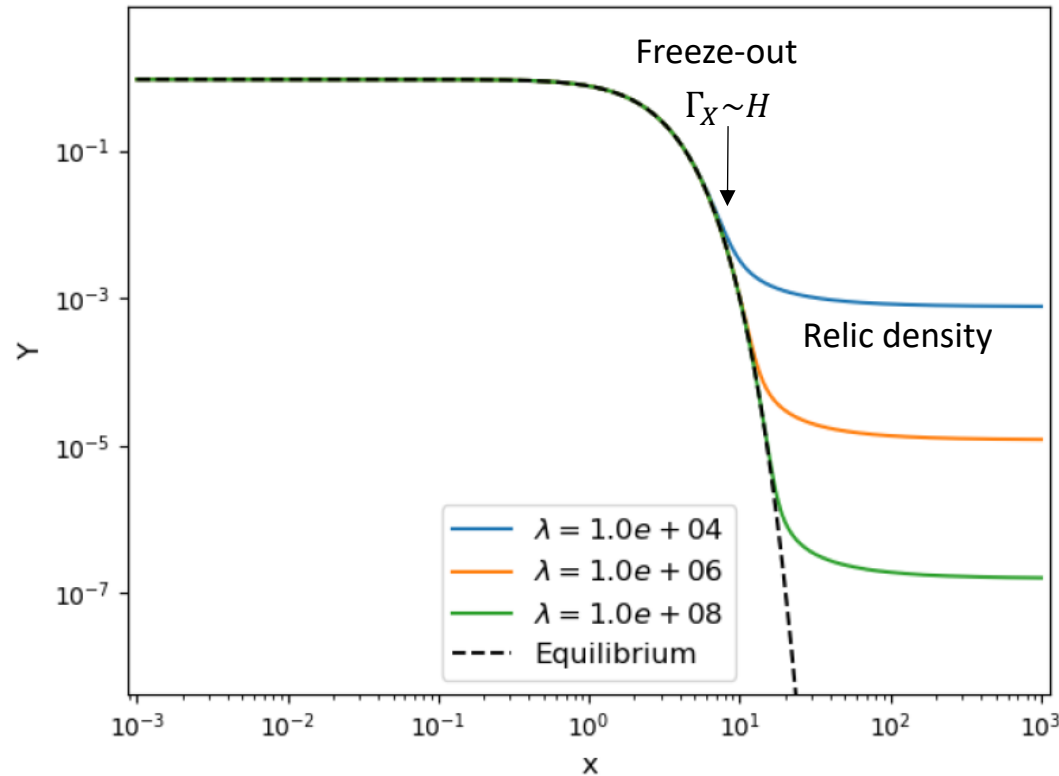
# Introduction – Dark Matter production mechanisms

## Freeze-out mechanism (Weakly Interacting Massive Particles – WIMPs)

$$X\bar{X} \leftrightarrow SM$$

# Introduction – Dark Matter production mechanisms

## Freeze-out mechanism (Weakly Interacting Massive Particles – WIMPs)



$$Y \equiv \frac{n_X}{s}, \quad x \equiv \frac{m}{T}$$

$$X\bar{X} \leftrightarrow SM$$

Dark Matter (DM) **evolution**:

$$\frac{dn_X}{dt} + 3Hn_X = -\langle\sigma v\rangle\left(n_X^2 - (n_X^{eq})^2\right)$$

Interactions **freeze-out** when:

$$\Gamma_X = n_X\langle\sigma v\rangle \lesssim H$$

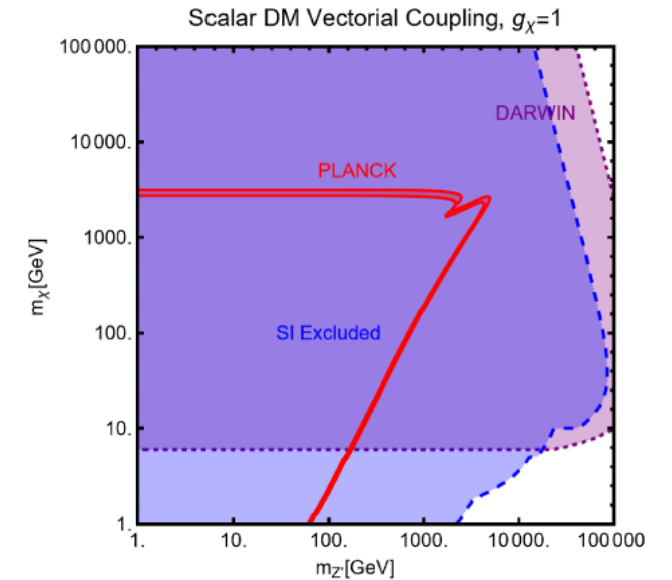
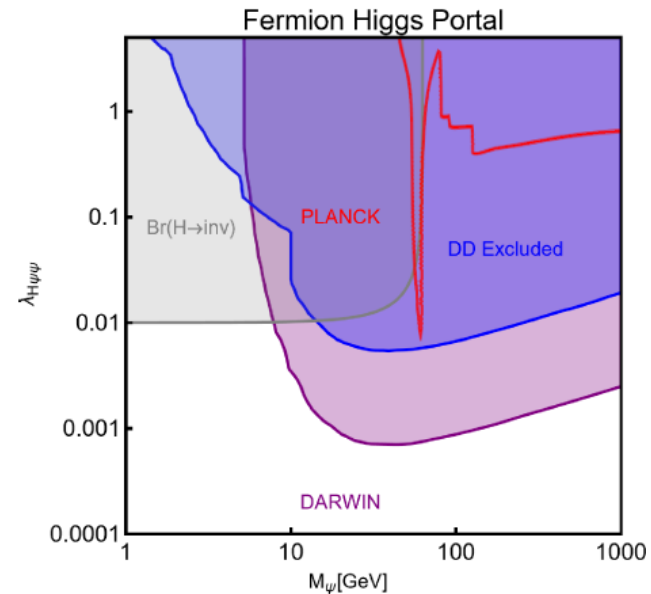
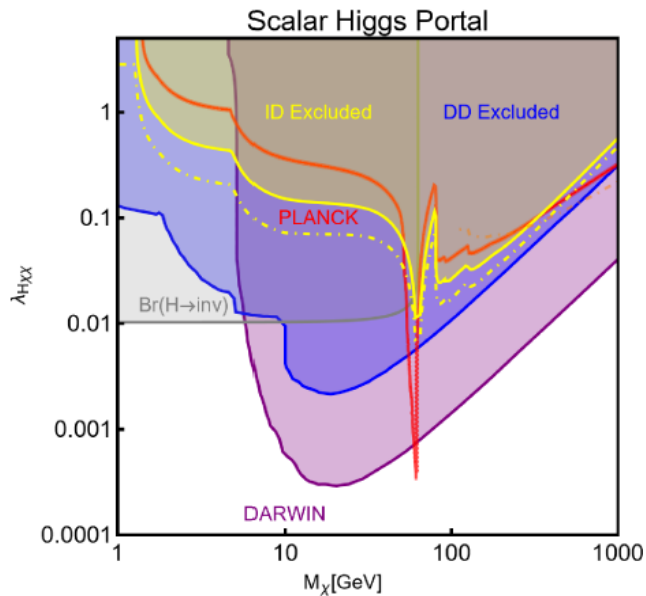
Present DM **abundance**:

$$\Omega_{X,0}h^2 \equiv \frac{\rho_{X,0}}{\rho_{c,0}/h^2} \sim \frac{1}{\langle\sigma v\rangle} \sim \frac{1}{\lambda}$$

# Introduction – Dark Matter production mechanisms

## Freeze-out mechanism

- **WIMPs** – no detection so far; very constrained by experiments.

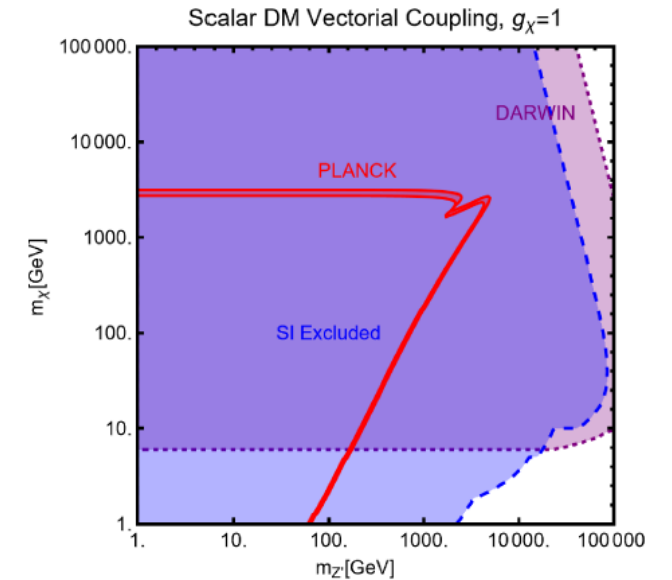
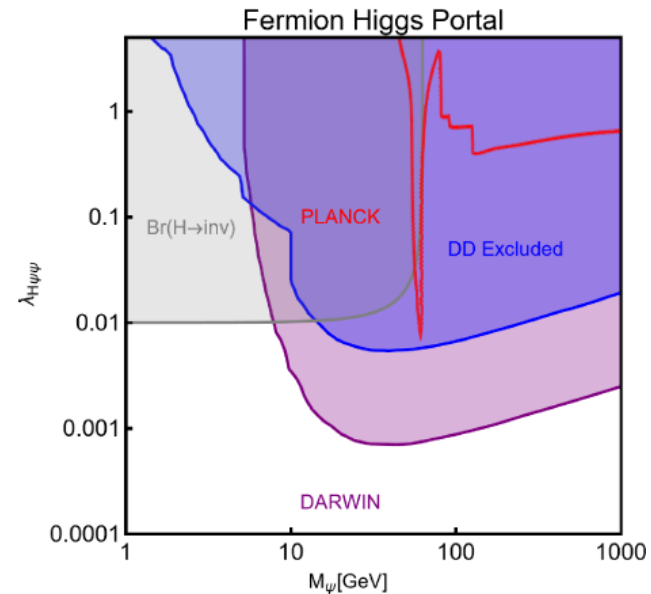
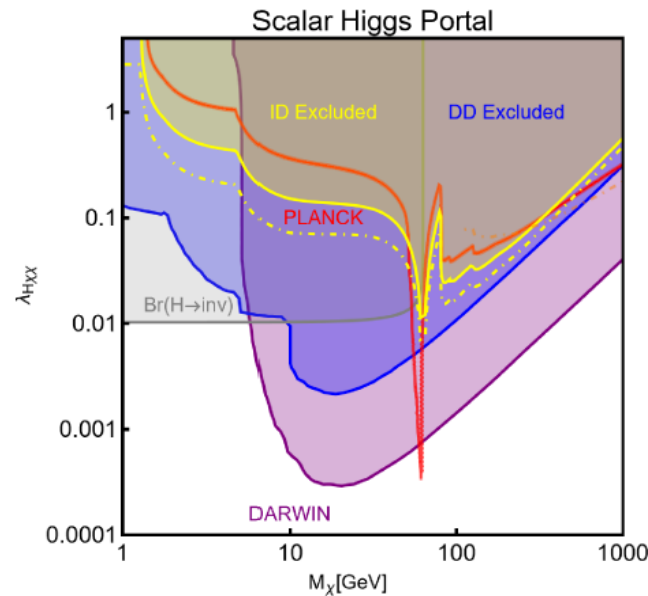


Credits: Arcadi et. al, arXiv:2403.15860

# Introduction – Dark Matter production mechanisms

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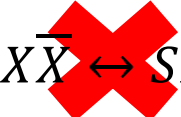
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“The waning of the WIMP?”

# Introduction - Dark Matter production mechanisms

$$X\bar{X} \leftrightarrow SM$$

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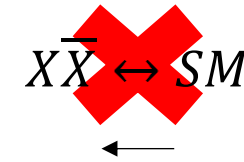
# Introduction – Dark Matter production mechanisms

**Freeze-in mechanism – Feebly Interacting Massive Particles (FIMPs)**

$$X\bar{X} \leftrightarrow SM$$

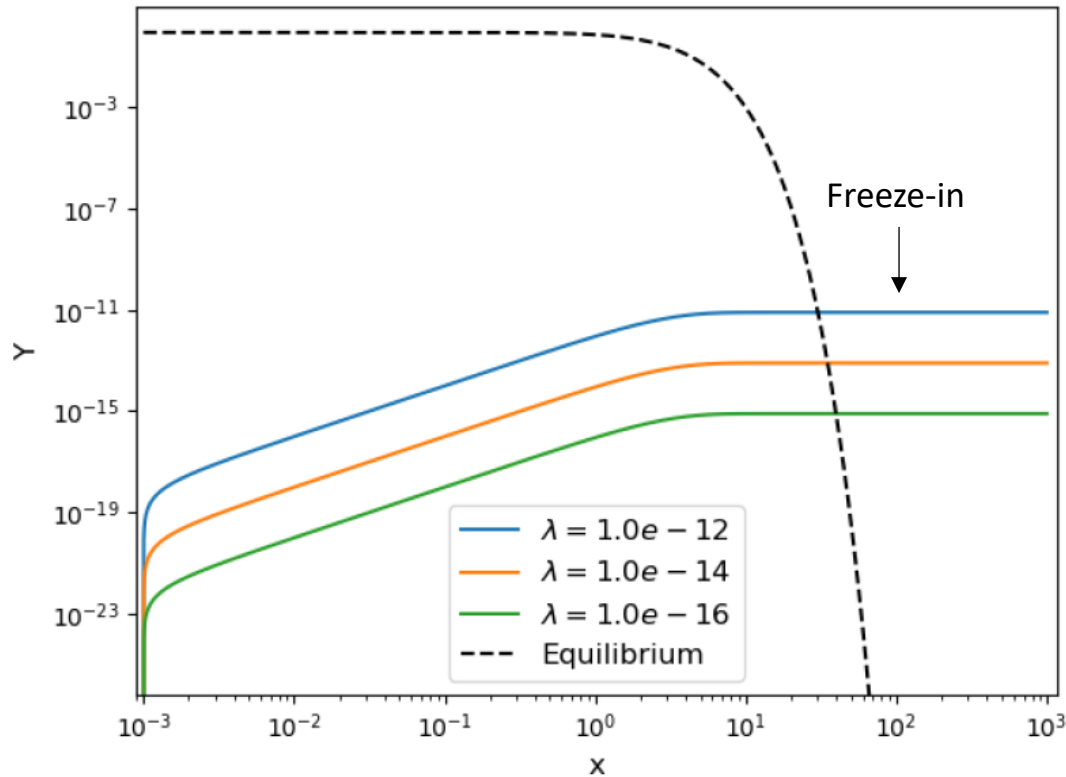
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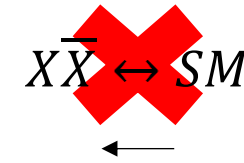

$$X\bar{X} \leftrightarrow SM$$

# Introduction - Dark Matter production mechanisms

## Freeze-in mechanism - Feebly Interacting Massive Particles (FIMPs)



$$Y \equiv \frac{n_X}{s}, \quad x \equiv \frac{m}{T}$$



DM evolution:

$$\frac{dn_X}{dt} + 3Hn_X = 2\Gamma_{\sigma \rightarrow XX} \frac{K_1(m_\sigma/T)}{K_2(m_\sigma/T)} n_\sigma^{eq}$$

Interactions rate:

$$\Gamma_X < H \text{ always}$$

Present DM abundance:

$$\Omega_{X,0} h^2 \sim \Gamma_{\sigma \rightarrow XX} \sim \lambda$$

# Introduction – Dark Matter production mechanisms

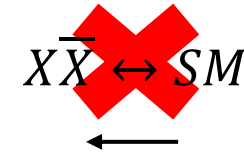
## Freeze-out

$$X\bar{X} \leftrightarrow SM$$

- Interactions **freeze-out** when:  $\Gamma_X = n_X \langle \sigma v \rangle \lesssim H$ ;
- **WIMPs** – Weakly Interacting Massive Particles;
- $\Omega_{X,0} h^2 \sim \frac{1}{\lambda}$ ;
- But:
  - **no detection** so far;
  - Large parameter space **very constrained by experiments.** [Arcadi et al. arXiv:2403.15860]

vs

## Freeze-in



- $\Gamma_X < H$  **always**;
- **FIMPs** – Feebly Interacting Massive Particles;
- $\Omega_{X,0} h^2 \sim \lambda$ ;
- **Small couplings** to attain the **observed relic abundance**;
- Can evade stringent observational constraints;
- But: **hard to probe.**

# Introduction – Dark Matter production mechanisms

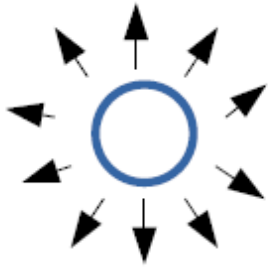
## Freeze-in mechanism challenges:

- 1 – **Small** couplings (hard to probe);
- 2 – Assumes **zero** (or negligible) **initial dark matter** abundance;

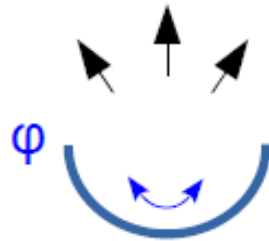
**How can we probe FIMPs?**

# Particle Production Background

**Feeble coupled particles** can be copiously **produced during and after inflation** (all add up):



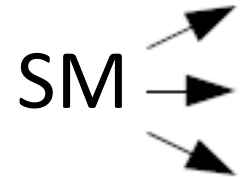
Scalar  
fluctuations



Inflaton  
oscillations



Inflaton  
decay



Freeze-in

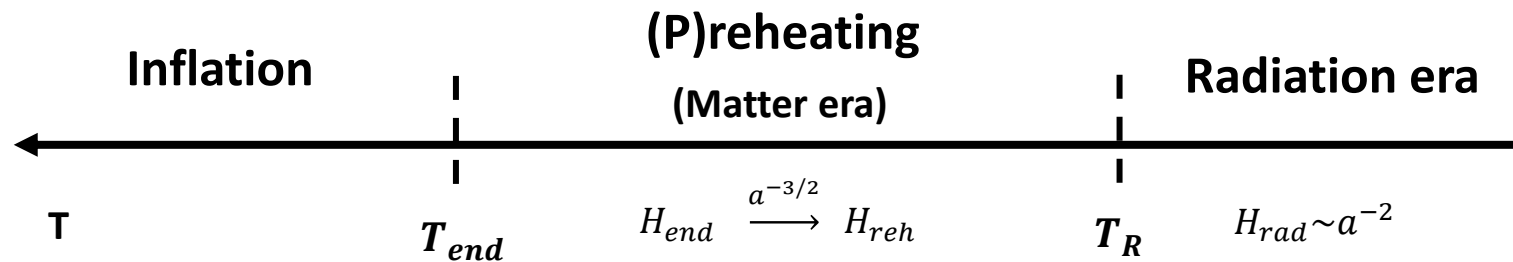
- Very small (**feeble**) couplings to other particles  $\Rightarrow$  **No thermal equilibrium**;
- Even if there are **no couplings** to other fields, **gravitational particle production** is still **on**!

# The model – Freeze-in at stronger coupling

How do we get rid of the excess of dark relics?



→ inflaton,  $\phi$ , oscillating in a quadratic potential,  $\frac{1}{2}m_\phi^2\phi^2$ , **behaves like matter**



$$\rho_\phi \propto a^{-3}, \rho_{rel\ relic} \propto a^{-4} \Rightarrow \frac{\rho_{rel\ relic}}{\rho_\phi} \propto a^{-1}$$

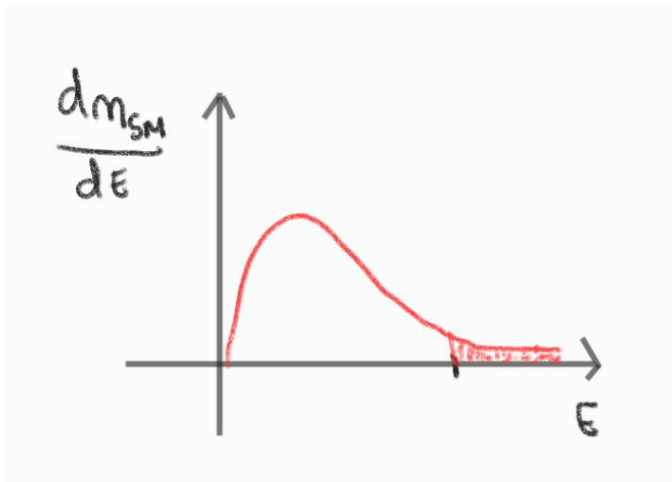
**Dilution of the relics:**  $\Delta_{NR} \equiv \left(\frac{H_{end}}{H_{reh}}\right)^{1/2} > 1$  → **lower reheating temperature,  $T_R$**

# The model – Freeze-in at stronger coupling

- Our model: **DM freeze-in** production, in the range  $T_R < m_{DM}$

If  $T_R < m_{DM}$ :

Only particles at the **Boltzmann tail**,  $E/T \gg 1$ , have **energy to produce DM**



**Boltzmann-suppressed** DM production requires a  
**stronger coupling**



**Testable!**

# The model – Scalar DM Higgs portal

Real scalar dark matter  $s$  through the **Higgs portal**

$$V(s) = \frac{1}{2} \lambda_{hs} s^2 H^\dagger H + \frac{1}{2} m_s^2 s^2$$

$$T_R < m_s$$

DM number density,  $n$ :

$$\dot{n} + 3Hn = \Gamma(h_i h_i \rightarrow ss) - \Gamma(ss \rightarrow h_i h_i)$$

$$\Gamma(ss \rightarrow h_i h_i) = \langle \sigma(ss \rightarrow h_i h_i) v_r \rangle n^2$$

# The model – Negligible DM Annihilation

$$\dot{n} + 3Hn = \Gamma(h_i h_i \rightarrow ss) - \Gamma(ss \times h_i h_i)$$

Solve the Boltzmann equation:

$$\frac{n}{T^3} = \int_{T_R}^0 - \frac{\Gamma(h_i h_i \rightarrow ss)}{HT^4} dT$$

$$\Gamma(h_i h_i \rightarrow ss) \simeq \frac{\lambda_{hs}^2 T^3 m_s}{2^7 \pi^4} e^{-2m_s/T}$$

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$$Y_{DM} \equiv \frac{n}{s} = \frac{\sqrt{90} 45}{2^9 \pi^7 g_*^{3/2}} \frac{\lambda_{hs}^2 M_{Pl}}{T_R} e^{-2m_s/T_R}$$



$$\lambda_{hs} \simeq 3 \times 10^{-11} e^{m_s/T_R} \sqrt{\frac{T_R}{m_s}}$$

$$Y_{obs} = 4.4 \times 10^{-10} \left( \frac{GeV}{m_s} \right)$$

Freeze-in case

# The model – Thermalization requirement

Real scalar dark matter  $s$  through the **Higgs portal**

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Only **thermalizes** if

$$\Gamma(h_i h_i \rightarrow ss) = \Gamma(ss \rightarrow h_i h_i)$$

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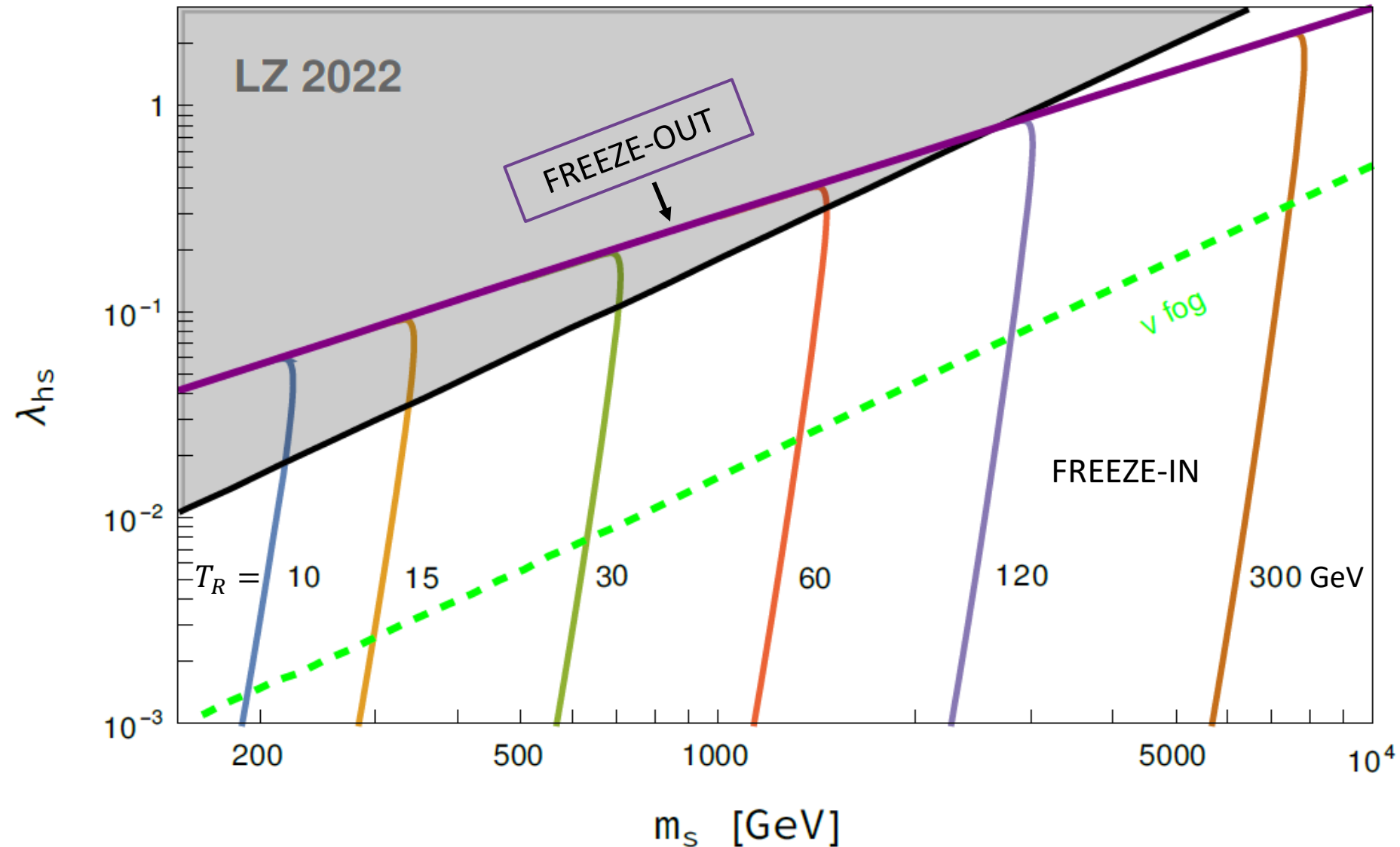
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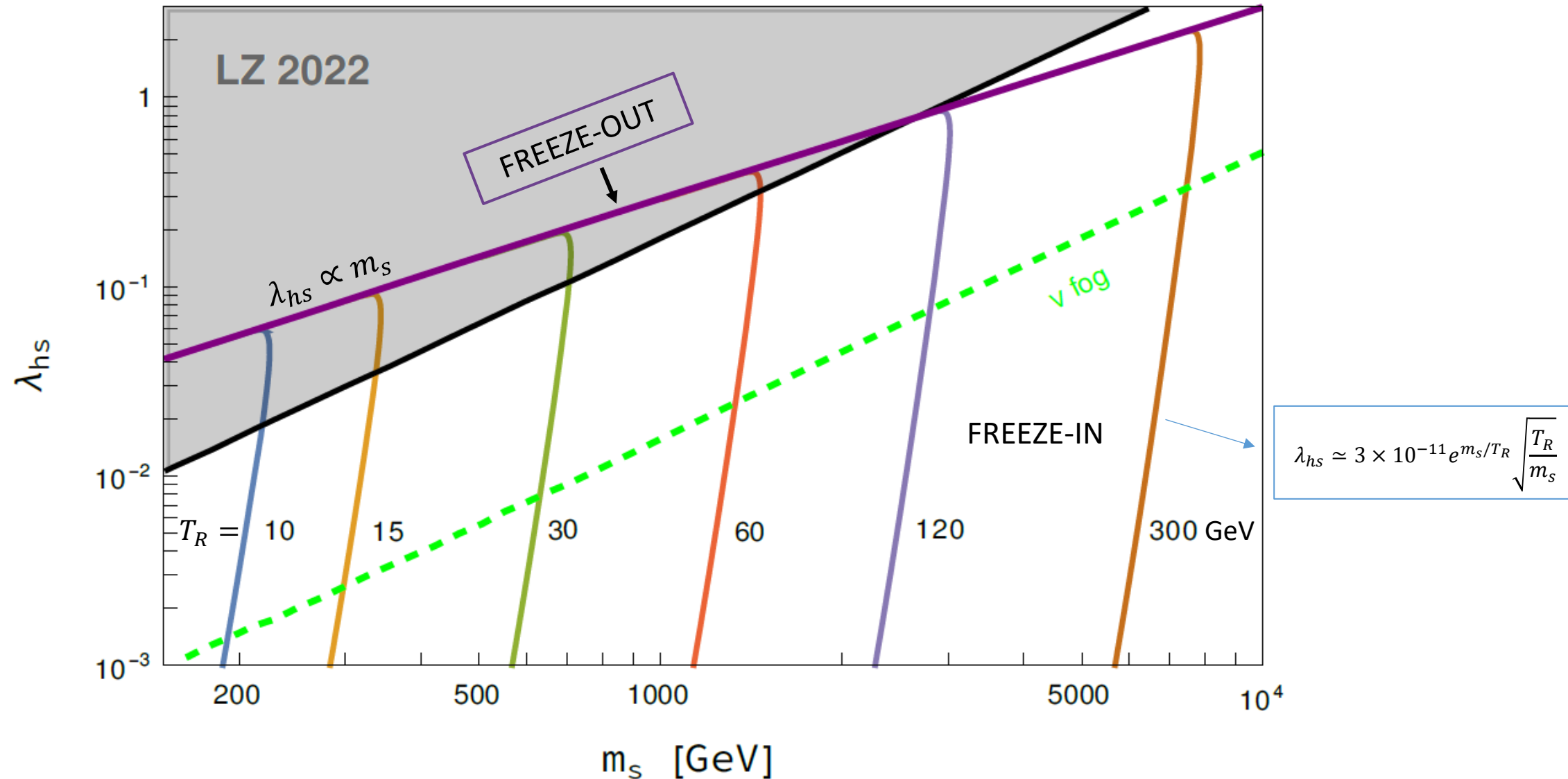
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Freeze-out case

# Phenomenology – Direct detection prospects

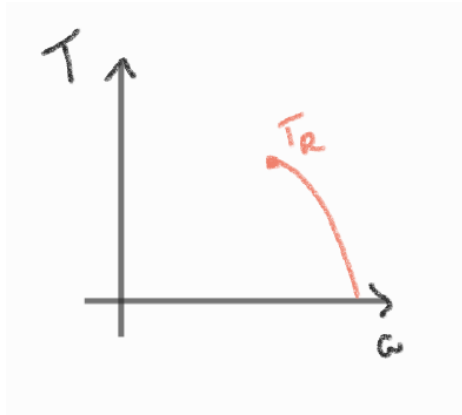


# Phenomenology – Direct detection prospects



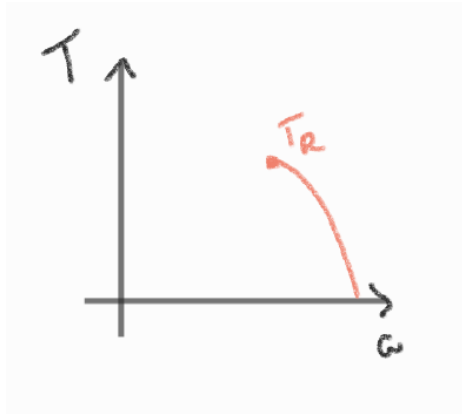
# What if reheating is not instantaneous?

So far, we are considering that most of **DM** is **produced** at  $T_R$ :

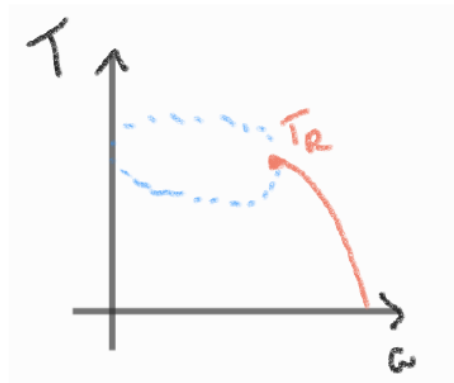


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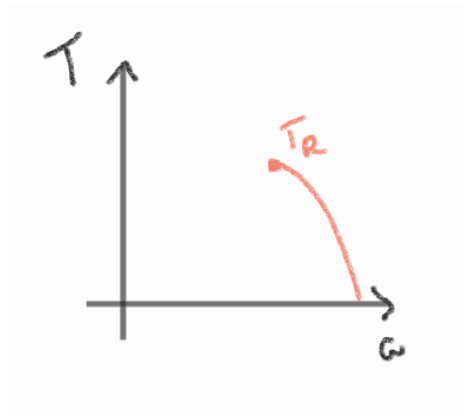


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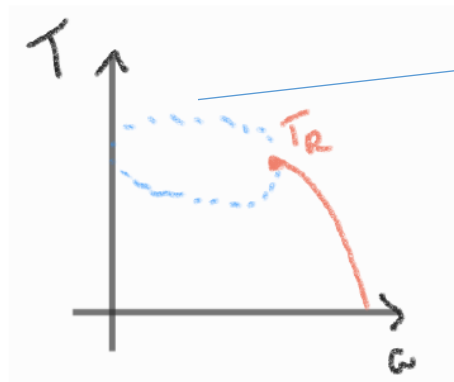


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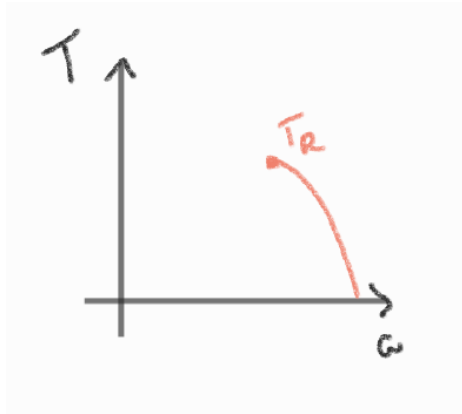
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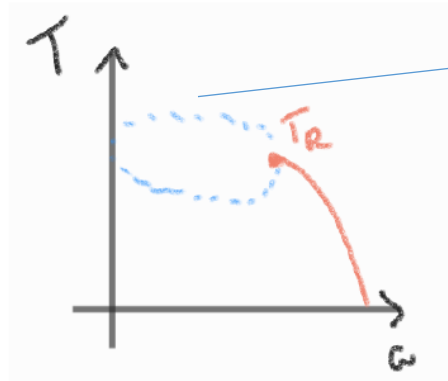
Assumption: in [CC, Costa, Lebedev, 2306.13061], **preexisting DM** abundance can be **neglected**

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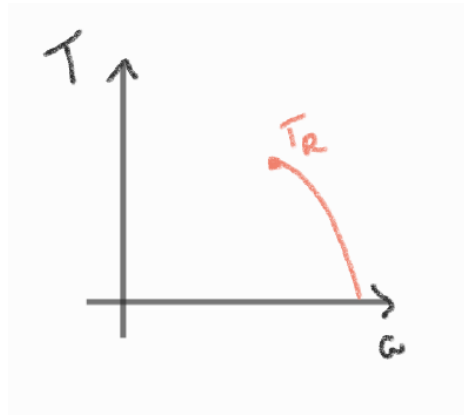


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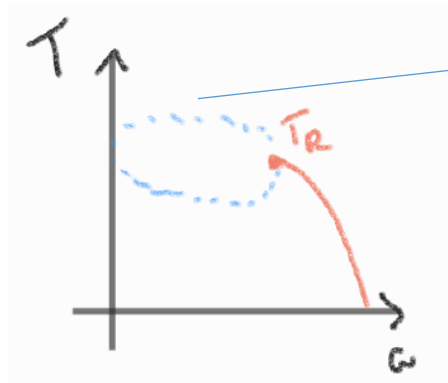
Is this an **adequate** assumption?

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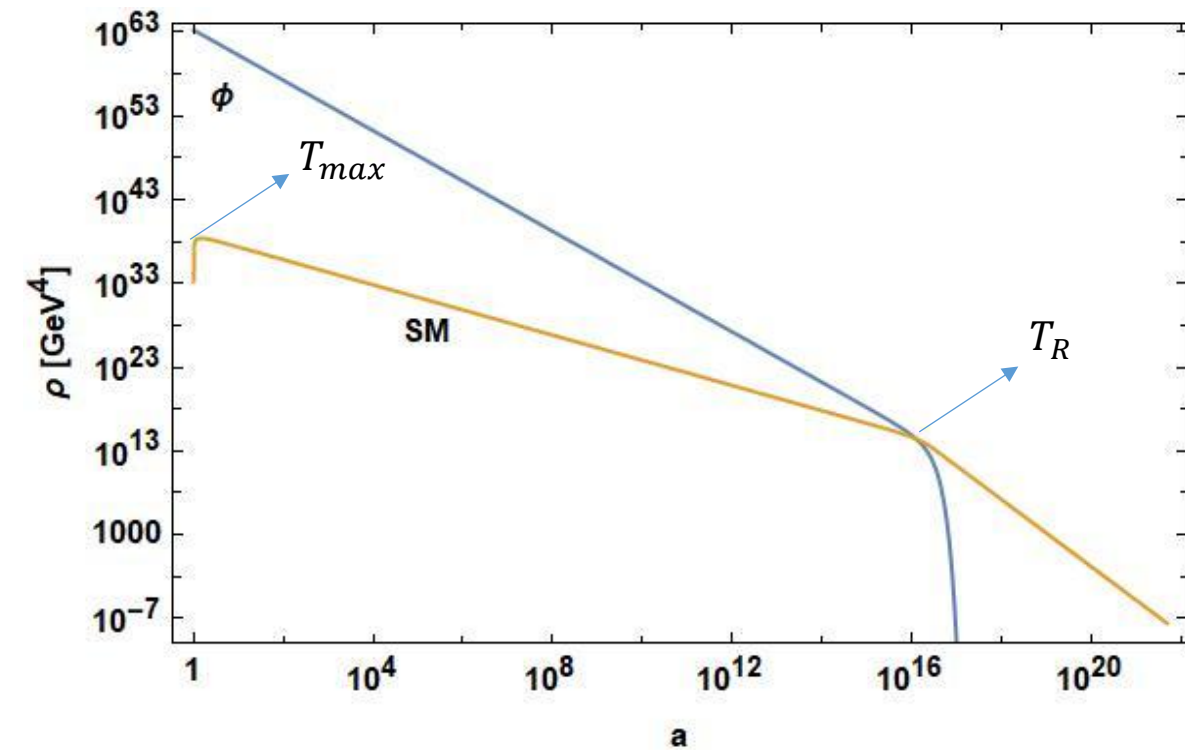
[CC, Costa, Lebedev, 2402.04743]



**Evolution** of the **SM** temperature and its consequences for **freeze-in** at **stronger coupling**

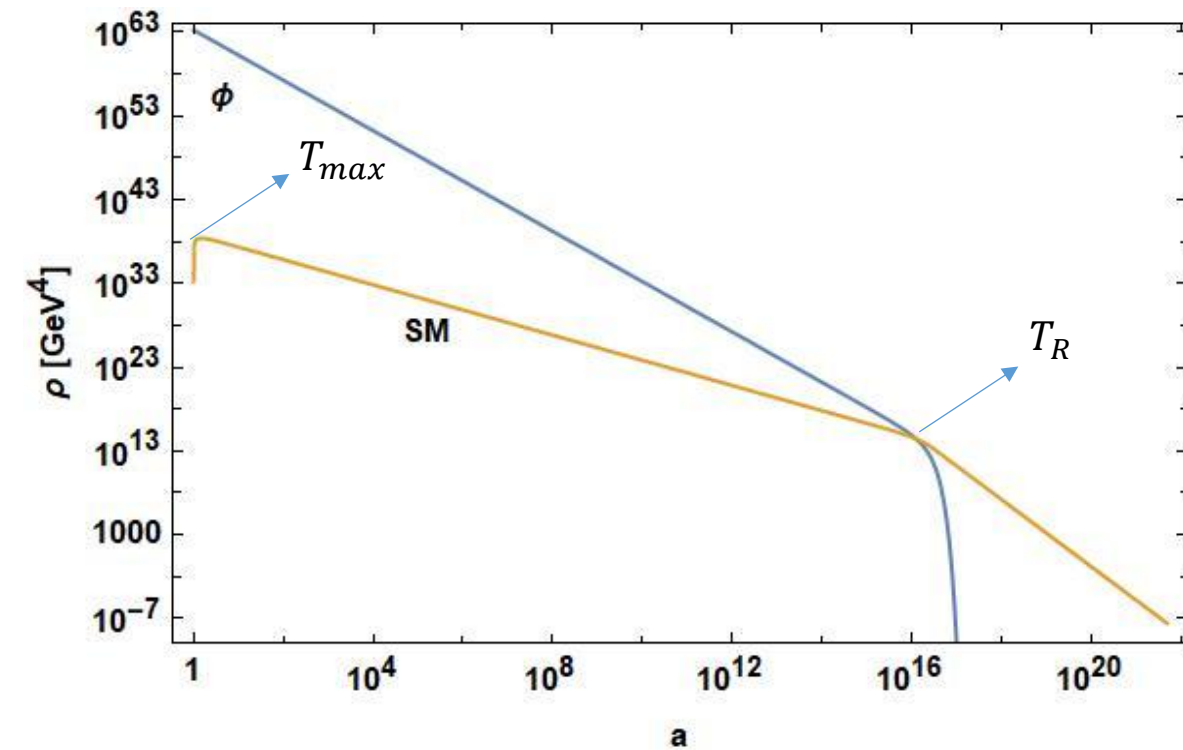
# $T_{max}$ and $T_R$

$$\varphi \rightarrow SM$$



# $T_{max}$ and $T_R$

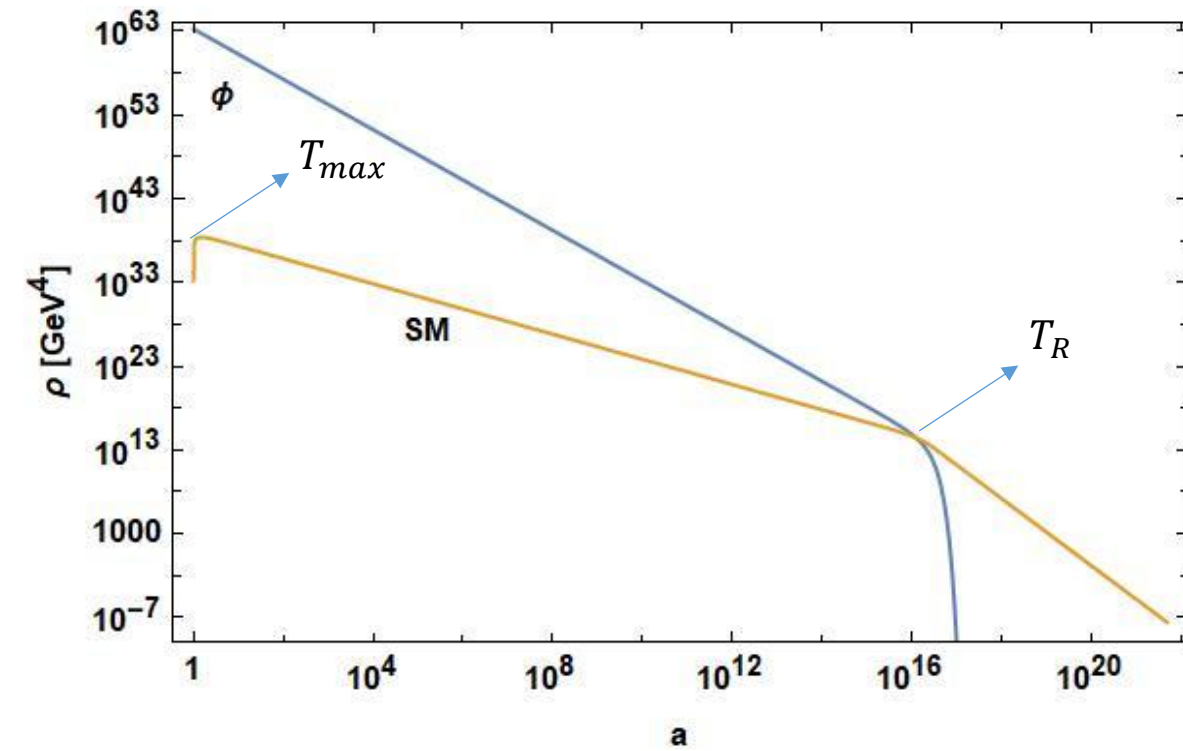
$$\varphi \rightarrow SM$$



$$T_{max} \gg T_R$$

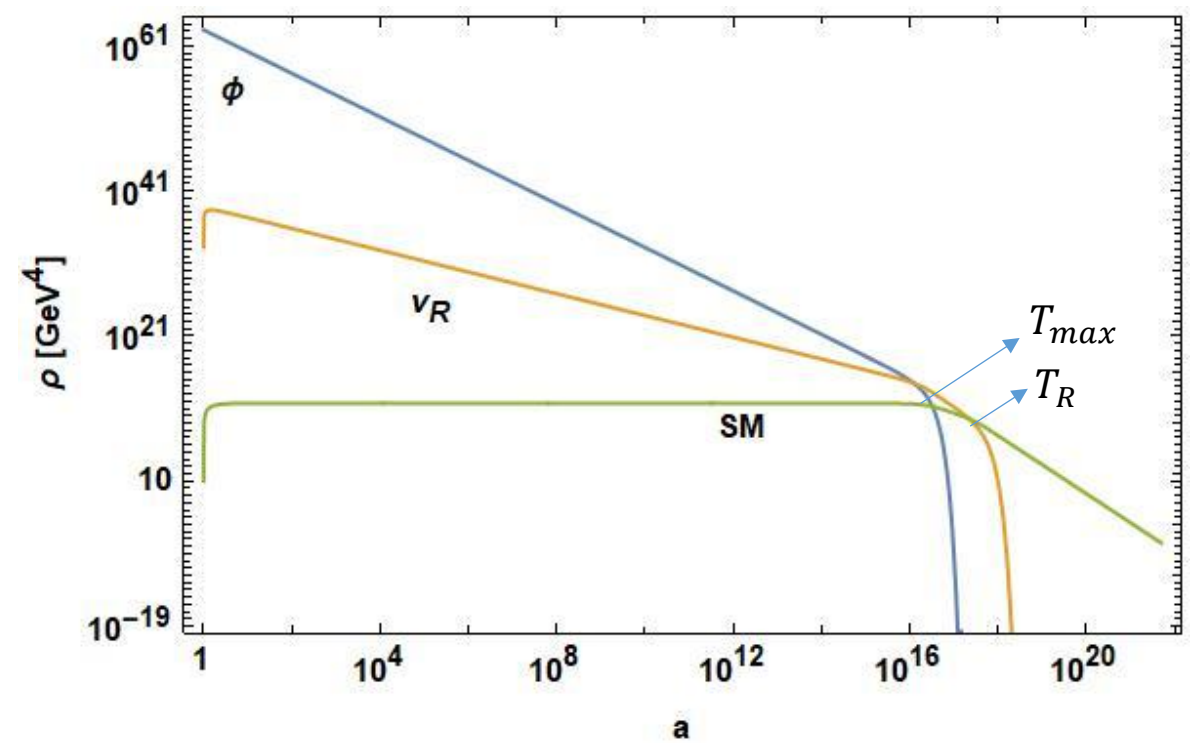
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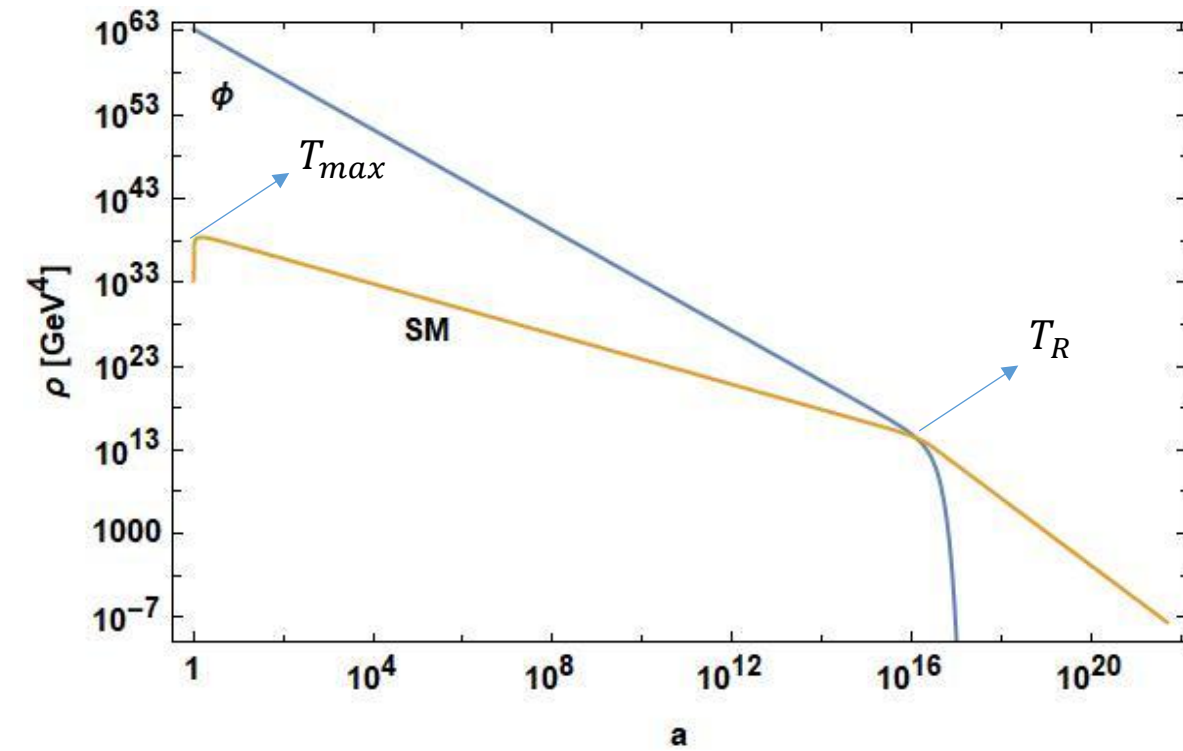
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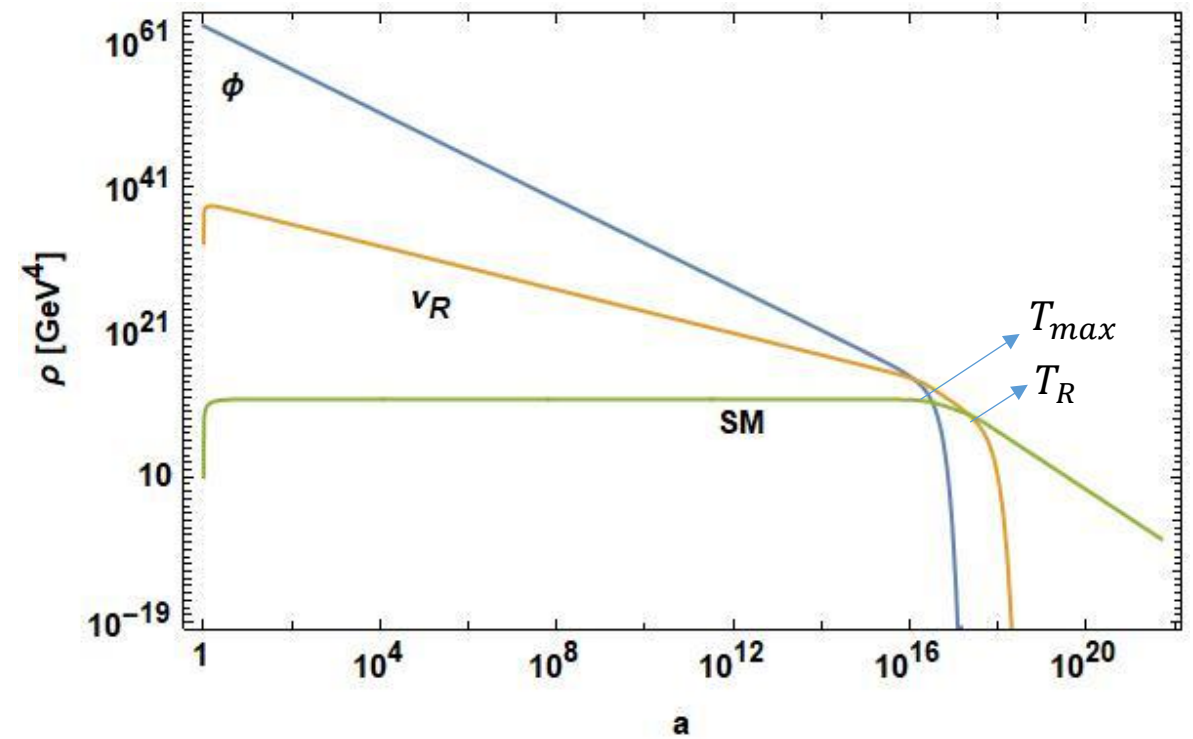
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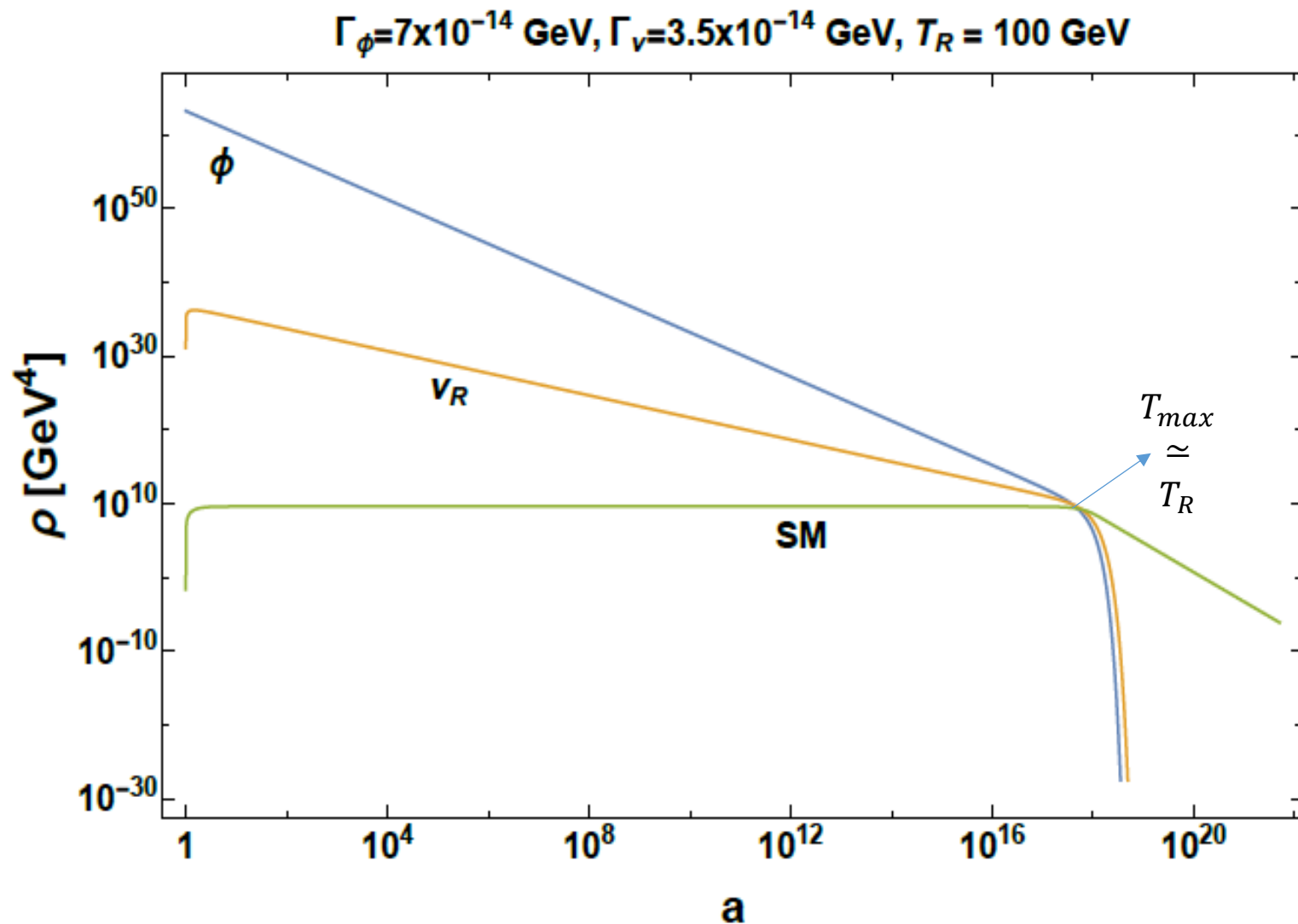
$T_{max} \gg T_R$

$\varphi \rightarrow \nu_R \rightarrow SM$



$T_{max} \simeq T_R$

# SM sector production via $\nu_R$ decay



If  $\Gamma_\phi \sim \Gamma_\nu$

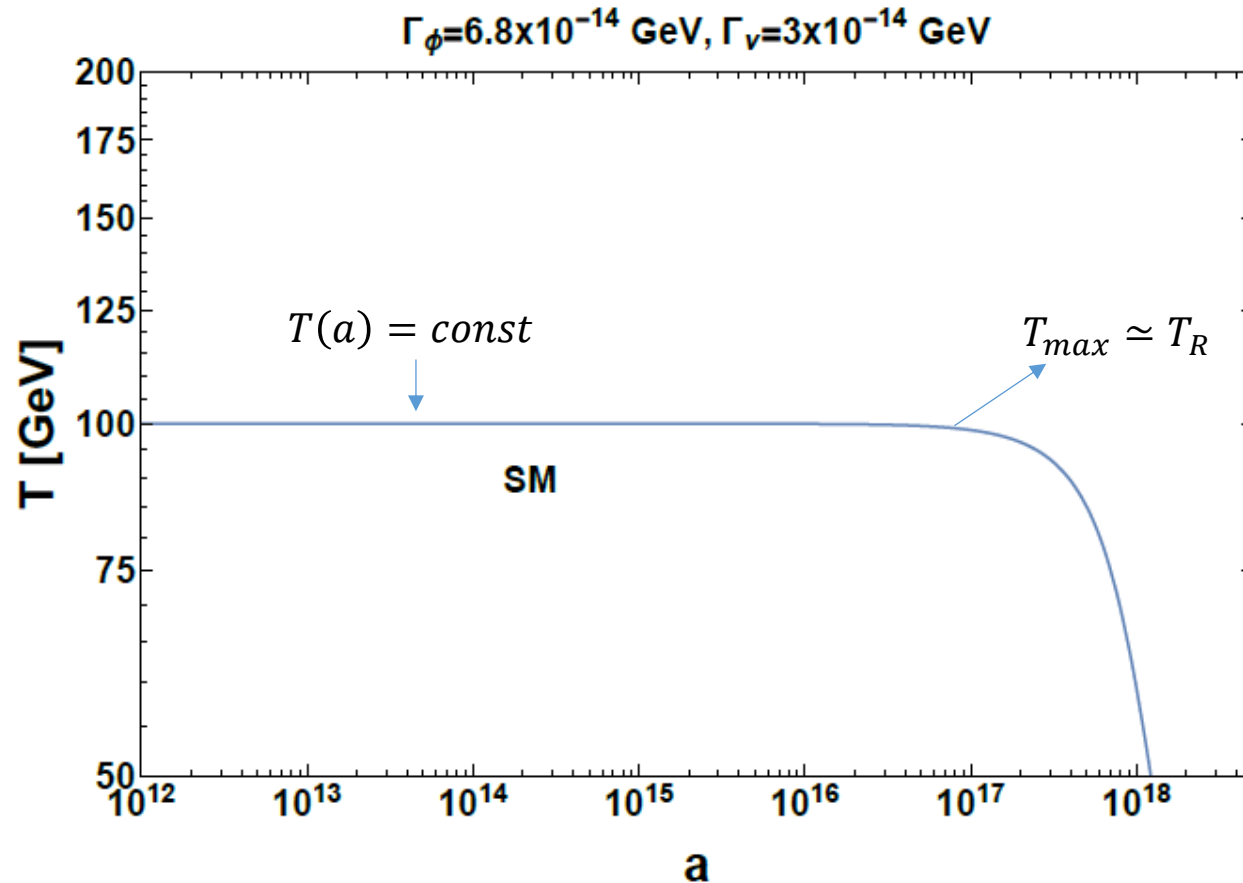


$\phi$  and  $\nu_r$  decay at the same time



$T_{max} \simeq T_R$

# DM abundance



## Total DM particle number

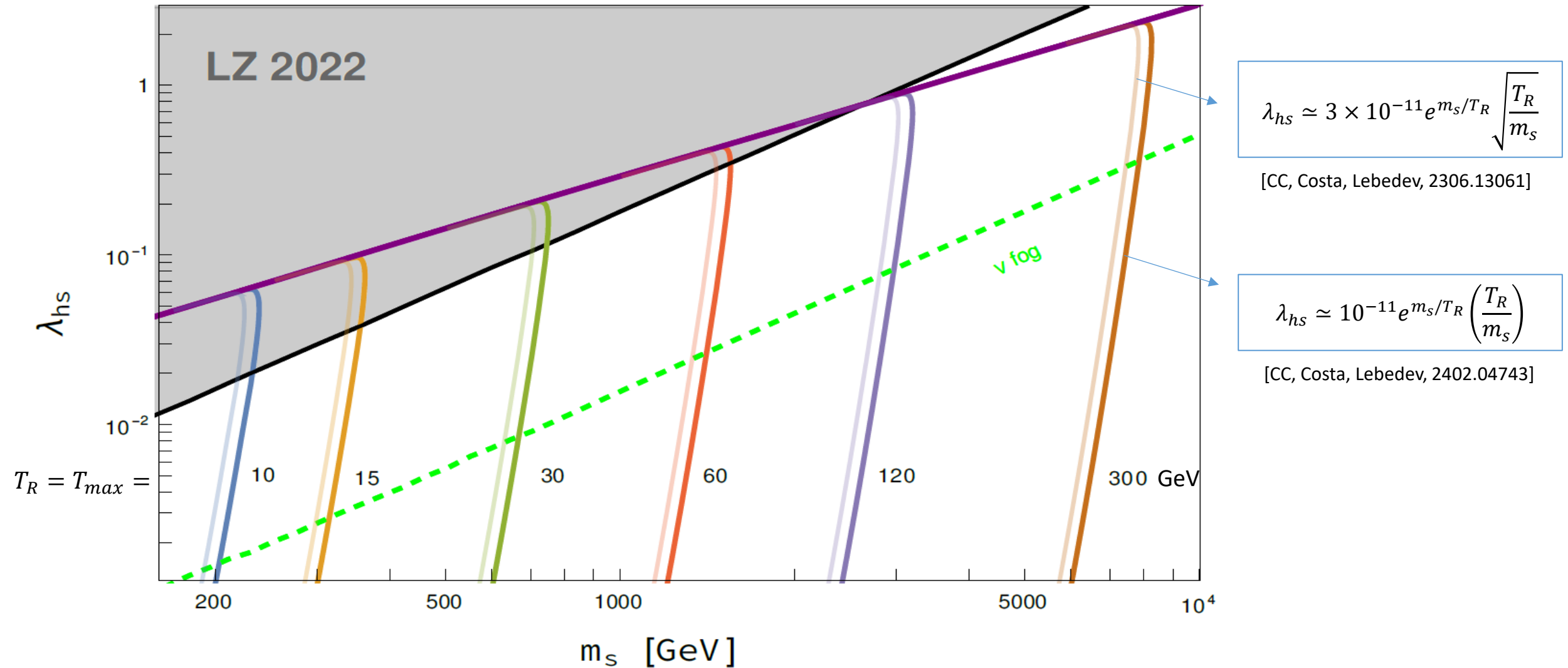
$$a^3 n|_{\text{total}} = a_{\text{max}}^3 n(a_{\text{max}})|_{T=\text{const}} \left( 1 + (m+3) \frac{T_{\text{max}}}{2m_s} \right)$$

## DM yield

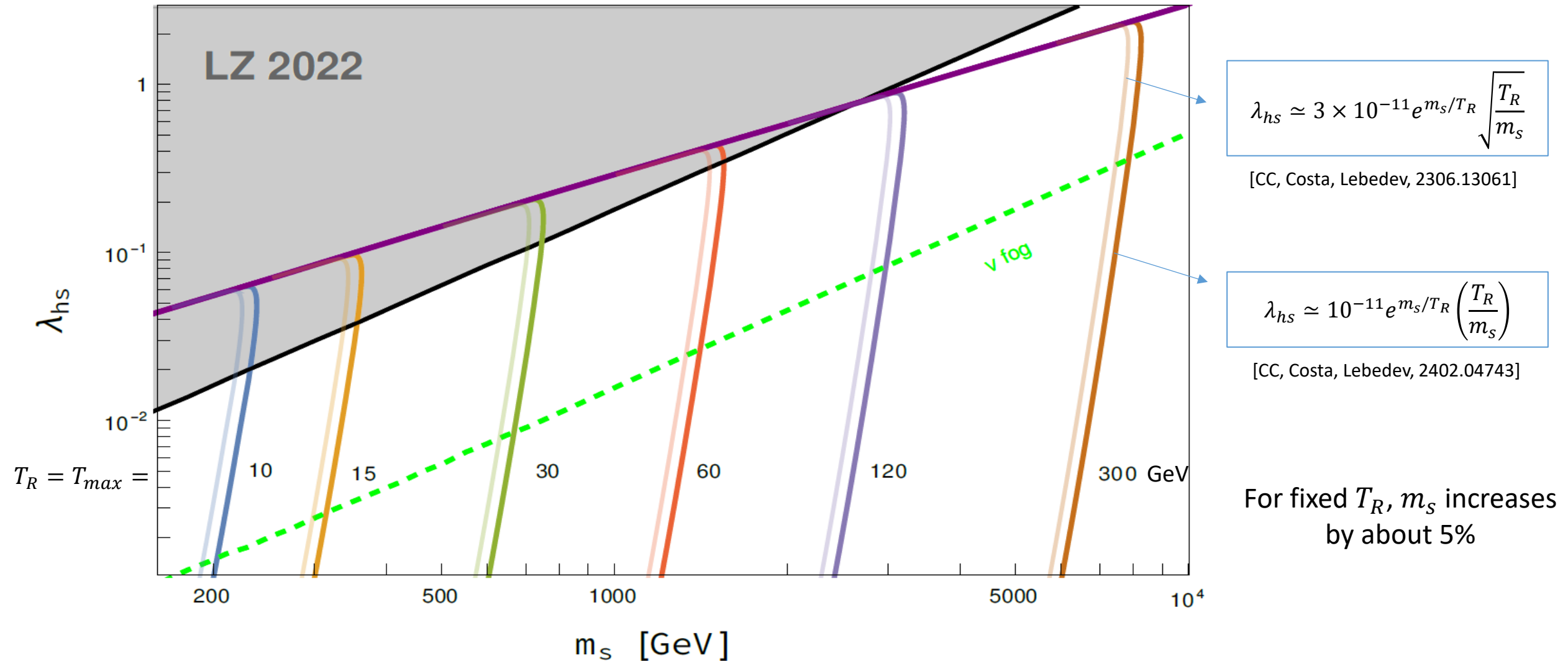
$$Y_{\text{new}} \simeq Y_{\text{old}}(T_{\text{max}}) \frac{m_s}{T_{\text{max}}}$$

in which  $T_R \rightarrow T_{\text{max}}$

# Phenomenology – Direct detection prospects



# Phenomenology – Direct detection prospects



# Conclusions

- **DM** can be **produced abundantly** via **gravity** in the early Universe;
- An **early matter** era leads to a **lower** reheating temperature ( $T_R$ ) and can **dilute DM** produced gravitationally;
- We have studied the **Higgs portal DM**, with DM being produced via **freeze-in**;
- If  $m_{DM} > T_R$ , freeze-in requires a **significant coupling**;
- This model **can already be tested** by **direct detection** experiments like LZ 2022;
- Further probes by XENONnT, DARWIN.

**Thank you for your attention! / Muito obrigada pela vossa atenção!**

Backup slides

# Oscillating scalar field as DM candidate

**Does an oscillating scalar field behave like non-relativistic matter?**

Potential:  $V(\phi) = \frac{1}{2} m_\phi^2 \phi^2$

Generic cosmological epoch:  $a(t) = \left(\frac{t}{t_i}\right)^p, p > 0.$  Hubble parameter:  $H = \frac{p}{t}$

Klein-Gordon (KG) eq. :

$$\ddot{\phi} + 3\frac{p}{t}\dot{\phi} + m_\phi^2 \phi = 0 \quad \xrightarrow{m_\phi t \gg 1} \quad \phi(t) \simeq \frac{\phi_i}{a(t)^{\frac{3}{2}}} \cos(m_\phi t + \delta_\phi)$$

Energy density:  $\rho_\phi = \frac{1}{2} \dot{\phi}^2 + V(\phi) \sim a^{-3} \quad \longrightarrow \quad \text{Non-relativistic matter.}$

# Oscillating scalar field as DM candidate

## When does it start to oscillate?

KG:

$$\ddot{\phi} + \underbrace{3H\dot{\phi}}_{\text{friction term}} + m_{\phi}^2 \phi = 0$$

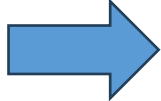
friction term

$H > m_{\phi} \Rightarrow$  Overdamped regime. No oscillations.

$H < m_{\phi} \Rightarrow$  Underdamped regime. The field oscillates.

# Gravitational annihilation of the inflaton during reheating

[Y. Ema, R. Jinno, K. Mukaida, K. Nakayama, 1502.02475]

Inflaton oscillations  Scale factor (a) and Hubble parameter oscillate

The scale factor  $a(t)$  is obtained by integrating  $\dot{a}/a = H = \langle H \rangle + \delta H$ :

$$a(t) \simeq \langle a(t) \rangle \left( 1 - \frac{1}{2(n+2)} \frac{\phi^2 - \langle \phi^2 \rangle}{M_P^2} \right), \quad \langle a(t) \rangle \simeq a_i \left( \frac{t}{t_i} \right)^{\frac{n+2}{3n}}$$

# Gravitational annihilation of the inflaton during reheating

[Y. Ema, R. Jinno, K. Mukaida, K. Nakayama, 1502.02475]

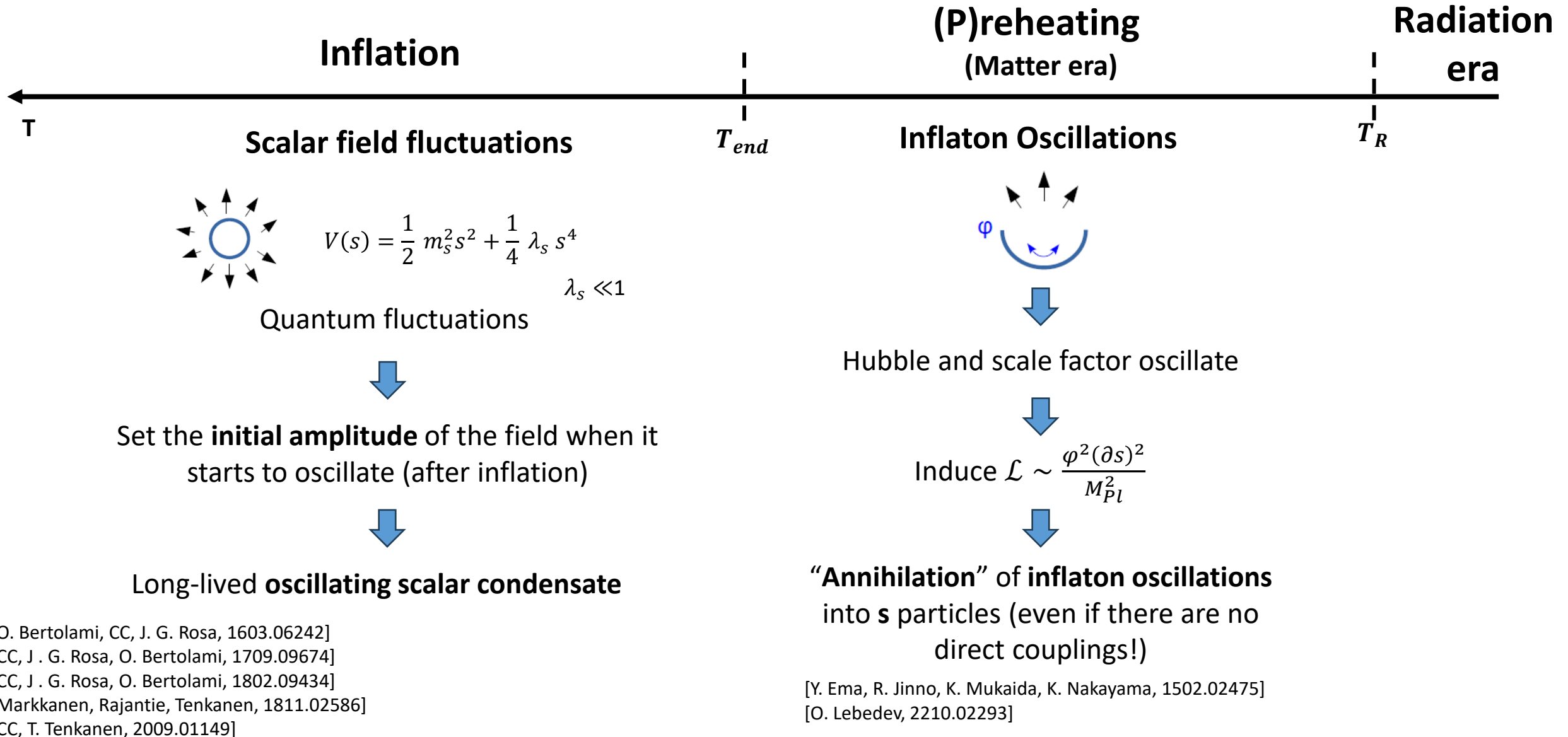
$$S_M = \int d^4x \sqrt{-g} \left[ -\frac{1}{2} g^{\mu\nu} \partial_\mu \chi \partial_\nu \chi - \frac{1}{2} m_\chi^2 \chi^2 \right], \quad (2.12)$$

where we assume  $m_\chi \ll m_\phi$ . As shown above, the scale factor and hence  $\sqrt{-g}$  contains  $\phi^2$  dependence. Therefore, neglecting terms including  $m_\chi$ , the action can be expanded as

$$S_M = \int d\tau d^3x \langle a(t) \rangle^2 \left( 1 - \frac{1}{n+2} \frac{\phi^2}{M_P^2} \right) \frac{1}{2} [\chi'^2 - (\partial_i \chi)^2], \quad (2.13)$$

where we have used the conformal time  $d\tau = dt/a(t)$  and the prime denotes derivative with respect to  $\tau$ . This explicitly shows that the inflaton  $\phi$  couples to  $(\partial\chi)^2$  and  $\phi$  (partially) “decays” or “annihilates” into  $\chi$  particles. According to the analysis of particle production under the oscillating background  $\phi$  [5,6], it might be interpreted as the annihilation of the inflaton into  $\chi$  particles. Thus we call this “gravitational annihilation” for convenience in the following.

# Particle Production Background - Examples



# Particle production background - Scalar fluctuations during inflation

- Quantum fluctuations for a massive field  $\left(\frac{m_\phi}{H_{inf}} < \frac{3}{2}\right)$ :

$$|\delta\phi_k| \simeq \frac{H_{inf}}{\sqrt{2k^3}} \left(\frac{k}{aH_{inf}}\right)^{\frac{3}{2}-\nu_\phi}$$

Integrating over all super-horizon  
modes



$$\langle\phi^2\rangle \simeq \frac{1}{3-2\nu_\phi} \left(\frac{H_{inf}}{2\pi}\right)^2$$

$$\nu_\phi = \left(\frac{9}{4} - \frac{m_\phi^2}{H_{inf}^2}\right)^{\frac{1}{2}}$$

- Quantum fluctuations for a massive field  $\left(\frac{m_\phi}{H_{inf}} > \frac{3}{2}\right)$ :

$$|\delta\phi_k|^2 \simeq \left(\frac{H_{inf}}{2\pi}\right)^2 \left(\frac{H_{inf}}{m_\phi}\right) \frac{2\pi^2}{(aH_{inf})^3}$$

Integrating over all super-horizon  
modes



$$\langle\phi^2\rangle \simeq \frac{1}{3} \left(\frac{H_{inf}}{2\pi}\right)^2 \left(\frac{H_{inf}}{m_\phi}\right)$$

# Particle Production background - Quantum gravity effects

- Quantum gravity is believed to induce all operators consistent with gauge symmetry (including Planck-suppressed couplings between the inflaton and DM)

$$\Delta\mathcal{L}_6 = \frac{C_1}{M_{\text{Pl}}^2} (\partial_\mu\phi)^2 s^2 + \frac{C_2}{M_{\text{Pl}}^2} (\phi\partial_\mu\phi)(s\partial^\mu s) + \frac{C_3}{M_{\text{Pl}}^2} (\partial_\mu s)^2 \phi^2 - \frac{C_4}{M_{\text{Pl}}^2} \phi^4 s^2 - \frac{C_5}{M_{\text{Pl}}^2} \phi^2 s^4$$



Lead to **particle production** during the **inflaton oscillation epoch** and can produce **excessive abundance of stable scalars**

Most efficient in  
particle production:

$$\frac{C_4}{M_{\text{Pl}}^2} \phi^4 s^2$$

# Particle Production background – Dilution factors

During inflation:

$$\Delta_{\text{NR}} \gtrsim 10^7 \lambda_s^{-3/4} \left( \frac{H_{\text{end}}}{M_{\text{Pl}}} \right)^{3/2} \left( \frac{m_s}{\text{GeV}} \right)$$

Inflaton oscillation:

$$m_s \lesssim 10^{-6} \Delta_{\text{NR}} \left( \frac{M_{\text{Pl}}}{H_{\text{end}}} \right)^{3/2} \text{ GeV}$$

Quantum gravity:

$$\Delta_{\text{NR}} \gtrsim 10^{17} C^2 \frac{m_s}{\text{GeV}}$$

# The model – DM production inefficient

Real scalar dark matter  $s$  through the **Higgs portal**

$$V(s) = \frac{1}{2} \lambda_{hs} s^2 H^\dagger H + \frac{1}{2} m_s^2 s^2$$

DM number density,  $n$ :

$$\dot{n} + 3Hn = \Gamma(h_i h_i \rightarrow ss) - \Gamma(ss \rightarrow h_i h_i)$$

$$\Gamma(ss \rightarrow h_i h_i) \simeq \frac{\lambda_{hs}^2}{64 \pi m_s^2} n^2$$

$$\underbrace{\hspace{1.5cm}}_{\langle \sigma(ss \rightarrow h_i h_i) v_r \rangle}$$



$$\lambda_{hs,*} \simeq 90 e^{m_s/(2T_R)} \sqrt{\frac{m_s}{M_{Pl}}}$$

Critical coupling

# SM sector production via $\nu_R$ decay

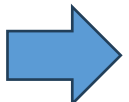
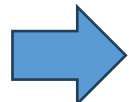
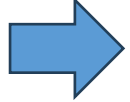
Evolution of the energy density of the Universe:

$$\dot{\rho}_\varphi + 3H\rho_\varphi = -\Gamma_\varphi\rho_\varphi$$

$$\dot{\rho}_\nu + 4H\rho_\nu = \Gamma_\varphi\rho_\varphi - \Gamma_\nu\rho_\nu$$

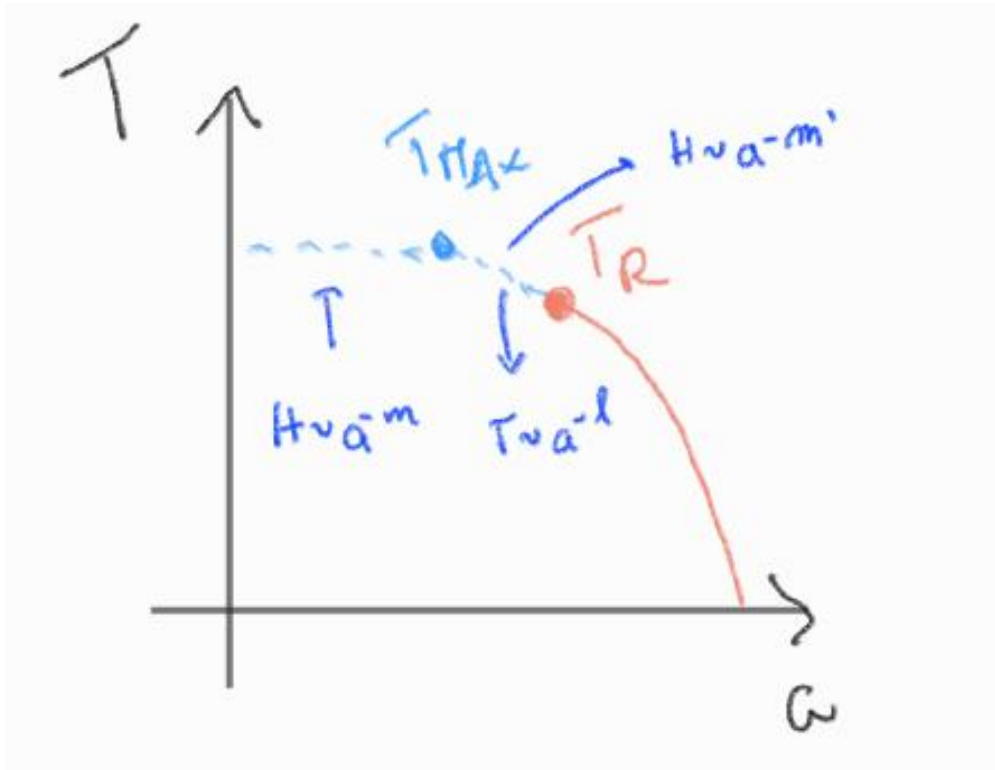
$$\dot{\rho}_{SM} + 4H\rho_{SM} = \Gamma_\nu\rho_\nu$$

$$\rho_\varphi + \rho_\nu + \rho_{SM} = 3H^2 M_{Pl}^2$$

If  $\Gamma_\varphi \sim \Gamma_\nu$    $\varphi$  and  $\nu$  decay at the same time  SM sector takes over the energy balance immediately thereafter   $T_{max} \simeq T_R$

$$T_{max} > T_R$$

In the limit  $m_s \gg T_{max}$

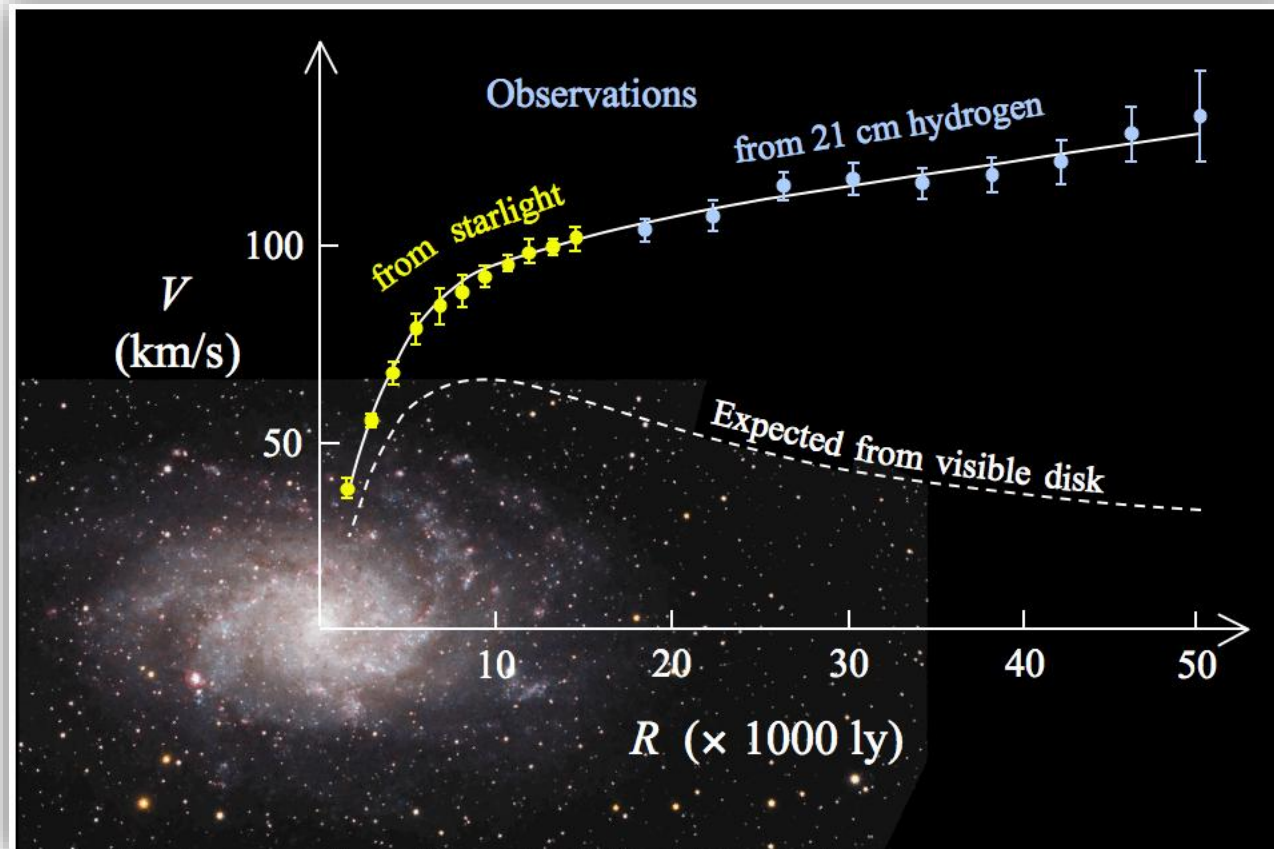


$$\lambda_{hs} \rightarrow \lambda_{hs} \times \left( \frac{T_{max}}{T_R} \right)^{\frac{m'+3-5l}{2l}}$$

# Introduction – Why do we think that dark matter exists?

- **Evidence** for dark matter (DM) come from different sources:

## Galaxy Rotation curves



$$m \frac{v(r)^2}{r} = \frac{GmM(r)}{r^2}$$



$$v(r) = \sqrt{\frac{GM(r)}{r}}$$

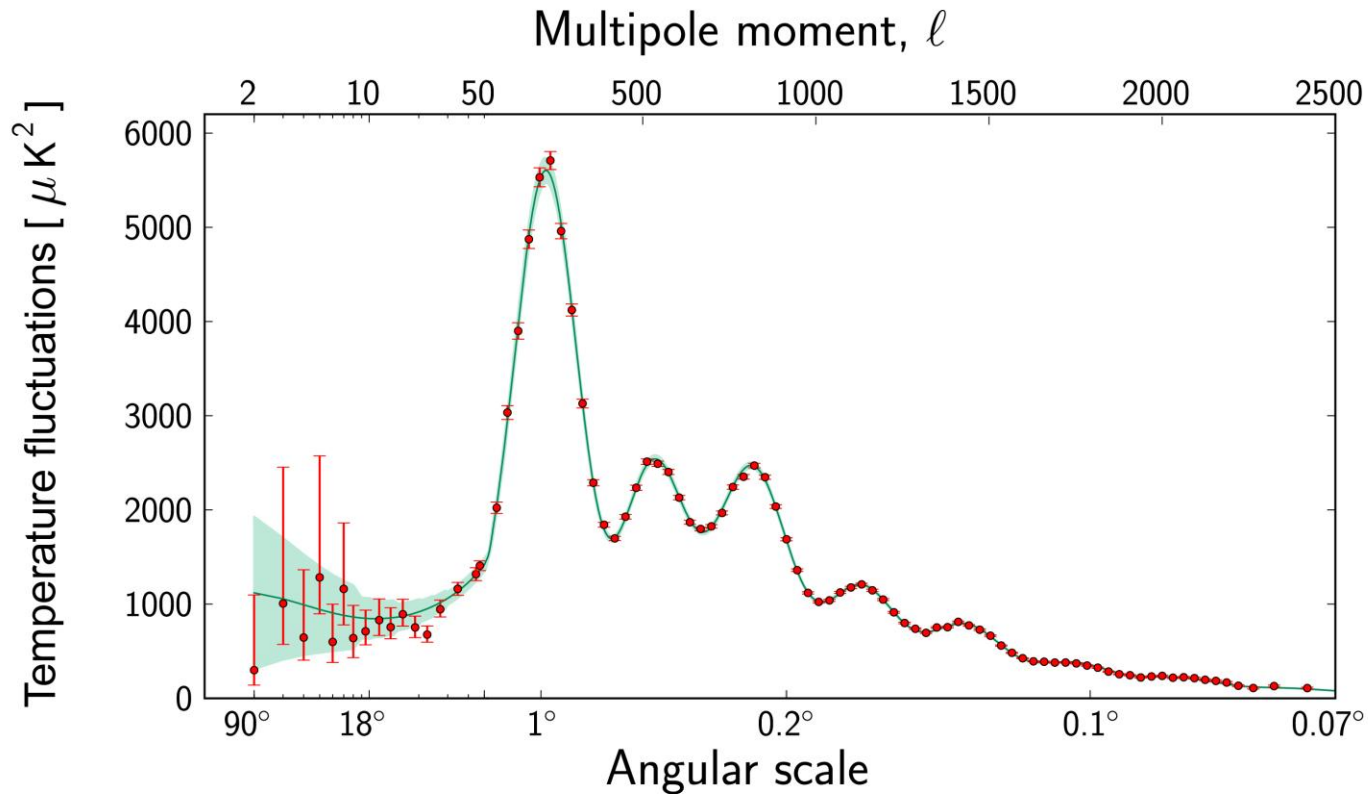
Since  $v(r)$  seems to be constant in the halo, this means that  $M(r) \sim r$ .

Credits: Mark Whittle, University of Virginia

# Introduction – Why do we think that dark matter exists?

- **Evidence** for dark matter (DM) come from different sources:

## Baryon Acoustic Oscillations of the Cosmic Microwave Background (CMB)

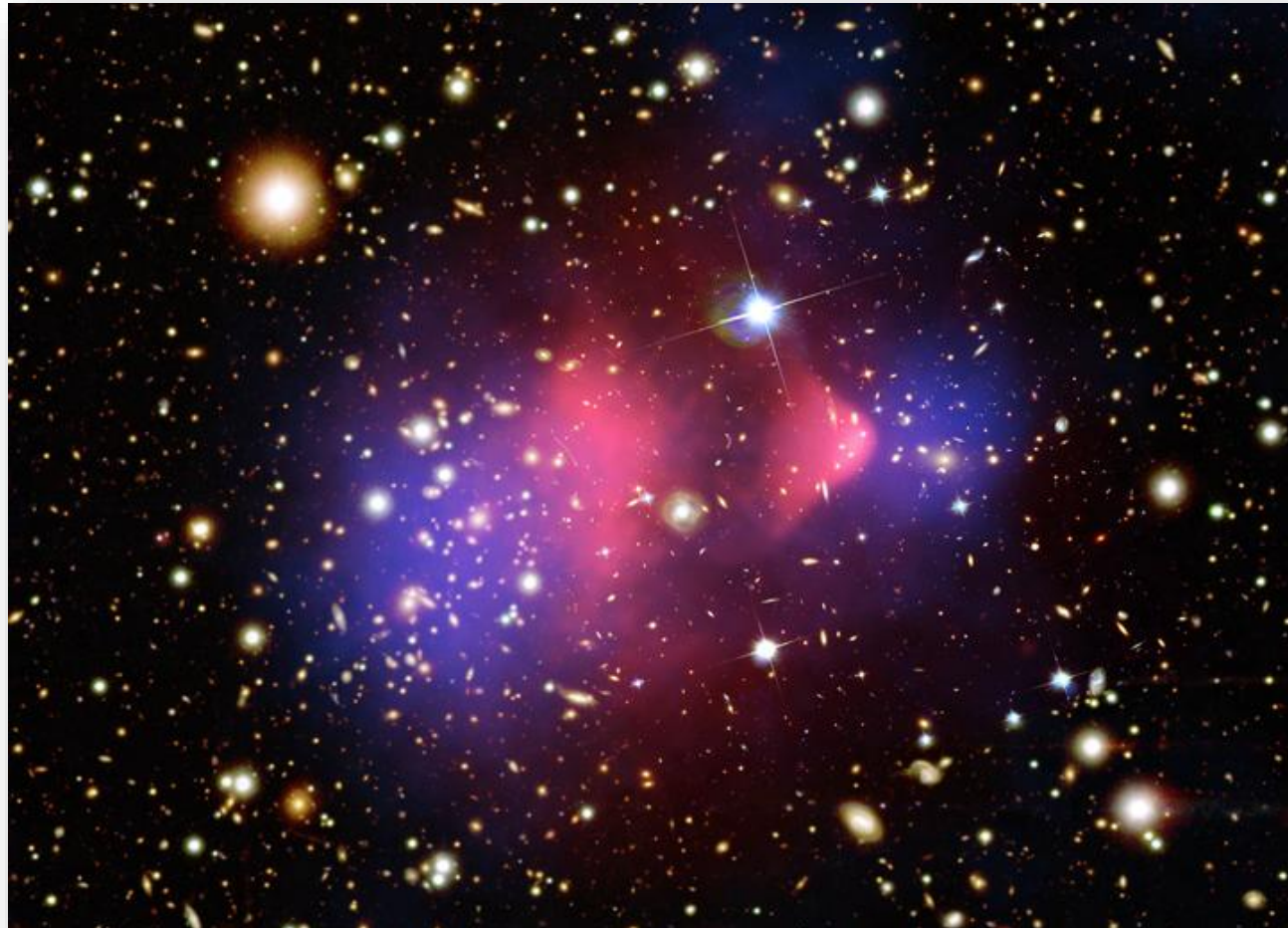


Credits: Planck Collab.

# Introduction – Why do we think that dark matter exists?

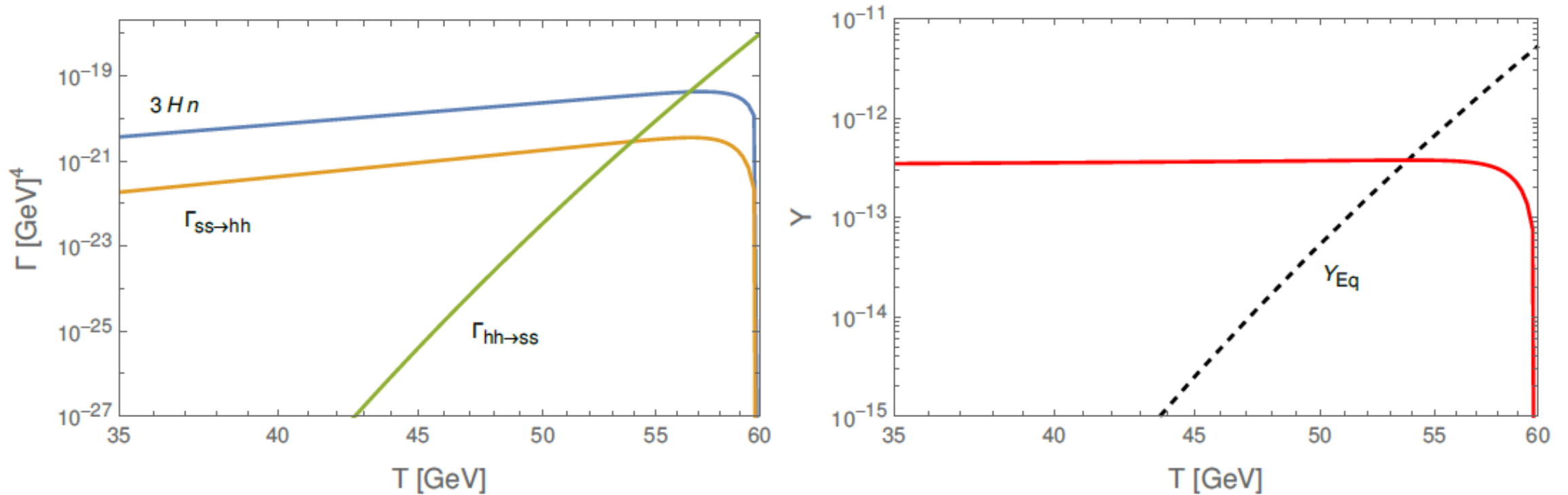
- **Evidence** for dark matter (DM) come from different sources:

## Bullet Cluster, gravitational lensing



Credits: NASA.

# Phenomenology – Reaction rates



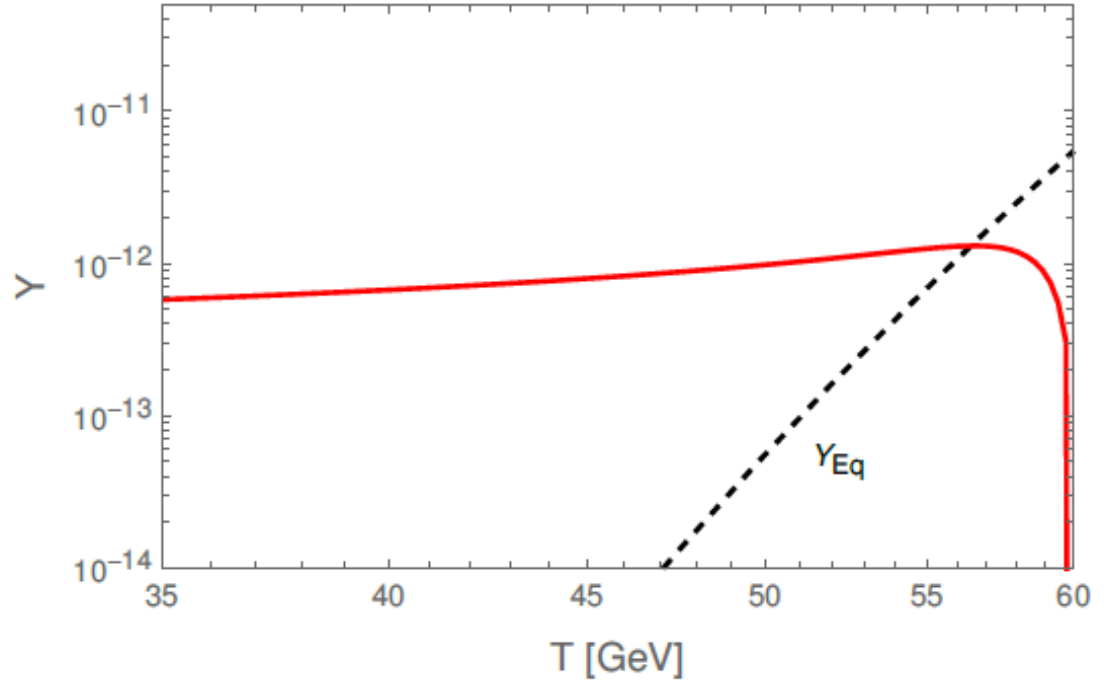
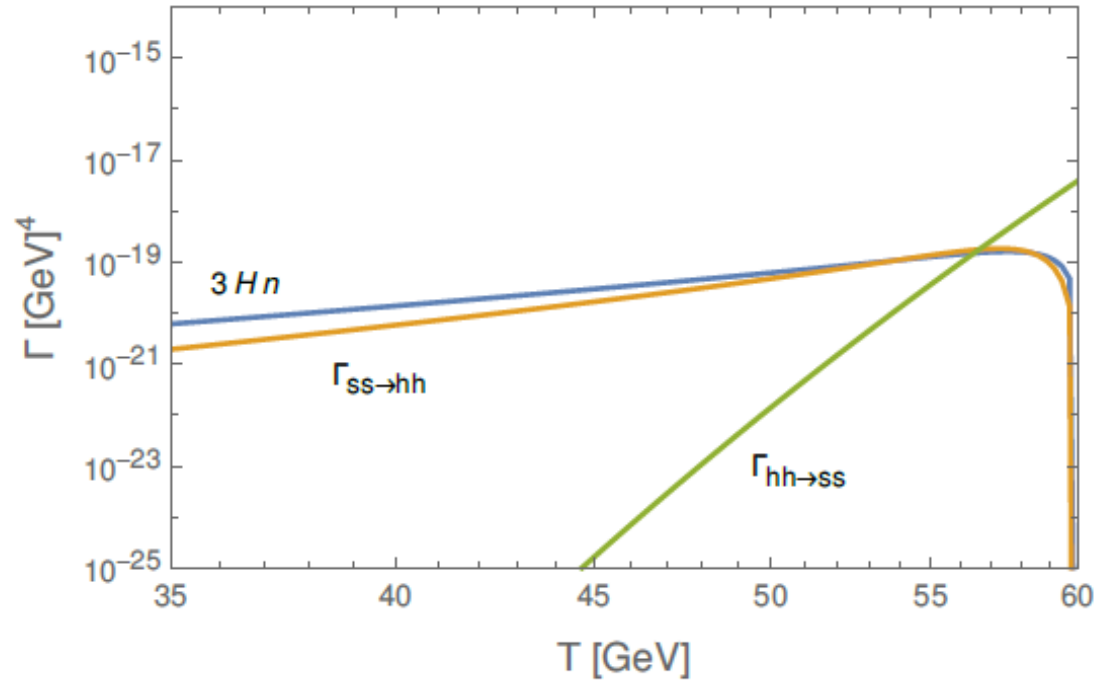
$$T_R = 60 \text{ GeV}, m_s = 1453 \text{ GeV}, \lambda_{hs} = 0.2$$

Annihilation rate is never significant



Freeze-in regime

# Phenomenology – Reaction rates



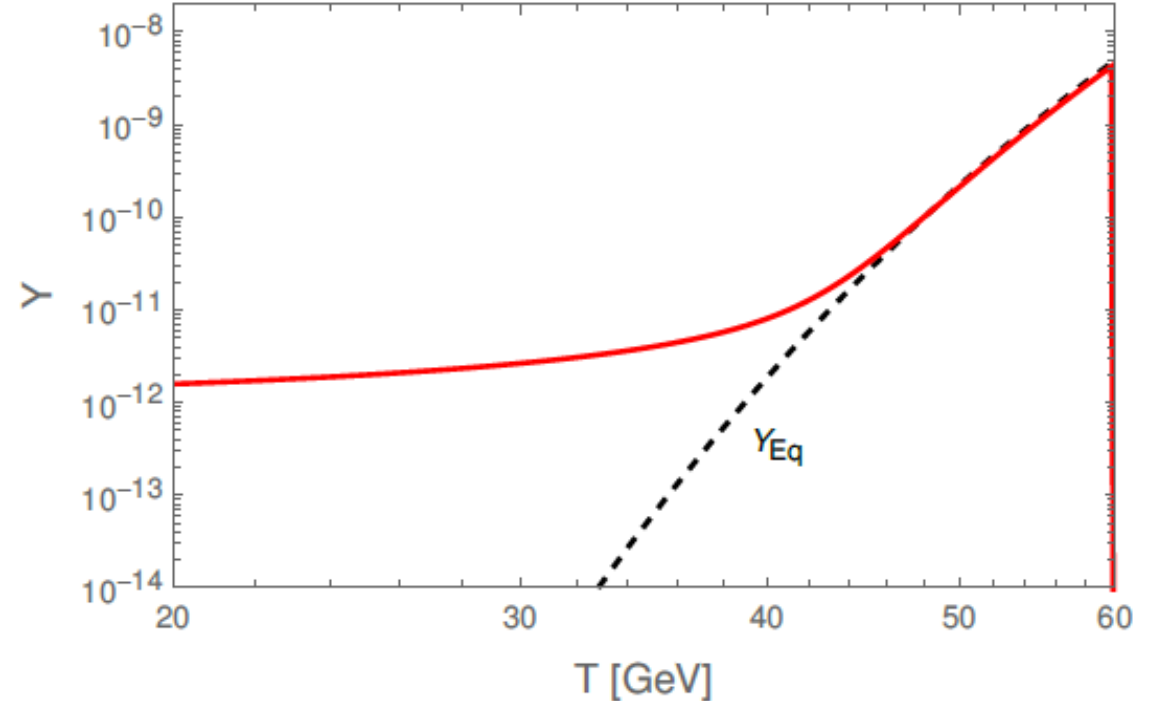
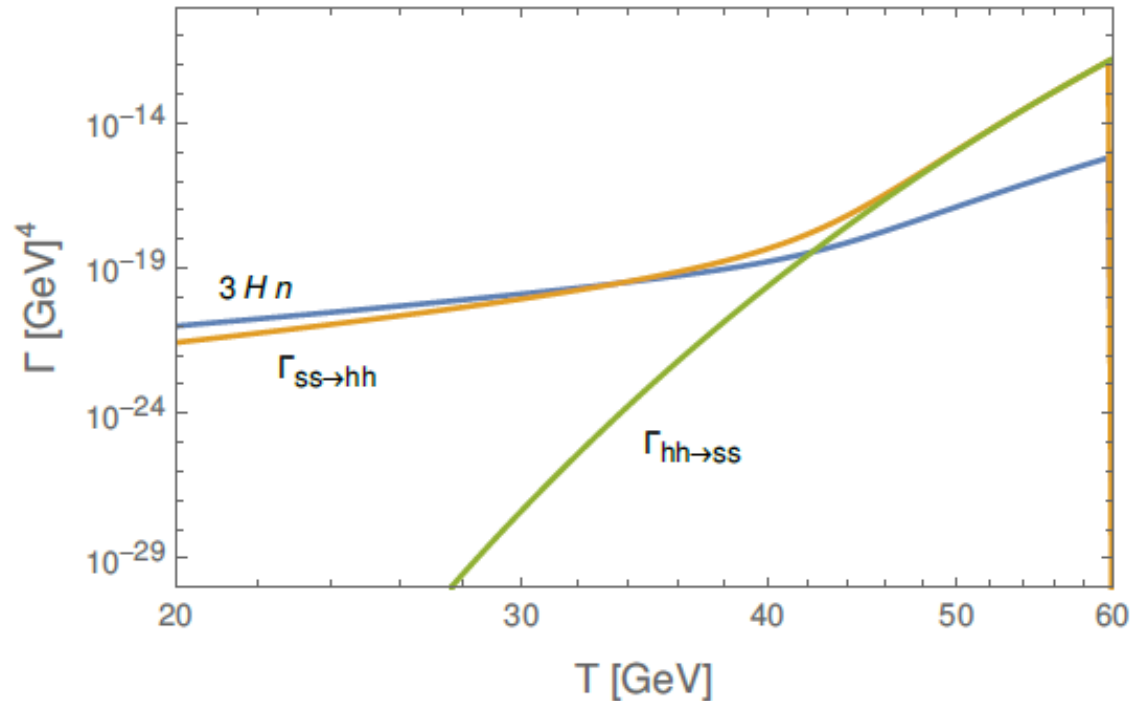
$$T_R = 60 \text{ GeV}, m_s = 1451 \text{ GeV}, \lambda_{hs} = 0.39$$

Annihilation rate is significant for some time



Freeze-in close to Freeze-out regime

# Phenomenology – Reaction rates



$$T_R = 60 \text{ GeV}, m_s = 1012 \text{ GeV}, \lambda_{hs} = 0.297$$

Annihilation rate = production rate  
for some time – system thermalizes



Freeze-out regime